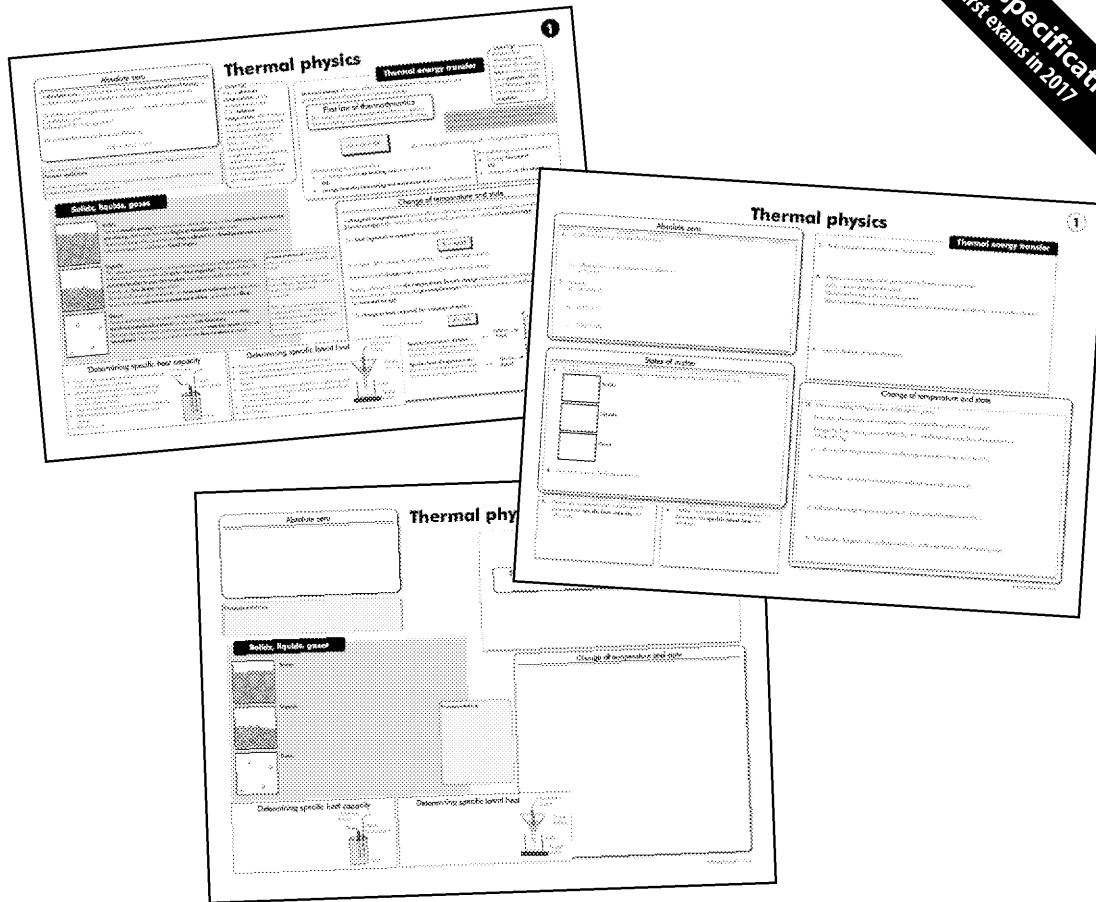


2015 specification  
first exams in 2017



# Topic on a Page

For A Level Year 2 OCR Physics A

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# Teacher's Introduction

This topic-on-a-page resource has been designed to help your students revise the test their knowledge after you have taught each section of the **OCR A Level Year 2** modules 5 and 6. Each page is closely tied to the OCR specification, ensuring all is covered. Activity pages are designed to be complementary to OCR A Level Topic Education, so students won't be repeating the same questions.

There are four sections to this resource, each with its own features:

1. **Topic-on-a-page sheets:** these are the main pages which intend to clearly consolidate and recap all the key information from Year 2 of the OCR A Physics course.
2. **Activity pages:** these are identical to the Topic-on-a-page sheets, but contain a variety of tasks, from filling in missing words to performing calculations. The activity pages aim to ensure that the student understands all the key knowledge required of them and give them the opportunity to demonstrate how well they have remembered and understood the content of the course.
3. **Outline pages:** these are the Topic-on-a-page sheets, but with most of the content removed. Students can research the topics, e.g. for homework, and bring in as much information as they can.
4. **Mark scheme:** full answers for the activity pages.

The 'topic-on-a page', 'activity' and 'outline-only' sheets are designed to be A3 size at A4 with no loss of detail. When photocopying activity pages on A3, we suggest a worksheet on the reverse. If using at A4 size, we suggest photocopying each A3 sheet as a double-sided A4 page to avoid shrinking the space available for answers.

Each page presents information in a variety of ways, including:

- **Bold key words** – essential terminology in bold, allowing students to skim and scan
- **Bullet point processes** – complex processes and lists have been summarised
- **Graphs** – sketch graphs illustrate complex points without providing unnecessary detail
- **Comparison tables** – a quick way of comparing key features of different structures
- **Method and calculation boxes** – concisely state the equations used in required calculations
- **Exam tips** – aid memorisation, revision and exam technique in areas where students struggle

We hope you find these pages useful during your teaching and your students' revision.

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\* resulting from minor specification changes, suggestions from teachers and peer reviews, or occasional errors reported by customers

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## Absolute zero

At **absolute zero** (-273 °C) an object will have **minimum internal energy** as the kinetic energy of the molecules will have been brought down to zero.

The Kelvin scale of temperature is an absolute scale of temperature, with 0 K at absolute zero.

A change of 1 K = a change of 1 °C.

The relationship between kelvin and Celsius is:

$$T(K) \approx \theta(^{\circ}C) + 273$$

If two or more objects or systems are at the same temperature, they are said to be in **thermal equilibrium**.

If two or more systems can exchange energy or mass between each other, they will tend towards thermal equilibrium over time.

# Thermal physics

### Exam Tip!

$T$  is an **absolute temperature**, and is measured in kelvins.

$\theta$  is a **relative temperature**, which relates to a specific reference point.

For Celsius, this reference point is the triple point of water at 0 °C or 273 K.

Always use absolute temperatures for calculations, but if it's a change in temperature, in which case relative temperatures will give the same value.

**Internal energy:** the potential energies of

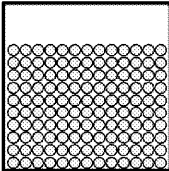
### First law

The change of internal energy is equal to the total energy transferred to or from the system.

Internal energy is conserved.

- no energy transfer
- OR
- energy transferred

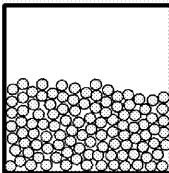
## Solids, liquids, gases



### Solids

There is **small spacing** between atoms and molecules, so the **intermolecular forces are strong**, and solids have the **highest densities** of any state.

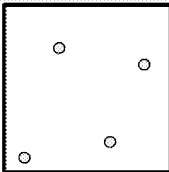
Atoms and molecules in solids are **very ordered** have **fixed positions** which they vibrate around, so solids have **fixed shapes**.



### Liquids

The spacing between atoms and molecules is greater in liquids than in solids, but the spaces are still **quite close together**. Because of this, the **intermolecular forces are weaker**, but still relatively strong, and liquids are **less dense** than solids.

Atoms and molecules in liquids are **somewhat ordered** and can't move much, but they **can move around each other**, so liquids can **flow**.



### Gases

Atoms and molecules in gases are very far apart, so they have **very weak intermolecular forces** and have **low densities**.

Because the atoms and molecules in gases are **very far apart**, they are **unordered**. The atoms and molecules are **free to move** around.

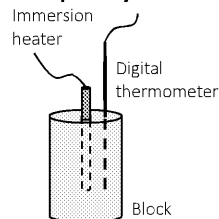
**Brownian motion** describes the erratic motion of a small particle in a fluid.

The molecules in the fluid move randomly and hit into the particle, making the particle move randomly.

This can be seen in smoke particles suspended in air – rather than remaining stationary, they are moving in one direction, but appear to move in all directions.

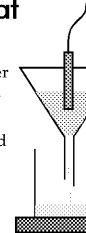
## Determining specific heat capacity

- Place immersion heater and digital thermometer in block or beaker of substance
- Heat block and record the energy transferred using the power rating of the heater and the amount of time elapsed
- Measure temperature of block at regular intervals
- Plot energy transferred against temperature change
- Gradient is  $mc$



## Determining specific latent heat

- Place immersion heater in a funnel filled with ice
- Heat ice, determining energy from the power of the heater
- At regular intervals, measure the mass of the water in the beaker
- Compare mass to a control set-up, which is unheated, and the mass of the water from this beaker is subtracted from the mass of the melted ice
- Plot energy transferred against mass of melted water
- Gradient is  $L$



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A change in kinetic energy

The heat

$m =$

A substance

During

remains

The change

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# Ideal gases

## Ideal gas laws

**Gas laws:** a set of **experimental** laws that look at the relationship between pressure, volume and temperature of a gas.

**Molar mass:** the mass of one mole of substance in  $\text{kg mol}^{-1}$

**Molecular mass:** the mass of a molecule in u (atomic mass unit)

Ideal gas law:

$$\frac{pV}{nT} = \frac{pV}{NkT}$$

The pressure law  
(constant volume):

$$\frac{p}{T} = \text{constant}$$

Charles' law  
(constant pressure):

$$\frac{V}{T} = \text{constant}$$

Boyle's law  
(constant temperature):

$$pV = \text{constant}$$

Work done on a gas:

$$W = p\Delta V$$

**Avogadro's constant** ( $N_A$ ) is the number of atoms in 12 g of carbon isotope  $^{12}_6\text{C}$ .

An isotope's or chemical's **molar mass** describes how much mass is in  $N_A$  **molecules** of that chemical.

The **Boltzmann constant** (**k**) is related to Avogadro's constant

$$\text{by } k = \frac{R}{N_A}$$

$p$  = pressure of the gas  
 $V$  = volume of the gas  
 $T$  = temperature of the gas  
 $n$  = number of moles in a gas  
 $N$  = number of molecules in a gas  
 $W$  = work done on the gas  
 $N_A$  = Avogadro's constant =  $6.02 \times 10^{23} \text{ mol}^{-1}$   
 $R$  = gas constant =  $8.31 \text{ J K}^{-1} \text{ mol}^{-1}$   
 $k$  = Boltzmann constant =  $\frac{R}{N_A} = 1.38 \times 10^{-23} \text{ J K}^{-1}$

## Molecular kinetic theory model

The molecular kinetic theory applies the gas laws to **individual molecules**. Molecules in a fluid are in **constant random, rapid motion**.

The kinetic theory is based on a statistical mathematical model, so only applies to large numbers of particles.

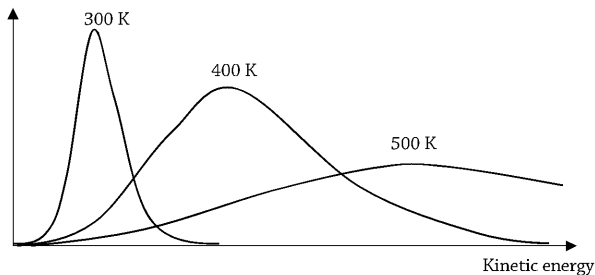
### Kinetic theory equation

The kinetic theory equation gives the pressure of an ideal gas in terms of the **root mean square velocity** of the particles in the gas. Root mean square velocity is a way of taking an average of all the speeds of the particles.

$$p = \frac{Nm\overline{c^2}}{3V}$$

$\overline{c^2}$  = root mean square velocity

Number of particles



The **Maxwell-Boltzmann distribution** shows the number of particles with a given kinetic energy. At higher temperatures, there are still particles with lower kinetic energies, but there are far more particles with higher kinetic energies so the average kinetic energy is higher overall.

$M_c$

Pressure law:

Charles' law:

Boyle's law:

Average molecular kinetic energy

Internal energy of an ideal gas

For an ideal gas, the internal energy is directly proportional to the absolute temperature.

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## Circular motion

For an object to move with **circular motion** the object must continually deviate from its straight line direction and, therefore, continuously **change its velocity**.

This implies that there is acceleration, and to accelerate a force must be exerted on the object.

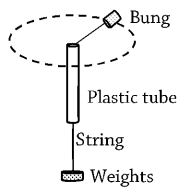
The force that causes an object to maintain circular motion is called a **centripetal force**.

The centripetal force **always** acts towards the **centre** of rotation.

A relationship between radians and degrees is:

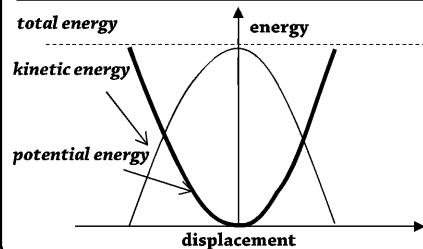
$$\text{radians} = \text{degrees} \times \frac{\pi}{180}$$

### Investigating circular motion



- Mark a point on the string
- Hold the plastic tube and 'whirl' the bung around
- Vary the speed until the mark just appears
- Measure the time for 10 rotations of the bung and determine the speed of the bung
- Add weights and repeat

### Energy-displacement graphs of SHM for free oscillations



The **total energy** of a simple harmonic system is constant. At minimum displacement, speed is at a maximum and so **kinetic energy** is maximum. Kinetic energy is converted to **potential energy** as displacement increases.

## Periodic motion

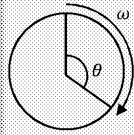
### Angular quantities

Angular velocity:  $\omega = \frac{v}{r} = 2\pi f$

Centripetal acceleration:  $a = \frac{v^2}{r} = \omega^2 r$

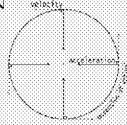
Centripetal force:  $F = \frac{mv^2}{r} = m\omega^2 r$

**These equations are in the data booklet!**



For constant speed in a circle  
 $v = \omega r$

$v$  = linear speed, in  $\text{m s}^{-1}$   
 $r$  = radius of circular path, in  $\text{m}$   
 $\omega$  = angular velocity, in  $\text{rad s}^{-1}$   
 $f$  = frequency, in  $\text{Hz}$   
 $a$  = centripetal acceleration, in  $\text{m s}^{-2}$   
 $F$  = centripetal force, in  $\text{N}$



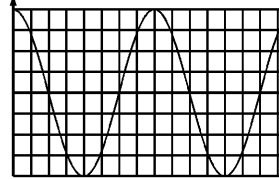
An object with an **angular frequency** (sometimes called angular speed),  $\omega$ , of  $1 \text{ rad s}^{-1}$  moves through one radian of a circle in one second.

For a circle of a radius of  $2\pi$  metres, this corresponds to moving 1 m around the circumference of the circle.

An object that goes around an entire circle in 1 s has  $\omega = 2\pi \text{ rad s}^{-1}$ .

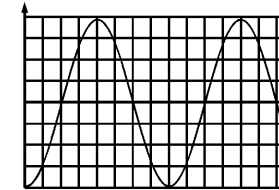
**Simple harmonic motion** is which acceleration is **proportional** and **opposing in direction** to

Displacement/m



$$\text{displacement} = x = A \cos \omega t$$

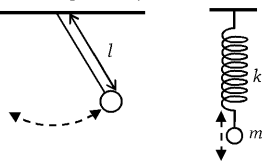
Acceleration/ $\text{m s}^{-2}$



$$\text{acceleration} = a = -A \omega^2 \cos \omega t$$

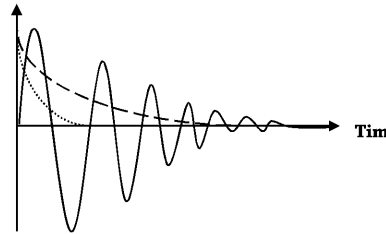
### Investigating simple harmonic motion

- For a spring-mass system or pendulum:



- Mark the equilibrium position of the system
- Move the mass away from its equilibrium position
- Measure the time for 10 oscillations past the marker
- Divide by 10 for the period of one oscillation

Amplitude



### Damped oscillations

Oscillations of systems will eventually **lose their amplitude** due to resistance from friction or air resistance.

**Light damping:**



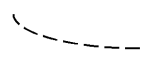
the time period is **independent** and, therefore, each wave cycle of time for oscillations to decrease.

**Critical damping:**



the **minimum amount of damping** to stop over the course of one oscillation to stop over the course of one oscillation.

**Heavy damping:**



damping that is **stronger than critical damping** and causes the system to return to equilibrium over a **longer amount of time** than critical damping.

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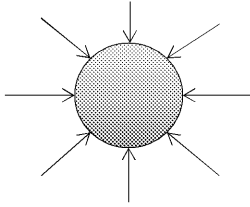
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## Gravitational fields

Gravitational fields are generated by all masses, and affect all masses.

**Radial field:** A field that is spherical and **acts towards a central point**. Gravitational fields are radial. A radial gravitational field around a planet can be seen to the right.



**Uniform field:** A field that has **no variation**. Gravitational fields are approximated as uniform near the surface of planets.

In the case of gravitational fields, a **field line** gives the path that a smaller mass takes towards a larger mass due to the force of gravity. A higher density of field lines shows a stronger gravitational field, and a stronger force that a mass will experience.

### Exam Tip!

A spherical object can be treated as a point particle with its entire mass at its centre.

## Gravitational field strength

The gravitational field strength,  $g$ , is the force,  $F$ , per unit mass,  $m$ , on an object in a uniform gravitational field.

$$g = \frac{F}{m}$$

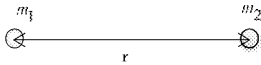
The gravitational field strength of the Earth near the surface is  $9.81 \text{ N kg}^{-1}$ .

The magnitude for  $g$  in a radial field is:

$$g = \frac{GM}{r^2}$$

## Newton's law of gravitation

Gravity is the universal attractive force that acts between all matter.



Newton determined the **force of gravitation** between two masses to be:

$$F = \frac{Gm_1m_2}{r^2}$$

- So the force due to gravity
- increases with mass
  - decreases with distance

$F$  = force due to gravity  
 $G$  = gravitational constant  
 $= 6.67 \times 10^{-11} \text{ N m}^2 \text{ kg}^{-2}$   
 $m_1$  = mass of object 1  
 $m_2$  = mass of object 2  
 $r$  = distance between centres of mass

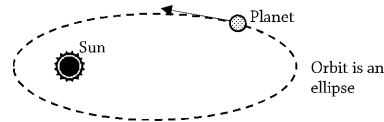
# Gravitational fields

## Kepler's laws of planetary motion

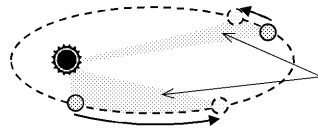
Kepler's laws describe the motion of orbiting bodies, such as planets around the Sun.

Kepler's laws are:

1. A planet orbits the Sun in an elliptical orbit, with the Sun at one of the focal points of the orbit.



2. The area swept out by a line connecting the Sun and a planet sweeps out a constant area in a given time.



This shows the movement of the planet during two equal periods of time. Planet travels faster when closer to the Sun, so that both shaded areas are of equal size.

3. The period of a planet's orbit squared is proportional to the average radius of the planet's orbit cubed, or:

$$T^2 \propto r^3$$

$$T^2 = \left(\frac{4\pi^2}{GM}\right)r^3$$

### Derivation of Kepler's third law

$$F_{\text{centripetal}} = F_{\text{gravitational}}$$

$$\frac{mv^2}{r} = \frac{GMm}{r^2}$$

$$v^2 = \frac{GM}{r}$$

$$\left(v = \frac{2\pi r}{T}\right)$$

$$\frac{4\pi^2 r^2}{T^2} = \frac{GM}{r}$$

$$T^2 = \left(\frac{4\pi^2}{GM}\right)r^3$$

Kepler's laws apply to any orbital system, such as moons or galaxies.

For orbiting bodies, the centripetal force allowing orbit to occur is the gravitational force of the body at the centre of the orbit.

## Geostationary satellites

A **geostationary satellite** is a satellite that has an **orbital period** around Earth equator of **one day** (24 hours).

Since the rotational period is also 24 hours, then the satellite stays at a **fixed position** above Earth's equator.

The distance of a geostationary satellite above Earth can be found using **Kepler's third law** derived above.

Geostationary satellites are used in **communications** and **navigation systems**, such as the satnav that is used in cars.

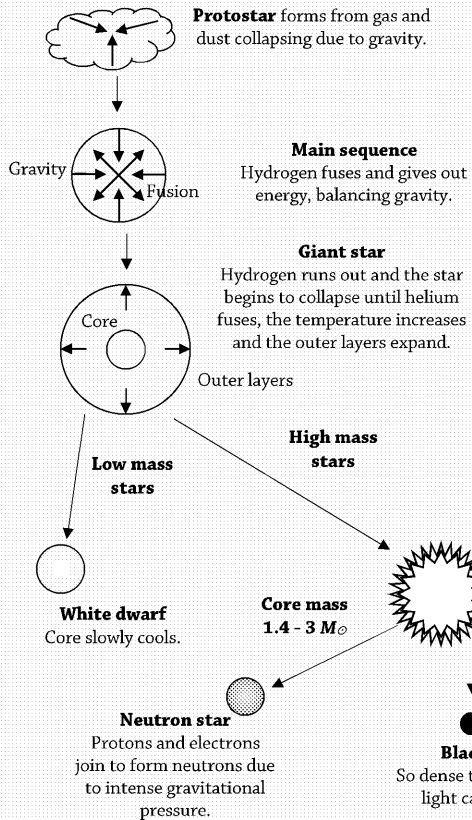
Geostationary satellites have to orbit at a set distance so that their centripetal acceleration is equal to the acceleration to gravity. This can be found by equating the two.

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## Life cycle of a star



## The deaths of stars

### White dwarfs

A white dwarf is the leftover core of a star, with a mass of up to  $1.4 M_{\odot}$ . This mass is known as the **Chandrasekhar limit**. This is the incredibly **hot core** of the star, formed once all the fuel has been used up and the outer layers of a red giant are thrown out into space. No fusion occurs, but the core does not collapse. This is because the core is supported by **electron degeneracy pressure** – the repulsive forces between electrons stopping them getting any closer together.

### Supernovae

Higher mass stars undergo a **supernova** stage – an incredibly bright explosion when the star collapses in on itself, which triggers fusion of elements heavier than iron.

After a supernova, the core left behind can be either a **neutron star** or a **black hole**.

### Neutron stars

If the core left over after a supernova has a mass of  $1.4 \times$  to  $3.0 \times$  solar masses, it forms a neutron star, with a radius of about 10 km. In the core of a neutron star, gravity is so great that protons and electrons are forced together to become neutrons.

### Black holes

If the core left over is heavier than  $3 \times$  solar masses, it forms a black hole. A black hole produces such a strong gravitational field that nothing can escape, not even light. The surface around a black hole from which nothing can escape is called the event horizon.

Giant stars are large and bright. The cooler **red giants** fuse helium in their cores, and form after main sequence stars run out of hydrogen. Hotter **supergiants** are higher mass giant stars.

## The Hertzsprung–Russell (HR) diagram

A diagram showing stars categorised by temperature and brightness. Stars fall into several groups on the Hertzsprung–Russell diagram.

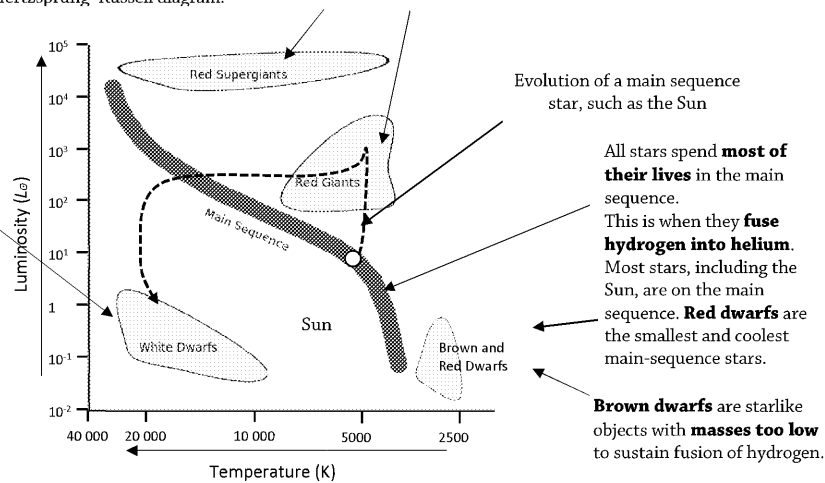
**White dwarfs** are the incredibly hot cores of stars which **no longer undergo fusion**.

White dwarfs gradually cool and radiate all their heat, and become black dwarfs.

### Exam Tip!

The x-axis is logarithmic and decreases in temperature from left to right.

The y-axis is measured in terms of our Sun's luminosity ( $L_{\odot}$ ), which increases in brightness going up the axis.



All stars spend **most of their lives** in the main sequence. This is when they **fuse hydrogen into helium**. Most stars, including the Sun, are on the main sequence. **Red dwarfs** are the smallest and coolest main-sequence stars.

**Brown dwarfs** are starlike objects with **masses too low** to sustain fusion of hydrogen.

# Stars

## Absorption

Energy energy

Ionisation

$n = 3$

$n = 2$

$n = 1$

$n = 1$

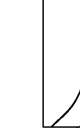
Phot layer abso

Emission by elect line spe electron

## Black-body

- Any object radiates
- Hot objects radiate more
- A black body is a perfect absorber and emitter of radiation
- A star is a black body

Power/W



## Wien

$\lambda_{max}$

## Example

The Sun of power

$$T = \frac{2.9 \times 10^{-3}}{\lambda} = \frac{L}{4\pi r^2} = \epsilon$$

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# Cosmology

## Distances in astrophysics

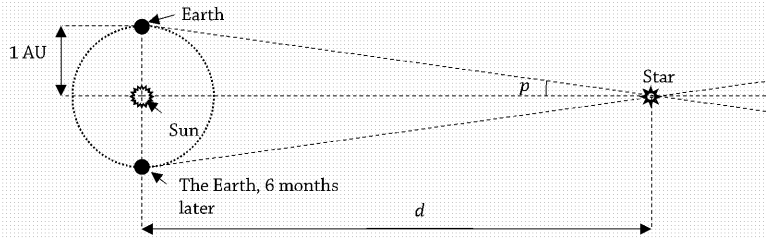
When discussing objects in space, units like metres and kilometres start to become unhelpful, as they're so much smaller than the distances we want to talk about! Instead we use units like **astronomical units**, **light years** and **parsecs**.

$$\begin{aligned} 1 \text{ AU} &= 1.50 \times 10^{11} \text{ m} \\ 1 \text{ ly} &= 9.46 \times 10^{15} \text{ m} \\ 1 \text{ pc} &= 3.08 \times 10^{16} \text{ m} \\ 1 \text{ pc} &= 2.06 \times 10^5 \text{ AU} = 3.26 \text{ ly} \end{aligned}$$

- Astronomical unit (AU):** The distance between the Earth and the Sun  
**Light year (ly):** The distance travelled by light in a year  
**Parsec (pc):** The distance to a star that subtends an angle of 1 arcsecond as seen from Earth as it orbits the Sun.

### Stellar parallax

As Earth orbits the Sun, the positions of nearby stars appear to shift against a fixed background of distant stars. This effect is called **parallax**.



By trigonometry,  $d$  is very big compared to 1 AU

$$\tan p = \frac{1 \text{ AU}}{d}$$

so

$$p = \frac{1}{d}$$

$p =$  parallax, in seconds of arc  
 $d =$  distance in parsecs

This uses the small angle approximation  $\tan \theta \approx \theta$

## Cosmological principle

The cosmological principle is a simple but useful idea, without which astrophysics would be impossible.

The cosmological principle states:

- The universe is **homogeneous** – its density is relatively uniform on a large scale.
- The universe is **isotropic** – it looks the same when looking in any direction and from any point.
- The laws of physics are **universal**.

This is important because it means that we can apply what we see in our own galactic neighbourhood to other areas of the universe.

The cosmological principle is an acknowledgement that there's nothing especially important about the Milky Way or our position in it – if there were, we wouldn't be able to assume anything about what we see in other areas of the universe, because the laws of physics might be different.

### Exam Tip!

This is a rough estimate of the age of the Universe! There are other ways to give an indication about the Universe's ages, such as by estimating the ages of the oldest galaxies by their compositions.

$$(H_0 \approx 70 \text{ km s}^{-1} \text{ Mpc}^{-1} = 2.27 \times 10^{-18} \text{ s}^{-1})$$

**The Doppler effect** is the change in of This can be observed in light from distant stars.

- Light from stars moving away from us is called **red shift**.
- Light from stars moving towards us is called **blue shift**.

### Doppler effect:

(for  $v \ll c$ )

$$z = \frac{\Delta \lambda}{\lambda} \approx \frac{v}{c}$$

## Hubble's law

By comparing the velocity of different galaxies, we can see that galaxies far away from Earth are moving away faster.

### Hubble's law:

This recession of galaxies suggests that the universe is moving away from every point in space.

On a small scale, this expansion is opposed by gravity and electrostatic forces, so individual galaxies can be seen on a cosmological scale.

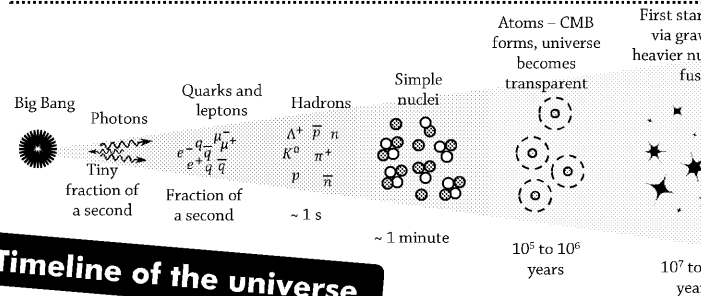
**The Big Bang theory** is a theory of how the universe began. It says that at the start of the universe, all matter and energy were compressed to a single point. This singularity then expanded, and it is this expansion that is the cause of the universe's current size.

### Age of the universe

- Assume  $H_0$  is constant
- $d$  is the distance the furthest galaxies move away from the initial singularity
- $v$  is the velocity at which these galaxies are moving away
- This gives

$$t_{\text{universe}} = \frac{d}{v} = \frac{1}{H_0}$$

$$t_{\text{universe}} = \frac{1}{2.27 \times 10^{-18}} = 4.4 \times 10^{17} \text{ s}$$



## Timeline of the universe

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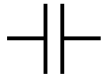
## Capacitance

A **capacitor** is an electrical device that **stores charge**. Capacitors are useful for storing energy and 'smoothing' AC signals in power generation.

In a capacitor, a current causes negative charge to build up on the negative plate, and positive charge to build up on the positive plate. The current never flows through the capacitor itself.

**Capacitance, C**, of a capacitor is defined as the **charge stored, Q, per unit potential difference, V**. The greater the potential difference needed to store a unit charge, the lower the capacitance.

In a circuit, a capacitor is symbolised by two parallel lines



$$C = \frac{Q}{V}$$

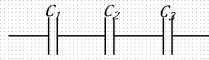
C = capacitance  
Q = charge stored  
V = potential difference across capacitor

## Combining capacitors

Combining multiple capacitors in a circuit can be modelled as having a single capacitance.

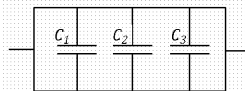
For capacitors in series:

$$\frac{1}{C_{total}} = \frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3} + \dots + \frac{1}{C_n}$$

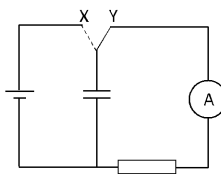


For capacitors in parallel:

$$C_{total} = C_1 + C_2 + C_3 + \dots + C_n$$



## Measuring capacitance



This circuit can be used to investigate capacitance.

When the switch is **connected to X**, the **capacitor charges**, and when it is **connected to Y**, the **capacitor discharges across the resistor**.

By calculating the maximum potential across the capacitor and total charge held by the capacitor, we can find the capacitance of the capacitor and energy stored by the capacitor.

By attaching the voltmeter and ammeter to a **data logger** we can collect data for graphs of charge, potential difference and current as the capacitor charges and discharges.

## Energy stored by capacitor

When a capacitor is charged, energy is stored in the capacitor as **electric potential energy**.

The energy stored by a capacitor increases with both charge stored and potential difference across the plates.

Incredibly large capacitors known as **super capacitors** can even be used as batteries to store energy for later usage.

Energy stored:

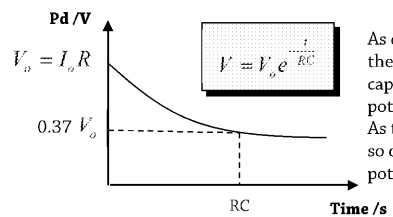
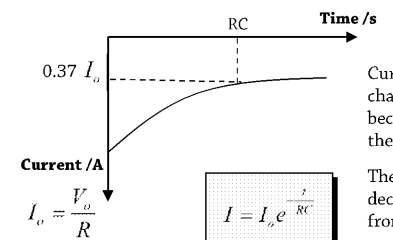
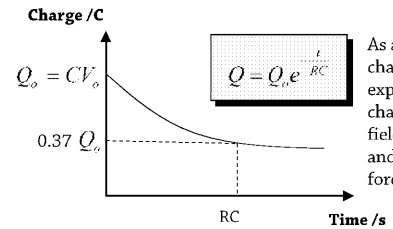
$$E = \frac{1}{2} QV = \frac{1}{2} CV^2 = \frac{1}{2} \frac{Q^2}{C}$$

# Capacitors

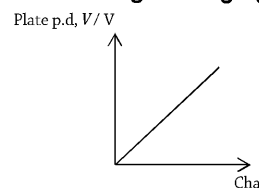
## Capacitor charge and discharge

As a capacitor is charged or discharged, the charge and potential difference across the capacitor and current through the capacitor follows exponential decay relationships.

### Discharging a capacitor



### Voltage-charge



Gradient of V - Q graph =  $\frac{Q}{V}$

Area under V - Q graph =  $\frac{1}{2} QV$

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## Electric field strength

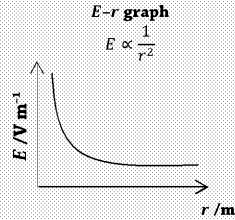
**Electric fields** arise due to a charged object and can be represented by field lines that show the **path a positive charge would take** if placed in the field. When a charged object is in the presence of an electric field it will experience an electrostatic force that is exerted by the field.

**Electric field strength** is defined as the **force,  $F$ , per unit charge,  $Q$** , in the field:

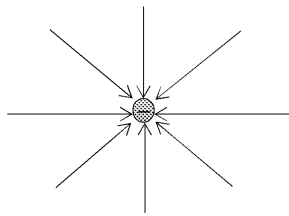
$$E = \frac{F}{Q}$$

$E$  = electric field strength  
 $F$  = force on charge  
 $Q$  = charge

So a greater electric field strength produces a larger force on a charge.



## Radial fields

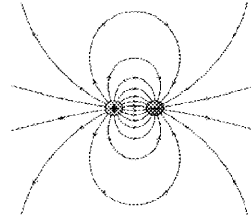


The radial field around a negative point charge.

It is attractive because electric fields are always drawn with reference to a positive point charge.

The electric field strength created by a point charge is given by

$$E = \frac{1}{4\pi\epsilon_0} \frac{Q}{r^2}$$



The field lines of a positive and negative charge brought close together.

A positive charge would be attracted to the negative charge and repelled from the positive charge.

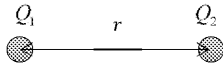
EL  
pc  
Th  
/

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/

## Coulomb's law

Coulomb's law gives the **electric force between two charges**

$$F = \frac{1}{4\pi\epsilon_0} \frac{Q_1 Q_2}{r^2}$$



where  $\epsilon_0$  is a constant called the **permittivity of free space**.  
 $\epsilon_0 = 8.85 \times 10^{-12} \text{ F m}^{-1}$

Therefore, the force between two charges follows the **inverse square law**.

Force increases with greater charge or smaller distance.

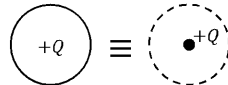
$F$  = force       $Q$  = charge       $r$  = distance between charges

### Exam Tip!

Air can be considered a vacuum when determining forces between charges

### Exam Tip!

A charged sphere can be modelled as a point charge at the centre of the sphere



### Exam Tip!

Attractive forces are negative, repulsive forces are positive

## Work done to move charge

$$\Delta W = Q\Delta V$$

A potential difference of 1 V do 1 J of work on a charge of

**Dielectrics** are any insulating materials store a charge.

A **parallel plate capacitor** is comprised conducting plates with a dielectric in bet

The relative permittivity (dielectric const defined as a ratio of the capacitance of th capacitance of the same volume of free s)

A dielectric with a high relative permittivity Dielectrics tend to be good electrical in

For a parallel plate capacitor, capacitance

$$C = \frac{A\epsilon_0\epsilon_r}{d}$$

$A$  = area of p  
 $\epsilon_0$  = permitt  
 $= 8.85 \times 10^{-12}$   
 $\epsilon_r$  = relative dielectri  
 $d$  = distance

## Electric and gravitational fields

Electric and gravitational fields have many similarities!

	Gravitational	Electrostatic
<b>Source of force field</b>	Mass	Charge
<b>Interaction</b>	Masses always attract	Charges can attract or repel
<b>Force</b>	Inverse square law relationship with respect to distance between masses $F = \frac{GMm}{r^2}$	Inverse square law relationship with respect to distance between charges $F = \frac{1}{4\pi\epsilon_0} \frac{Q_1 Q_2}{r^2}$
<b>Field strength</b>	Force per unit mass	Force per unit charge
<b>Potential in radial field</b>	Always less than zero	Sign depends on the charges

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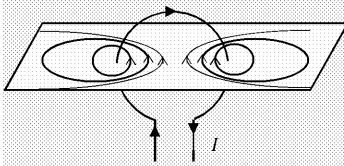
## Magnetic flux density

Magnetic field lines are used to map magnetic fields.

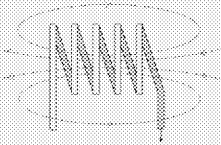
Magnetic field around a current-carrying wire



Magnetic field around a current-carrying flat loop



Magnetic field around a current-carrying solenoid



Force on a current-carrying wire in a magnetic field:

$$F = BIL \sin \theta$$

$F$  = force on wire  
 $B$  = magnetic field strength  
 $I$  = current through wire  
 $L$  = length of wire  
 $\theta$  = angle between wire and field

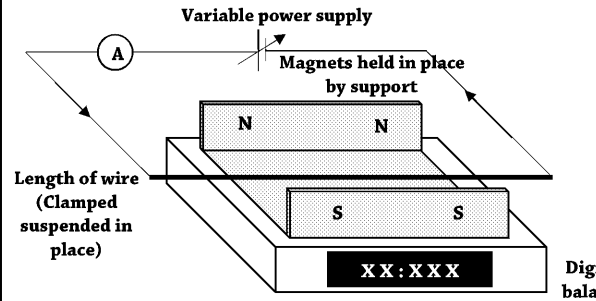
**Magnetic flux density:** is the force per unit length per unit current on a current-carrying conductor at right-angles to a magnetic field

## Electromagneti

### Investigation of force of a wire

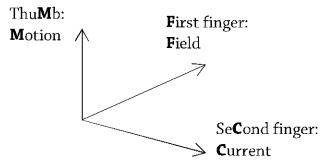
The set-up below can be used to investigate the effect of current on magnet force generated.

The current is varied, and the change in weight of the magnets is recorded - change in weight is due to the force of the magnetic field generated by the



### Fleming's left-hand rule

The rule allows you to determine the direction of motion, field and current in relation to one another:



**Exam Tip!**  
Remember that current is reversed for a negative charge

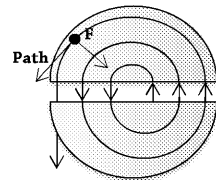
### Charges moving in circular paths

If a charge moves in a circular path in the presence of a magnetic field, we know that the force acting on the particle must be acting towards the centre of the circle.

The magnetic field is being used to control the path direction of the moving charge.

This concept is used in devices such as cyclotrons used in medical machinery to provide radiotherapy treatment

**Cyclotrons** can accelerate radioactive particles and control the direction of the particle beam in order to accurately hit the target area on a patient.



Centripetal force supplied by the force exerted by the magnetic field

$$r = \frac{mv}{BQ}$$

$r$  = radius of particle path  
 $m$  = mass of particle  
 $v$  = speed of particle  
 $B$  = magnetic field strength  
 $Q$  = particle charge

Magnetic field directed into the page for a positive particle

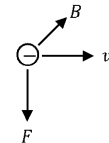
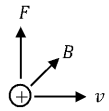
### Moving charges in a magnetic field

Force on charged particles moving in a magnetic field:

$$F = BQv$$

$F$  = force on particle  
 $Q$  = particle charge  
 $B$  = magnetic field strength  
 $v$  = particle velocity

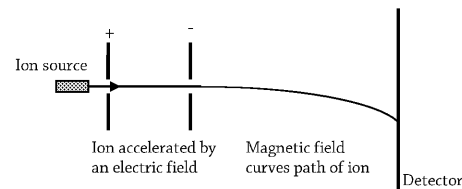
For a magnetic field directed **into the page** a **positive** charge moving to the **right** would experience a force **upwards** a **negative** charge moving to the **right** would experience a force **downwards**



**Exam Tip!**  
The above equations are only applicable if the particle is moving perpendicular to the direction of the field

### Velocity selector

In a velocity selector, an ion is accelerated across an electric field, and then its path is curved by a magnetic field until it hits a detector. The radius of the ion's path, and hence where it hits the detector, is determined by its mass.



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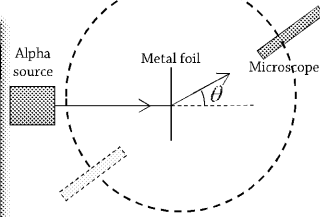


## Rutherford scattering

**Rutherford's scattering experiment** in 1908 provided new evidence about the structure of the atom and resulted in the scientific community moving on from J J Thomson's plum pudding model of the atom and adopting Rutherford's model.

### The experiment

An alpha source provided a **beam of alpha particles** that were aimed at a thin piece of **gold foil**.  
All alpha particles (positively charged) were of the **same energy** and the experiment was carried out in an **evacuated chamber**.  
The alpha particles were **detected** by a detector that remained at a **fixed radial distance** from the point of collision between the particles and the foil.  
**Light was emitted** when the particles hit the detector and these emissions of light could be seen by a microscope.



### The results

A small portion of alpha particles were **deflected by the foil through angles greater than 90°**.  
The majority of alpha particles passed through the foil, some with **no deflection** and some with a **small angle of deflection**.

### The conclusions

The majority of particles passed through the foil, which shows that the atoms making up the foil are likely **mostly empty space**. Most of the mass of the atom is concentrated in a small **nucleus** at the centre of the atom.  
Some alpha particles were deflected, which suggests that the **nucleus must be positively charged**, as the positively charged alpha particles were repelled as they approached the nucleus.

## Nuclei

### Nuclear radius

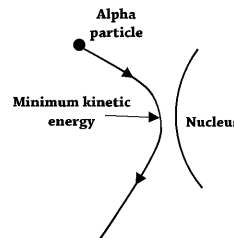
Estimates of nuclear radius can be determined from the **closest approach of alpha particle**:

The nucleus has a radius of around  $\sim 10^{-14}$  m

Closest approach of alpha particles

**Alpha particles are directed towards the atom and are deflected due to electrostatic repulsion.**

**The kinetic energy,  $E_k$ , of the alpha particle will reduce and the potential energy,  $E_p$ , will increase.**

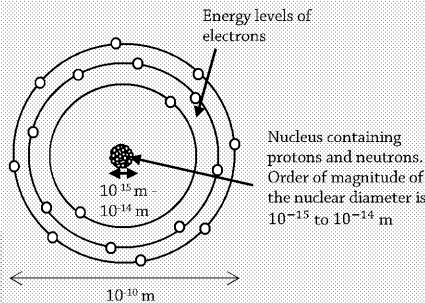


## Constituents of an atom

### Simple model of an atom

An atom is made up of:

1. a nucleus, where most of its mass is concentrated, that is comprised of protons and neutrons
2. electrons that sit in shells outside the nucleus



### Charge and mass of constituent parts

	Charge/ C	Mass/ kg
<b>Electron</b>	$-1.6 \times 10^{-19}$	$9.11 \times 10^{-31}$
<b>Proton</b>	$+1.6 \times 10^{-19}$	$1.67(3) \times 10^{-27}$
<b>Neutron</b>	0	$1.67(5) \times 10^{-27}$

**Specific charge:** the ratio of charge of an ion or particle to its mass

**Isotope:** two or more of the same element with the same number of protons but a different number of neutrons in their nuclei

### Nuclide notation

Nuclei can be written in the following form:



where A is the mass number (number of nucleons) and Z is the proton number (number of protons).

**Strong nuclear** nucleons, which bind

**Unstable nuclei** neutrons and protons from strong nuclear f

You will be able to describe unstable nuclear decay, emitting stable states

### Properties

The strong force between

- It has
- It has proto
- It is a
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## Particles and antiparticles

For every particle there is an antiparticle. A particle's antiparticle has an equal but opposite charge, and the same rest mass and energy as its particle counterpart.

Photon energy:

$$E = hf$$

$$f = \frac{c}{\lambda}$$

$$E = \frac{hc}{\lambda}$$

### Properties of antiparticles

	Particle	Charge, q	Rest mass, $m_0$	Rest energy, $E_0$
<b>Positron</b>	Electron	$+1.6 \times 10^{-19}$ C	$9.11 \times 10^{-31}$ kg	0.511 MeV
<b>Antineutron</b>	Neutron	0 C	$1.67(5) \times 10^{-27}$ kg	939.6 MeV
<b>Antiproton</b>	Proton	$-1.6 \times 10^{-19}$ C	$1.67(3) \times 10^{-27}$ kg	938 MeV
<b>Antineutrino</b>	Neutrino	0 C	0 kg	0 eV

### Pair production

**Pair production** occurs when a photon creates a particle and its corresponding antiparticle, disappearing in the process.

$$hf_{\min} = 2E_0$$

A photon with energy,  $E < 2E_0$ , could, therefore, not create a particle-antiparticle pair.

### Annihilation

**Annihilation** occurs when a particle and its corresponding antiparticle meet. Their individual masses are converted into the radiation energy of two photons.

$$2E_0 = 2hf_{\min}$$

## Particles

Antibaryons

3 antiquarks

- Protons and neutrons are baryons.
- Proton is the only stable baryon.
- All other baryons eventually decay into protons.
- Examples of antibaryons are antiprotons and antineutrons.
- Baryons have a baryon number of +1, whereas antibaryons have a baryon number of -1.
- All hadrons are affected by the strong nuclear force and the strong nuclear force.

## Quarks

	Symbol	Charge	Baryon number
<b>Up</b>	u	$+\frac{2}{3}$	$+\frac{1}{3}$
<b>Down</b>	d	$-\frac{1}{3}$	$+\frac{1}{3}$
<b>Strange</b>	s	$-\frac{1}{3}$	$+\frac{1}{3}$

## Quarks and antiquarks

**Quarks:** elementary particles that are the smallest known constituents that make up matter. There are three types of quarks you need to know.

## Application of conservation laws

### Conservation law decays/interactions

- Conservation of energy, momentum, and charge must be conserved in all changes.
- In any interaction, baryon and lepton numbers must be conserved.
- Strangeness must be conserved in strong and electromagnetic interactions but not weak interactions.

### Quark composition

- Neutron: udd
- Proton: uud
- Antineutron:  $\bar{u}\bar{d}\bar{d}$
- Antiproton:  $\bar{u}\bar{u}\bar{d}$
- Pion:  $u\bar{d}$  ( $\pi^+$ );  $u\bar{u}$  or  $d\bar{d}$  ( $\pi^0$ );  $d\bar{u}$  ( $\pi^-$ )
- Kaon:  $u\bar{s}$  ( $K^+$ );  $d\bar{s}$  or  $s\bar{d}$  ( $K^0$ );  $s\bar{u}$  ( $K^-$ )

You would be expected to know the decay of a baryon in terms of quarks

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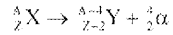
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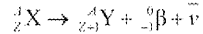
# Radioactive decay

## Types of decay

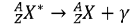
Alpha decay:



Beta decay:

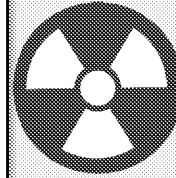


Gamma decay:



## Background radiation

- A low level of radiation is always around us, from both natural and man-made sources of radiation.
- Sources of background radiation:**
  - Natural:** Nuclear materials in ground, cosmic rays
  - Man-made:** Buildings, nuclear power plants, medical nuclear applications
- When calculating the amount of radioactivity present due to a source it is important, therefore, that the **background radiation is measured first** and that this value is **taken away** from the radioactivity measured when the source is present.



Type of radiation	Consists of	Range in air	Ionisation	Absorption	Applications
Alpha	Two protons + two neutrons	<10 cm	Creates around $10^4$ ions per cm in air	Stopped by thin metal foil or paper	Thickness measurements of paper Used in smoke detectors
Beta	Electron or positron	<1 m	Creates around 100 ions per mm in air	Stopped by 3-5 mm of aluminium	Thickness measurements of aluminium foil
Gamma	Photon of energy	Obeys inverse square law ( $1/r^2$ )	Weakly ionising	Stopped by several cm of lead	Used in medicine to image internal structure of the body

## Radioactive decay

**Radioactive decay** occurs when an atom is unstable, and emits radiation to obtain a **more stable state**.

Radioactive decay is a **random process**. This means that we can't know which nucleus in a sample will decay next, or when.

### Activity A:

the number of unstable nuclei that decay per second in a given sample:

$$A = A_0 e^{-\lambda t}$$

$$A = \lambda N$$

Decay probability:

$$\frac{\Delta N}{\Delta t} = -\lambda N$$

Number of unstable nuclei:

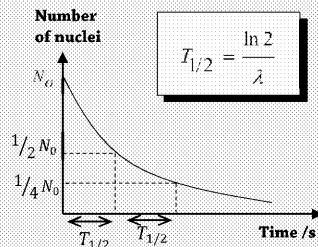
$$N = N_0 e^{-\lambda t}$$

$N$  = number of atoms in sample  
 $N_0$  = initial number of atoms in sample  
 $\lambda$  = decay constant  
 $t$  = time

The **half-life ( $T_{1/2}$ )** of a radioactive substance is the amount of time it takes for the activity of the substance to decrease to **half its original value**. Half-life is a constant, no matter the amount of substance left.

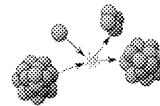
Half-life is used in medicine to determine which isotope to use to image inside a patient's body as the source needs only to be radioactive as long as the imaging takes and then should have as little radioactivity as possible.

It is also used in areas such as **carbon dating**. All living organisms have a roughly equal ratio of  $^{12}\text{C}$  to  $^{14}\text{C}$  in their bodies. When they die, the  $^{14}\text{C}$  slowly decays. By examining the amount of  $^{14}\text{C}$  left in a sample, its age can be determined.



binding energy per nucleon than the low mass temperatures and pressures than fission, so is

- Nuclear fission:** a large unstable nucleus splits into two smaller nuclei. The binding energy per nucleon will



Knowledge of the scientists to make energy use as an

## Induced fission

Fission isotopes

The uranium isotope is split into **two small** roughly equal mass and two or three **fission** Fission (thermal) neutrons can be harnessed Chain reactions only occur if the material is With each fission event huge amounts of en Fission chain reactions are used in **nuclear**

## The thermal n

- The **moderator** controls the speed of the neutron in order to induce fission. Graphite or **low probability of absorbing** neutrons at
- The **control rods** absorb neutrons to ensure each fission event. They have the ability to release of energy needs to be reduced. The ability to **absorb neutrons effectively**.
- The **coolant** extracts the heat and allows it electricity. Coolant is usually water or carbon **specific heat capacity** of the materials.

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# Medical imaging

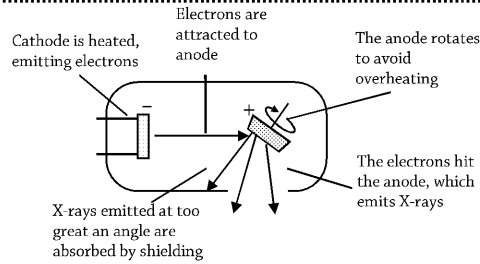
## X-rays

**X-rays** are produced by accelerating electrons through a potential and colliding them with a metal target – as the electrons hit the target and suddenly decelerate, their kinetic energy is converted to X-rays.

Electrons are released via thermionic emission – the cathode heats up and releases electrons.

As the electrons are accelerated, they gain energy,  $E = eV$ .

If all of this energy is converted to the energy of the X-ray, the energy of the X-ray will be  $eV = hc/\lambda$ .



## X-ray attenuation

As X-rays pass through matter, they are absorbed.

The intensity of the beam decreases exponentially.

**Attenuation:**  $I$  is the beam intensity  
 $x$  is the distance through the materials  
 $\mu$  is the linear attenuation coefficient  
 $\mu_m = \frac{\mu}{\rho}$  is the mass attenuation coefficient

$$I = I_0 e^{-\mu x}$$

### Attenuation

**Simple scatter:** 1–20 keV. X-rays are absorbed and re-emitted by atoms without changing energy, only direction.

**Photoelectric effect:** < 100 keV. X-rays are absorbed by an electron which then leaves the atom.

**Compton effect:** 0.5–5.0 MeV. X-rays are partly absorbed by an electron leaving the atom, and which is scattered with reduced energy.

**Pair production:** > 1.02 MeV. X-rays are converted into an electron-positron pair when approaching the nucleus.

**Ultrasound** is sound  
 20 kHz – outside the  
**Ultrasound scans**  
 body non-invasive  
 At each tissue boundary  
 The amount of energy  
 specific acoustic impedance  
 The reflections can

**A-scans** are single  
 The reflected energy  
 If the speed of sound  
 to the boundary can

**B-scans** are a rapid  
 The scans are swept  
 The reflected energy  
 brighter areas are darker

**Uses**  
 To see babies in the  
 To scan organs such

A special gel is  
 skin to reduce  
 because the gel  
 – it has the same  
 of skin, so fills  
 doesn't pass through

## Detection

**X-ray film** will react with X-rays by changing from white to black.

A contrast medium is used to increase the contrast of an image. A patient will ingest a sample of barium or iodine, which is opaque to X-rays so shows up well. This gives greater detail.

## CT scans

A **CT scan** involves a series of narrow beams of X-rays passed over the patient.

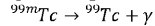
Each beam produces a 360° image of a 'slice' of the patient, and the camera then moves on to produce another 360° of the next 'slice'.

CT scans are much slower and more expensive than traditional X-rays, but produces 3D images with much higher detail.

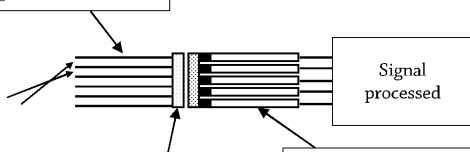
## Gamma camera

**Gamma cameras** are used to detect radiation emitted by radionuclide tracers.

A tracer commonly used with gamma cameras is technetium-99m. This is a short-lived isotope which gives off gamma rays.



**Collimator** removes photons travelling at an angle

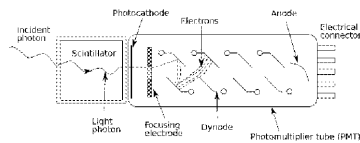
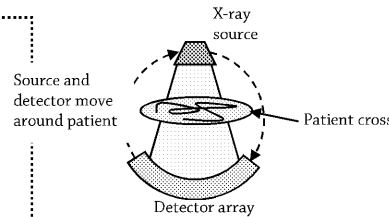


**Scintillator** produces many more photons, amplifying the signal

Photons travel through **light guide** and **photomultiplier tube array**, converting the photons into an electrical signal to be processed

In a photomultiplier tube, a photon is converted into an electron, which is then amplified into a cascade of electrons.

Technetium-99m can be attached to biological molecules, meaning it can easily be made to move to specific sites in the body.  
 ${}^{99m}\text{Tc}$  has a half-life of around six hours, so doesn't stay in the body too long.



In a **PET scan**, a positron-emitting tracer  
 Fluorine-18 is a tracer often used, which

The positron emitted in this decay quickly  
 Two gamma rays are emitted at 180° from

${}^{18}\text{F}$  is used as it can form a molecule  
 quickly moves towards areas of the body

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# Thermal physi

## Absolute zero

1. a) What is meant by the term 'absolute zero'?  
  
b) What is the value of absolute zero in kelvin and in Celsius?  
  
2. Convert:
  - a) 84.5 °C to K.
  - b) 114 K to °C.
  - c) 3520 °C to K.

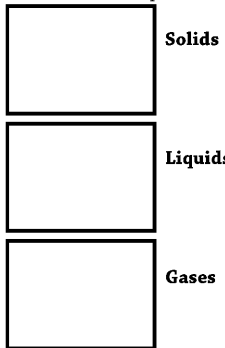
7. Define what is mea

8. During a camping t  
1030 J of heat is pu  
The water does 480  
What is the differer

9. State the first law o

## States of matter

3. Describe solids, liquids and gases below, including a diagram of the particles in each state.



4. State what is meant by Brownian motion.

5. Outline an experiment that could be used to determine the **specific heat capacity** of a substance.

6. Outline an experiment that could be used to determine the **specific latent heat** of a substance.

10. A bowl containing 1.

Over time, the ice cul

The specific heat cap.  
 $3.36 \times 10^5 \text{ J kg}^{-1}$ .

a) Calculate the ener

b) What can be said

c) Calculate the ener

d) Explain what hap

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# Ideal gases

1. Explain the difference between molecular mass and molar mass.

2. A  $6.5 \text{ m}^3$  oxygen canister is kept at a pressure of  $15,200 \text{ kPa}$  and a temperature of  $20 \text{ }^\circ\text{C}$ .

Calculate the number of moles in the canister.

$$R = 8.31 \text{ J mol}^{-1} \text{ K}^{-1}$$

3.  $0.34 \text{ J}$  of work is done on a gas, compressing it to a volume of  $48 \text{ cm}^3$ , at a constant pressure of  $950 \text{ Pa}$ . Calculate the initial volume of the gas.

4. a)

b)

c)

5. Describe how Charles' law can be investigated.

## Molecular kinetic theory model

6. Use the molecular kinetic theory model to explain each of the three gas laws.

7. A sample of helium is at  $10.0 \text{ }^\circ\text{C}$ .

The molar mass of helium is  $0.00400 \text{ kg mol}^{-1}$ .

**Note:**  $k = 1.38 \times 10^{-23} \text{ J K}^{-1}$

a) Calculate the kinetic energy of a helium molecule in the sample.

b) Calculate root mean square velocity of the helium molecule.

c) Calculate the total kinetic energy for  $5.00$  moles of helium.

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# Periodic motion

## Circular motion

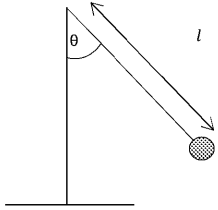
1. Explain how an object or a system can remain in a circular path.

## Angular quantities

2. A vibrating string is oscillating with a frequency of 20.0 Hz. Calculate its angular speed.
3. A geostationary satellite takes 24 hours to orbit Earth. The geostationary satellite is in circular orbit with a radius of 42,157 km.
  - a) Calculate the speed of the satellite around Earth.
  - b) Explain how the satellite is able to maintain a circular orbit around Earth.
  - c) Calculate the centripetal acceleration.

## Simple harmonic systems

7. A clock pendulum is swinging back and forth, and is shown here at its maximum amplitude.



- a) What can be said about the relationship between the pendulum's acceleration and its displacement from the equilibrium position?
- b) Sketch on the diagram the direction of the centripetal force.
- c) Explain how the kinetic energy and potential energy will change during the oscillation.

4. Wha

5. Calc  
displ

6. The  
repr  
simp  
a)

b)

c)

10. Define the term

8. What is a damped oscillation?

9. Sketch a graph of displacement against time for a system with:

- Light damping
- Heavy damping
- Critical damping

11. Explain the difference between oscillation.

Damped oscillations

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## Gravitational fields

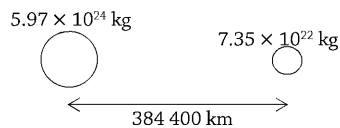
1. Give the definitions of a uniform field and a radial field and describe how these relate to gravitational fields.
2. a) Sketch a radial gravitational field around a planet, indicating the direction of the field lines.  
  
b) Explain what a gravitational field line indicates.

## Gravitational field strength

3. Every object on Earth feels a force of attraction directed towards the centre of Earth due to Earth's gravitational field.  
Earth has mass  $5.97 \times 10^{24}$  kg and a radius of 6371 km.  
Show that the gravitational field strength at the surface of Earth is  $9.81 \text{ N kg}^{-1}$ .

## Newton's law of gravitation

4. The sketch below shows the separation of Earth and the Moon.



Calculate the force of gravitation between Earth and the Moon.

## Gravitational fields

### Kepler's laws

5. State Kepler's three laws of planetary motion.

### Escape velocity

6. Determine the escape velocity needed for any object to escape Earth's gravitational field.  
Earth has mass  $5.97 \times 10^{24}$  kg and a radius of 6371 km.

### Geostationary satellites

8. Using Kepler's third law, show that the period of a geostationary satellite is roughly 24 hours.  
The orbital radius of a geostationary satellite is 35,786 km.

7. Derive Kepler's third law from the centripetal forces acting on the satellite.

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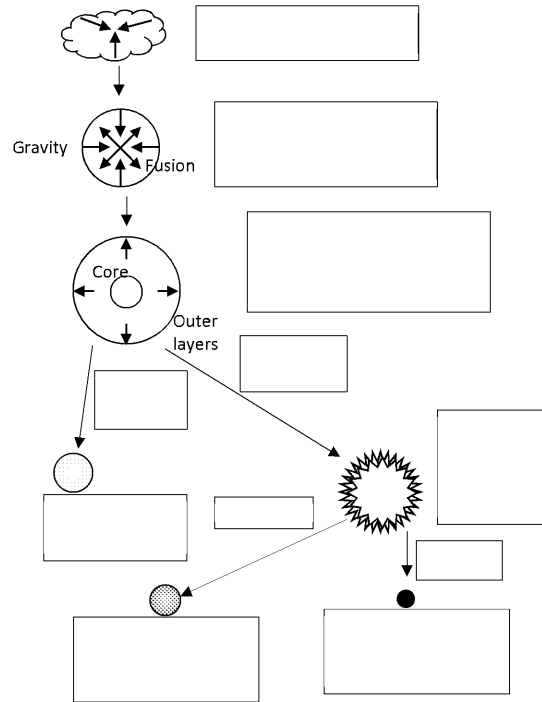
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# Stars

## Life cycle of a star

1. Complete the diagram below by adding a description for each stage of the life cycle of a star.

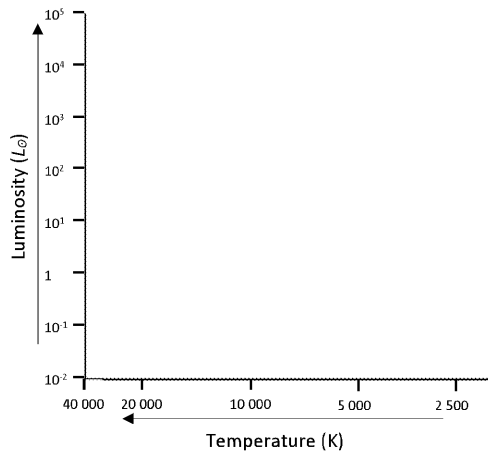


2. Describe the main characteristics of:
- A white dwarf
  - A neutron star
  - A black hole

4. A photon excites an electron from hydrogen's first excited state at  $-3.4$  eV, to its third excited state,  $-0.9$  eV. Calculate the wavelength of the photon.

## The Hertzsprung–Russell diagram

5. Complete the Hertzsprung–Russell diagram below, and add the path a sunlike star takes during its lifetime.



6. Describe the main features of the following types of star.
- Brown dwarf
  - Red giant star
  - Main-sequence star

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# Cosmology

## Astronomical distances

1. Convert:

- 4.37 ly to m (distance to Alpha Centauri – nearest star to the Sun)
- 779 km to AU (distance between the Sun and Jupiter)
- 30 kpc to AU (diameter of the Milky Way)
- $2.53 \times 10^6$  ly to pc (distance to Andromeda – nearest galaxy to the Milky Way)

2. Wolf 359 appears to travel 0.415 arcseconds over the course of a year.  
Calculate the distance to Wolf 359 in light years.

3. Describe the cosmological principle.

4. The Sombrero Galaxy has a red shift of 0.003416. The Fraunhofer  $H_\alpha$  line observed from the Sombrero Galaxy has a wavelength of 435.530 nm.

- Calculate the original wavelength of the Fraunhofer  $H_\alpha$  line.
- Calculate the recessional velocity of the Sombrero Galaxy.

Red shift

5. The Whirlpool Galaxy is 24 million light years away.  
Calculate the distance to the Whirlpool Galaxy in parsecs.

6. Show how Hubble's law can be used to estimate the distance to a galaxy.  
Use  $H_0 \approx 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$

7. Describe and explain the cosmological principle.

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# Capacitors

## Capacitance

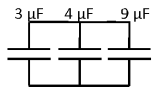
1. Define the term 'capacitance'.
2. What is a capacitor?
3. Explain how charge is stored on a parallel plate capacitor.
4. A  $5\mu\text{F}$  capacitor has  $4\text{ V}$  applied across its plates.
  - a) Calculate the total charge stored on the capacitor plates.

The potential difference applied to the plates is increased.

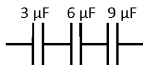
- b) Sketch a graph of how the charge stored on the plates will change as the potential difference applied to the plates is changed.

5. Calculate the total capacitance of the following combinations of capacitor.

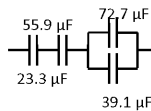
a)



b)



c)



7. Sketch the graphs of voltage

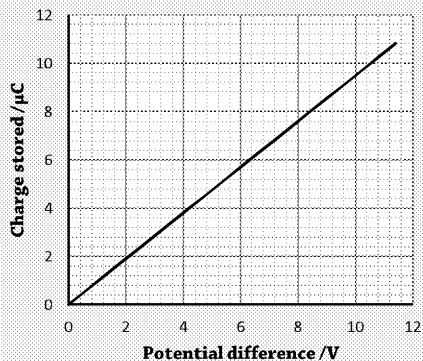
8. A  $50\mu\text{F}$  capacitor is being discharged. Initially the capacitor has  $4.0\text{ V}$  across it.

- a) Calculate the charge across the capacitor.

- b) Calculate the time it will discharge to half its initial charge.

9. A  $500\mu\text{F}$  capacitor is charged to  $10\text{ V}$ . Calculate the voltage across the capacitor after it has discharged for  $10\text{ s}$ .

## Energy stored by capacitor



6. The graph on the left shows the potential difference across a capacitor with varying charge stored by the capacitor.

Calculate the energy stored in the capacitor when there is a potential difference of  $6.00\text{ V}$  across the capacitor.

10. Draw a circuit with a capacitor and a variable resistor to investigate the effect of the resistance on the time taken for the capacitor to discharge.

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# Electric fields

## Electric field strength

### Electric field strength in a radial field

1. Sketch the electric field pattern around an isolated positive charge.
2. Calculate the electric field strength generated by a 3.0 mC positive charge felt at a distance of 3.0 mm.

3. Define 'electric field strength'.

4. Explain what a field line represents in an electric field pattern.

5. Calculate the magnitude of the electric field strength felt by +2.10 mC charge that experiences a 50.0 mN force.

### Electric field strength in a uniform field

6. Two parallel plates, which are separated by 0.0300 m, are connected to a power source and have a potential difference of 5.00 V between them.
  - a) Sketch the electric field pattern between the two plates.
  - b) Calculate the magnitude of the force exerted on a +1.10 mC charge positioned in between the two plates.

### Electric and gravitational fields

8. Fill in the missing values in the table below.

	Gravitational	Electros
Source of force field		Charge
Force	Inverse square law relationship with respect to distance between masses $F = \frac{GMm}{r^2}$	
Field strength		Force per unit
Potential in radial field	Always less than zero	

### Coulomb's law

7.
  - a) Describe what will happen to the force exerted on two charged objects as the separation between them increases.
  - b) Explain what will happen to the value of the force in (a) if the separation is increased to twice its original value.

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9.

10

12



# Electromagneti

## Magnetic flux density

1. Define 'magnetic flux density'.
2. A 0.3 m wire is carrying 0.6 A of current.  
  
It is placed perpendicular to a 3.2 T magnetic field coming out of the page, as seen to the right.
  - a) Calculate the magnitude of the force exerted on the wire.
  - b) Determine the direction of motion of the wire when it is placed in the magnetic field.
3. A wire is at an angle to a 82 mT magnetic field. The wire carries a 510 mA current, and 15 cm of the wire sits in the magnetic field. The wire experiences a force of 3.8 mN. Calculate the angle between the wire and the magnetic field.

## Moving charges in a magnetic field

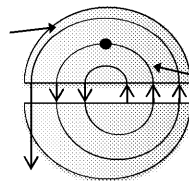
4. A -3.0 mC charge is moving to the right at  $1.6 \times 10^4 \text{ m s}^{-1}$  perpendicular to a 1.2 T magnetic field moving into the page.
  - a) Sketch the direction of the force exerted by the magnetic field on the moving charge.
  - b) Calculate the magnitude of the force exerted on the charge.

## Magnetic flux and magnetic flux

8. A rectangular coil with dimensions 5.0 cm  $\times$  10 cm is placed perpendicular to a 0.60 T magnetic field.  
The coil consists of 10 turns of wire.
  - a) Calculate the magnetic flux of the coil.
  - b) Calculate the magnetic flux linkage through the coil.
  - c) Explain how the magnetic flux linkage would alter if the coil was rotated relative to the magnetic field.

5. A cyclotron is used in medical physics to accelerate particles.

Magnetic field acts only in hemispheres



- a) State the direction of the magnetic field path shown is for a positive particle.
  - b) A particle accelerator operates with a 0.1 m radius. Calculate the radius of the path taken by a particle moving at a speed of  $2.5 \times 10^7 \text{ m s}^{-1}$ .
6. State Lenz's law.
  7. Calculate the magnitude of the emf induced in a coil of cross-sectional area of 0.070 m<sup>2</sup> and 50 turns that is placed in a magnetic field with magnetic flux density 1.3 T over 10 ms.

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## Rutherford scattering

1. What was J J Thomson's plum pudding model?
2. Explain why the scientific community ceased to use J J Thomson's model.
3. Sketch the apparatus used by Rutherford in his scattering experiment and explain what each piece of apparatus was intended for.
4. Why did Rutherford deduce that the majority of a nucleus's mass is concentrated in a small region at its centre?
5. Sketch diagrams of J J Thomson's and Rutherford's nuclear models to explain the differences in the models.

## Nuclei

10. State the approximate

11. Sketch a graph of inter diffraction for an elect

### Constant densit

13. a) Show that the dens approximately con.
- b) Calculate the value  
Use  $R_0 = 1.25 \text{ fm}$ .

### Stable and un

15. Define the terms:  
'strong nuclear force'  
'unstable nucleus'

17. Sketch the strength of separation.

## Constituents of an atom

### Simple model of an atom

6. Sketch and label the simple model of the atom.

### Nuclide notation

8. State the number of protons and neutrons in the following nuclei:
- a)  ${}_{92}^{238}\text{U}$
- b)  ${}_{2}^4\text{He}$
9. Give two examples of isotopes of the same element in nuclide form.

### Charge and mass of constituent parts

7. Fill in the table below. Use the data booklet if you get stuck.

	Charge	Mass
Electron		
Proton		
Neutron		

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# Particles

## Particles, antiparticles and photons

1. Comment on the relationship between charge and mass of a particle and its corresponding antiparticle.

3. Calculate the frequency of a photon of energy  $E = 2.80 \times 10^{-18} \text{ J}$

6. Fill in the words missing from the bubbles in the mind map.

### Properties of antiparticles

2. Complete the table below. *Use the data booklet if you get stuck.*

	Particle	Charge	Rest mass	Rest energy
Positron				
Antineutron				
Antiproton				
Antineutrino				

### Pair production

4. Calculate the minimum energy of the photon required to create a proton-antiproton pair.

### Annihilation

5. Calculate the minimum frequency of one of the photons produced when an electron and a positron meet.

Antibaryons:

3 antiquarks

Examples:

## Application of conservation laws

## Quarks and antiquarks

7. Define the term 'quarks'.

### Quarks

9. a) State three types of quark.

b) State the baryon number of the quarks from your answer to part (a).

c) State the charge of the antiquarks from your answer to (a).

10. Comment on whether the following are valid. Give reasons for your answers.

a)  $\pi^- + p \rightarrow K^0 + \Lambda^0$  ( $\Lambda^0 = udc$ )

b)  $\mu^- \rightarrow e^- + \bar{\nu}_\mu + \nu_e$

c)  $\nu_e + n \rightarrow \bar{p} + e^+$

11. Complete the following decay/interaction equations:

a)  $\mu^- \rightarrow e^- + \bar{\nu}_e + ?$

b)  $K^0 + p \rightarrow ? + \pi^-$

### Quark composition

8. State the quark composition of:

- a proton
- an antineutron
- $K^-$
- $\pi^0$

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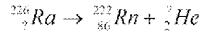
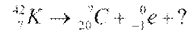
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# Radioactive decay

## Types of decay

1. Complete the following decay equations and comment on the type of decay represented:



2. Fill in the missing boxes in the following table.

Type of radiation	Consists of	Range in air	Ionisation	Absorption (stopped by...)	Example of application
Alpha		<100 mm	Creates around $10^4$ ions per cm in air		
			Creates around 100 ions per mm in air		Thickness measurements of aluminium foil
Gamma		Obeys inverse square law		Stopped by several cm of lead	

3. The following decay equation is:



Calculate the energy released.

$$\begin{aligned} m_n &= 1.0087 \text{ u} \\ m_{\text{Kr-90}} &= 89.9195 \text{ u} \\ 1 \text{ u} &= 931.5 \text{ MeV} \end{aligned}$$

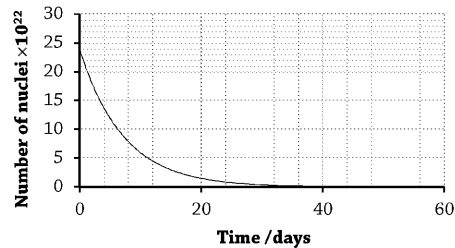
6.

## Radioactive decay

7. Explain what is meant by the statement 'radioactive decay is a random process'.

8. A sample of a radioactive isotope initially contains  $4.70 \times 10^{24}$  atoms. The decay constant for the isotope is  $2.50 \times 10^{-4} \text{ s}^{-1}$ .

- Calculate the remaining number of atoms of the isotope after 2,400 seconds.
- Calculate the activity of the sample after this time.
- What was the initial activity of the sample?



- From the graph, determine the half-life of the radioactive isotope.
- Calculate the decay constant of the isotope.

10. Explain how the

11. What is meant by

Change  
to be  
Control  
risk  
Radioactive  
shielding  
Pressure  
water  
Temperature  
nuclear fuel  
Fuel  
risk

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# Medical imaging

## X-rays

1. Describe how X-rays are produced for use in medical imaging.

2. After passing through bone with a thickness of 3.50 cm, the intensity of an X-ray beam is reduced to 0.122 of its initial value. The density of bone is  $1.8 \text{ g cm}^{-3}$ . Calculate the mass attenuation coefficient of bone.

3. Describe the following mechanisms of X-ray attenuation, and state the regions in which they are dominant.

**Simple scatter:**

**Photoelectric effect:**

**Compton effect:**

**Pair production:**

4. Describe how CT scans are different from traditional X-rays, and the advantages and disadvantages of CT scans over traditional X-rays.

## Radionuclides

5. Why is technetium-99m often used as a radionuclide tracer for use with gamma cameras?

6. With the use of a diagram, describe how gamma cameras collect and convert gamma rays from radionuclides into an image.

7. With the use of a diagram, describe how a photomultiplier tube works.

8. Describe how ultrasonography is used in medical imaging.

9. Describe the role of contrast agents in ultrasound.

11. Describe the advantages and disadvantages of ultrasound over other imaging techniques.

14. Describe how the Doppler effect is used in ultrasound.

16. Describe how PET scans are used in medical imaging.

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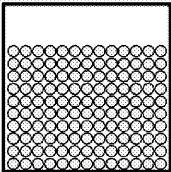
# Thermal physi

Absolute zero

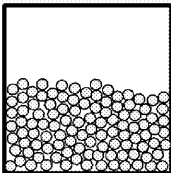
Thermal equilibrium

First la

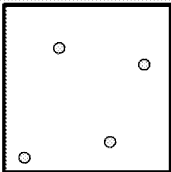
## Solids, liquids, gases



Solids



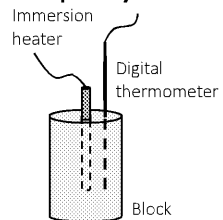
Liquids



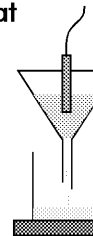
Gases

Brownian motion

### Determining specific heat capacity



### Determining specific latent heat



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# Ideal gases

## Ideal gas laws

## Molecular kinetic theory model

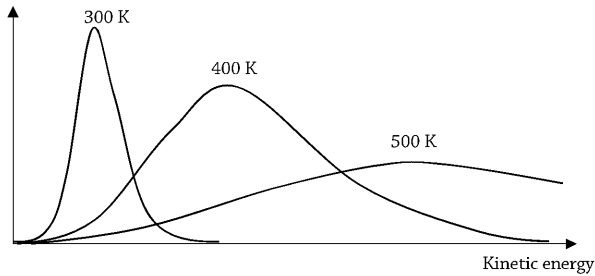
Kinetic theory equation

$M_c$

Average  
molecul  
kinetic e

Internal  
an ideal

Number of particles



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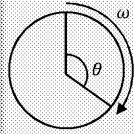
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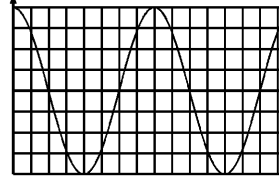
## Circular motion

## Periodic motion

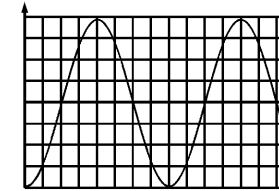
### Angular quantities



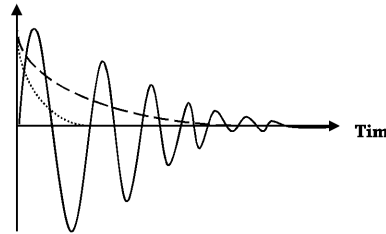
Displacement/m



Acceleration/m s<sup>-2</sup>

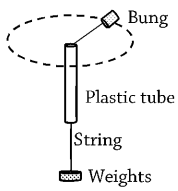


Amplitude

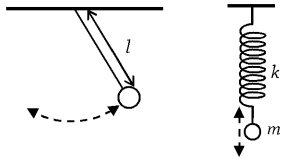


### Damped oscillations

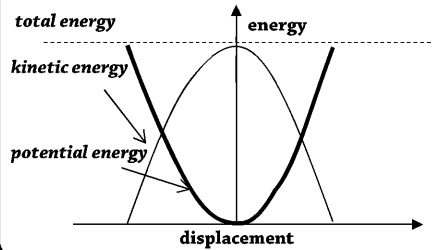
### Investigating circular motion



### Investigating simple harmonic motion



### Energy-displacement graphs of SHM for free oscillations



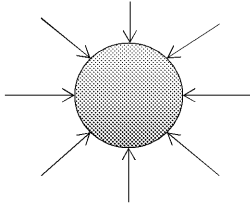
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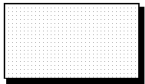




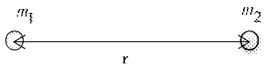
## Gravitational fields



## Gravitational field strength



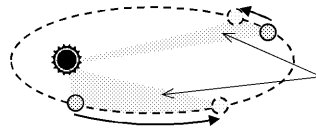
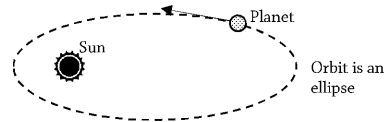
## Newton's law of gravitation



$$F = \frac{Gm_1m_2}{r^2}$$

# Gravitational fields

## Kepler's laws of planetary motion



This shows the movement of the planet during two equal periods of time. Planet travels faster when closer to the Sun, so that both shaded areas are of equal size.

### Derivation of Kepler's third law

## Geostationary satellites

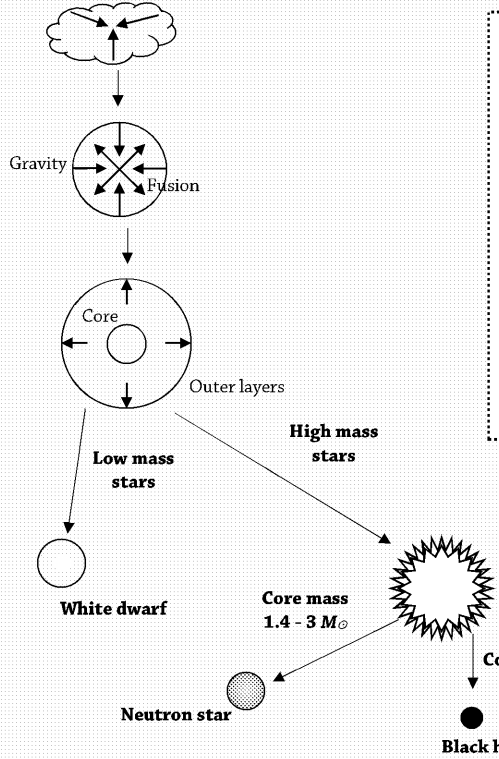
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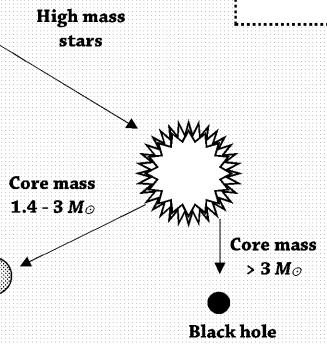


# Stars

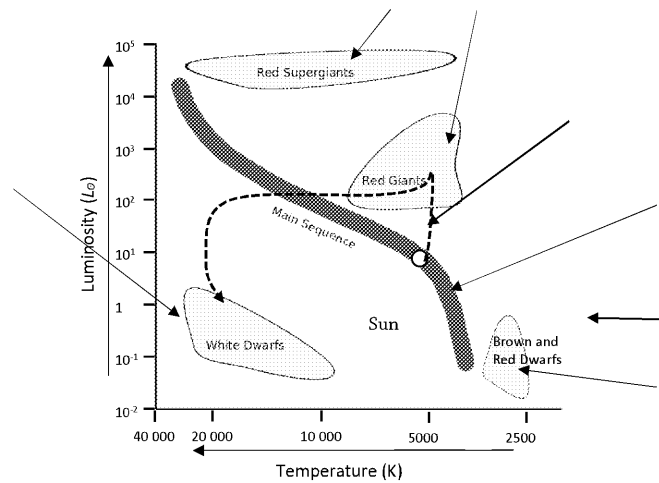
## Life cycle of a star



## The deaths of stars



## The Hertzsprung–Russell (HR) diagram



Absor

Black-b

Power/ W

Wien

Examp

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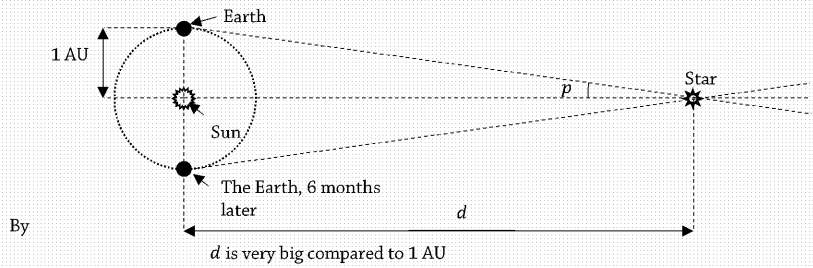


# Cosmology

## Distances in astrophysics



### Stellar parallax



By

$d$  is very big compared to 1 AU



Doppler effect:

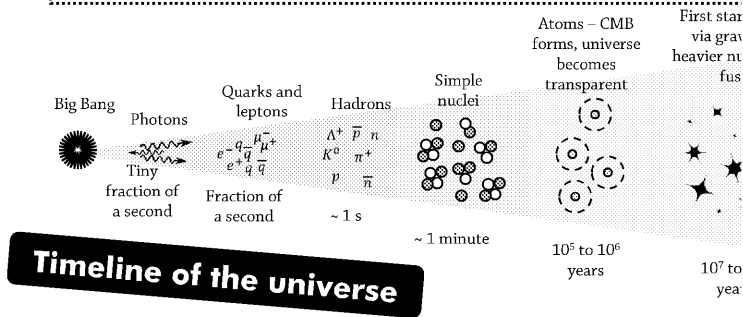
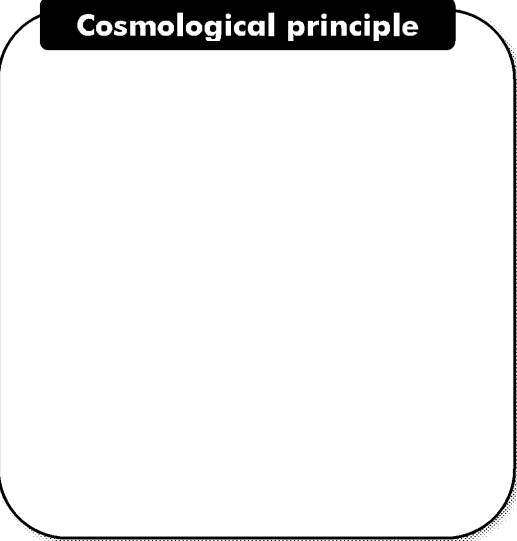


## Hubble's law

Hubble's law:



## Cosmological principle



## Timeline of the universe

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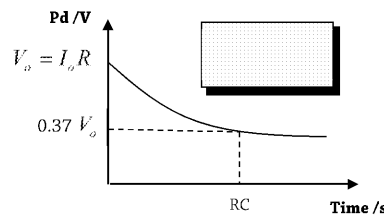
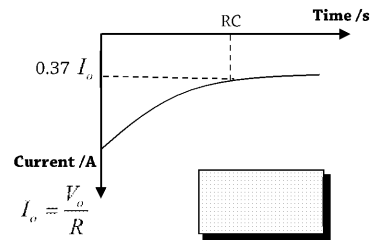
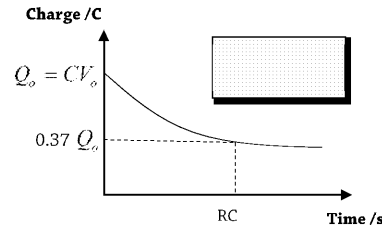
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# Capacitors

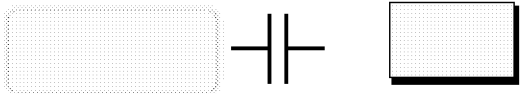
## Capacitor charge and discharge

Discharging a capacitor

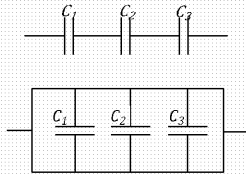


Voltage-charge graph

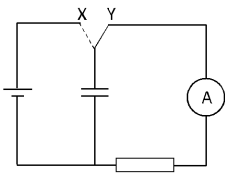
## Capacitance



## Combining capacitors



## Measuring capacitance



## Energy stored by capacitor

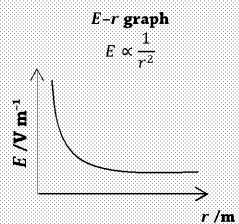
Energy stored:

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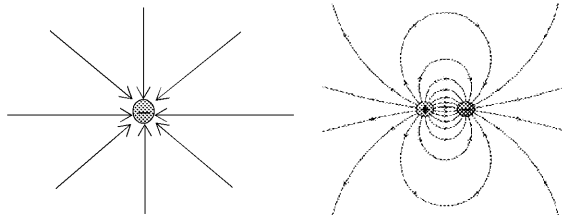
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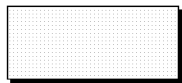
## Electric field strength



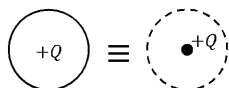
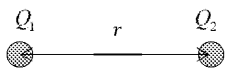
## Radial fields



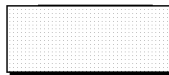
V/V



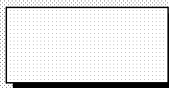
## Coulomb's law



Work done to move charge



## Electric and gravitational fields

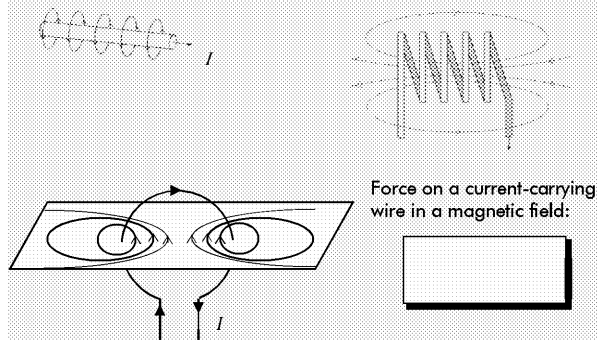


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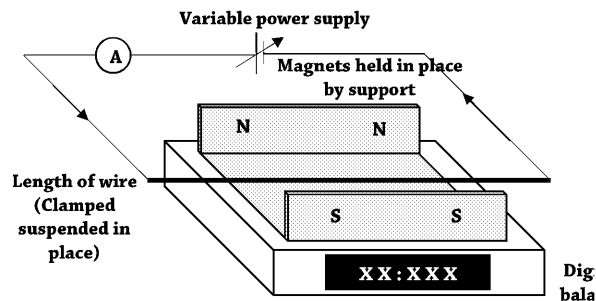


## Magnetic flux density

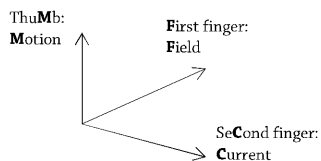


## Electromagneti

### Investigation of force of a wire

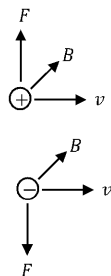


### Fleming's left-hand rule

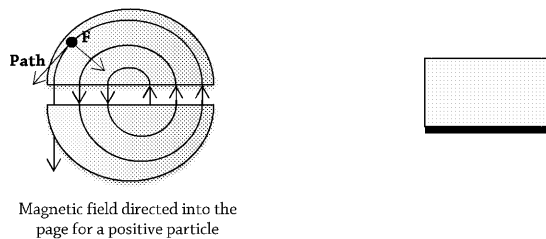


### Moving charges in a magnetic field

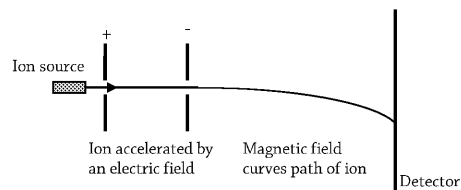
Force on charged particles moving in a magnetic field:



### Charges moving in circular paths



### Velocity selector



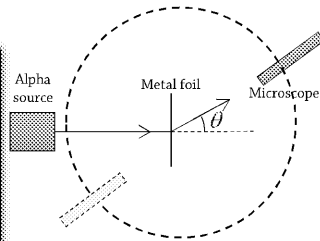
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## Rutherford scattering

### The experiment



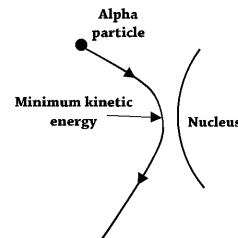
### The results

### The conclusions

## Nuclei

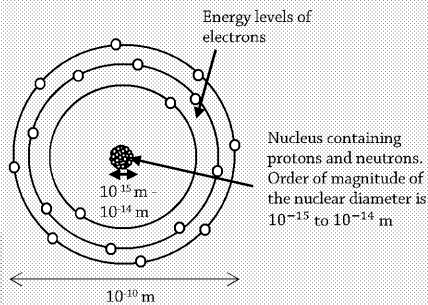
### Nuclear radius

#### Closest approach of alpha particles



## Constituents of an atom

### Simple model of an atom



Strong nuclear

Unstable nuclei

### Charge and mass of constituent parts

	Charge/ C	Mass/ kg
Electron		
Proton		
Neutron		

Specific charge:

Isotope:

### Nuclide notation

Prop

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## Particles and antiparticles

Photon energy:

$$f = \frac{c}{\lambda}$$

### Properties of antiparticles

	Particle	Charge, q	Rest mass, $m_0$	Rest energy, $E_0$
Positron	Electron			0.511 MeV
Antineutron	Neutron	0 C		939.6 MeV
Antiproton	Proton			938 MeV
Antineutrino	Neutrino	0 C	0 kg	0 eV

### Pair production

### Annihilation

## Particles

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### Quarks

	Symbol	Charge	Baryon number
Up			
Down			
Strange			

## Quarks and antiquarks

Quarks:

## Application of conservation laws

Conservation law  
decays/interactions

### Quark composition

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# Radioactive decay

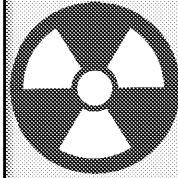
**Types of decay**

Alpha decay:

Beta decay:

Gamma decay:

**Background radiation**



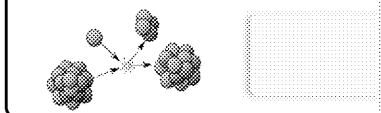
Type of radiation	Consists of	Range in air	Ionisation	Absorption	Applications
Alpha					
Beta					
Gamma					

## Radioactive decay

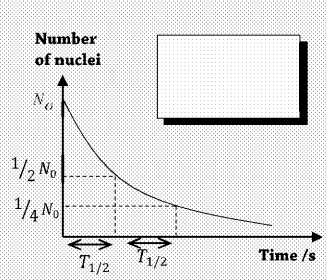
Activity A:

Decay probability:

Number of unstable nuclei:



## Induced fission



**The thermal n**

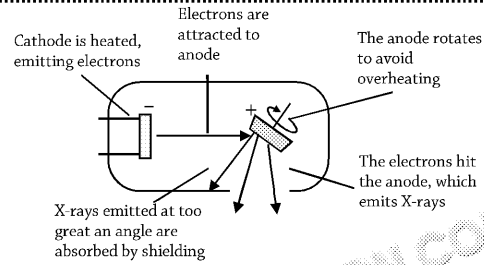
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# Medical imaging

## X-rays



## X-ray attenuation

Attenuation:

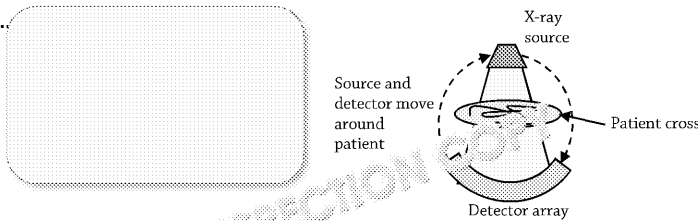


Attenuation



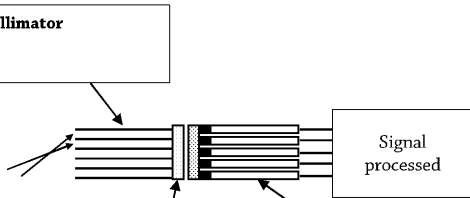
## Detection

CT scans

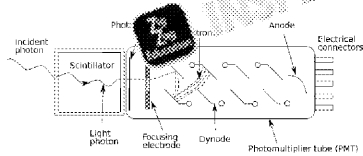


## Gamma camera

Collimator



Scintillator



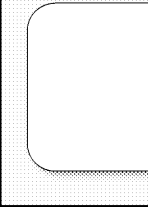
## Ultrasound

Ultrasound scan

A-scans

B-scans

Uses



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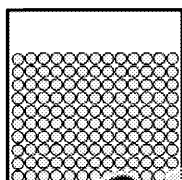


# Mark Scheme

## 1: Thermal physics

1. a) Absolute zero is the temperature at which all kinetic energy of a substance has energy is at a minimum.  
b)  $-273\text{ }^{\circ}\text{C}$ ,  $0\text{ K}$
2. a)  $357.5\text{ K}$   
b)  $-159\text{ }^{\circ}\text{C}$   
c)  $3790\text{ K}$

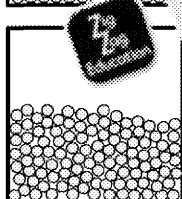
3.



### Solids

There is small spacing between atoms and molecules, so the intermolecular forces are strong. Solids have high densities.

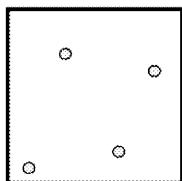
Atoms and molecules in solids are very ordered and have fixed positions. They do not have fixed shapes.



### Liquids

The spacing between atoms and molecules is greater in liquids than in solids, but they are still quite close together. Because of this, the intermolecular forces are still strong, and liquids are less dense than solids.

Atoms and molecules in liquids are somewhat ordered and can move around each other, so liquids can flow.



### Gases

Atoms and molecules in gases are very far apart, so they have weak intermolecular forces and have low densities.

Because the atoms and molecules in gases are very far apart, the intermolecular forces are negligible and molecules are free to move around.

4. Brownian motion describes the erratic motion of a small particle in a fluid. The molecules in the fluid move randomly and hit into the particle, making the particle move. This can be seen in smoke particles suspended in air – rather than remaining stationary they appear to bounce around.
5.
  - Place immersion heater and digital thermometer in block or beaker of substance
  - Heat block and record the energy transferred using the power rating of the heater. Can measure power using ammeter and voltmeter.
  - Measure temperature of block at regular intervals
  - Plot energy transferred against temperature change
  - Gradient is  $mc$
6.
  - Place immersion heater in a funnel filled with ice
  - Heat ice, determining energy from the power of the heater
  - At regular intervals, measure the mass of the water in the beaker
  - Compare mass to a control beaker which is unheated. The mass of the water from the mass of the melted ice
  - Plot energy transferred against mass of melted water
  - Gradient is  $mc$
7. The sum of the randomly distributed kinetic energies and potential energies of particles.
8. The internal energy will have increased as the temperature has increased.  

$$\Delta U = Q + W$$

$$\Delta U = 1030 - 480$$

$$\Delta U = 550\text{ J}$$

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9. The change of internal energy of an object is equal to the total energy transfer due to it.
10. a)  $Q = mc\Delta\theta$   
 $Q = 1.3 \times 2090 \times 5$   
 $Q = 13600 \text{ J}$
- b) The temperature remains constant as the ice goes under a change of state.
- c)  $Q = mL$   
 $Q = 1.3 \times 3.36 \times 10^5$   
 $Q = 437000 \text{ J}$
- d) The energy of the molecules increase and they vibrate enough to overcome the attractive forces (ice) therefore changes into a liquid (water).

**2: Ideal gases**

1. The molar mass is the mass of one mole of substance (in  $\text{kg mol}^{-1}$ ), whereas the mass of one molecule in atomic mass units (u).
2.  $pV = nRT$   
 $n = \frac{pV}{RT}$   
 $n = \frac{15\,200\,000 \times 6.5}{8.31 \times (20 + 273)}$   
 $n = 40\,600$
3.  $W = p\Delta V$   
 $V_{\text{initial}} = V_{\text{final}} + \frac{W}{p} = 48 \times 10^{-6} + \frac{0.34}{950}$   
 $V_{\text{initial}} = 410 \times 10^{-6} \text{ m}^3 = 410 \text{ cm}^3$
4. a) Doubles (using  $\frac{p}{T} = \text{constant}$ )  
 b)  $\frac{V}{T} = \text{constant}$   
 $\frac{V_1}{T_1} = \frac{V_2}{T_2}$   
 $T_2 = \frac{T_1 V_2}{V_1} = \frac{300 \times 1.1}{1.4}$   
 $T_2 = 240 \text{ K}$   
 c)  $pV = \text{constant}$   
 $p_1 V_1 = p_2 V_2$   
 $V_2 = \frac{p_1 V_1}{p_2} = \frac{1.12 \times 10^3 \times 5.12 \times 10^{-6}}{1.55 \times 10^3}$   
 $V_2 = 3.69 \times 10^{-6} \text{ m}^3 = 3.70 \text{ cm}^3$
5. Use a set-up using a piston attached to a pressure gauge. Ensure piston is free to move. Heat the set-up with a Bunsen burner. Measure change in height of piston to calculate volume. Check pressure gauge to ensure it is constant, if not, adjust volume. Plot volume against temperature. It should be a straight-line graph with gradient  $p$ .
6. **The pressure law:** As the temperature of a gas in a container with a fixed volume, as the temperature increases, the average speed of the molecules increases and, therefore, the molecules collide with the container walls more often. This increases the force exerted on the container walls and, therefore, the pressure increases.

**Boyle's law:** If the **volume** of the container of gas is decreased then the gas molecules collide more often between collisions with the container wall. This results in there being more collisions with the container wall and, therefore, the force exerted is increased and, therefore, so is the **pressure**.

**Charles' law:** As the **temperature** is increased on a gas, the average speed of the molecules increases. The molecules collide with the sides of the container harder and more often. If the volume is fixed, the greater force on the walls of the container results in the walls of the container expanding and, therefore, the **volume** increases.

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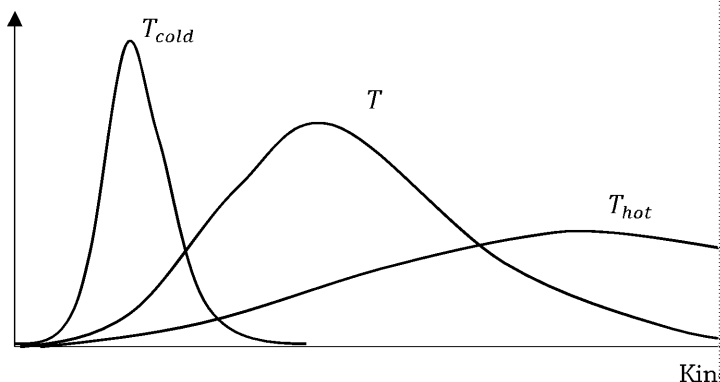


7. a)  $E_k = \frac{3}{2}kT$   
 $E_k = \frac{3}{2} \times 1.38 \times 10^{-23} \times (10 + 273)$   
 $E_k = 5.86 \times 10^{-21} \text{ J}$

b)  $E_k = \frac{1}{2}mc_{rms}^2$   
 $c_{rms} = \sqrt{\frac{2 \times 5.86 \times 10^{-21}}{0.004 \div (6.02 \times 10^{23})}}$   
 $c_{rms} = 1330 \text{ m s}^{-1}$

c)  $E_{k,total} = N_A \times n \times E_k$   
 $E_{k,total} = 6.02 \times 10^{23} \times 5 \times 5.86 \times 10^{-21}$   
 $E_{k,total} = 17600 \text{ J}$


8. Numl  particles



9.  $\frac{1}{2}m\overline{c^2} = \frac{3}{2}kT$   
 $pV = NkT$   
 $kT = \frac{pV}{N}$   
 $\frac{1}{2}m\overline{c^2} = \frac{3}{2} \frac{pV}{N}$   
 $p = \frac{1}{3} \frac{Nm}{V} \overline{c^2}$

**3: Periodic motion**

1. A centripetal force provides a force/acceleration towards the centre of the circular path

2.  $\omega = 2\pi f$   
 $\omega = 2\pi \times 20$   
 $\omega = 1$    $\text{s}^{-1}$

3. a)  $v = \frac{\text{circumference}}{\text{time for one rotation}}$   
 $v = \frac{2\pi r}{T}$   
 $v = \frac{2 \times \pi \times 42157 \times 10^3}{24 \times 60 \times 60}$   
 $v = 3065.7 \text{ m s}^{-1}$

b) Due to the centripetal force exerted on the satellite due to Earth's gravitational

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c)  $a = \frac{v^2}{r}$   
 $a = \frac{3605.7^2}{42157 \times 10^3}$   
 $a = 0.223 \text{ m s}^{-2}$

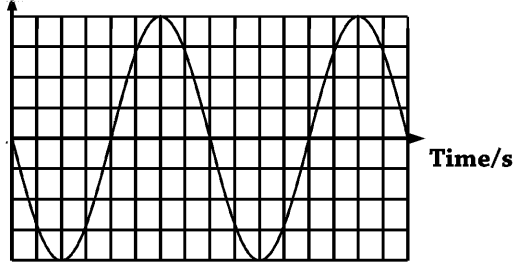
4. Simple harmonic motion refers to an oscillating motion where the acceleration of the object is directly proportional to the displacement from the equilibrium position and opposite in direction.

5.  $a = -\omega^2 x$   
 $a = -(1.2)^2 \times 0.8$   
 $a = 1.2 \text{ rad s}^{-2}$

6. a) • 0.5 m

•  $\frac{500}{2} = 250 \text{ s}$

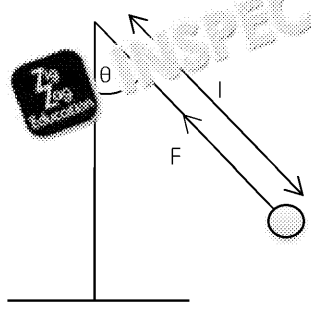
b)  $v_{\text{max}} = 0.01 \text{ m s}^{-1}$



c)  $v_{\text{max}} = \omega A$   
 $v_{\text{max}} = \frac{2\pi}{T} A$   
 $v_{\text{max}} = \frac{2\pi}{250} \times 0.5$   
 $v_{\text{max}} = 0.01 \text{ m s}^{-1}$

d)  $a_{\text{max}} = \omega^2 A$   
 $a_{\text{max}} = \left(\frac{2\pi}{T}\right)^2 A$   
 $a_{\text{max}} = \left(\frac{2\pi}{250}\right)^2 \times 0.5$   
 $a_{\text{max}} = 3.2 \times 10^{-4} \text{ m s}^{-2}$

7. a) The acceleration is directly proportional to the displacement from the equilibrium position.  
 b)



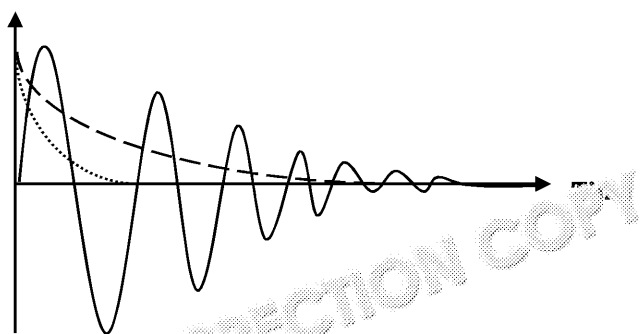
c) The kinetic energy is maximum at the equilibrium position and zero at the amplitude position. The potential energy is maximum at the amplitude position and zero at the equilibrium position.

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8. Oscillations in which energy and amplitude of oscillations are lost to the damping of
9. Heavy dashed line: Heavy damping  
Dotted line: Critical damping  
Solid line: Light damping

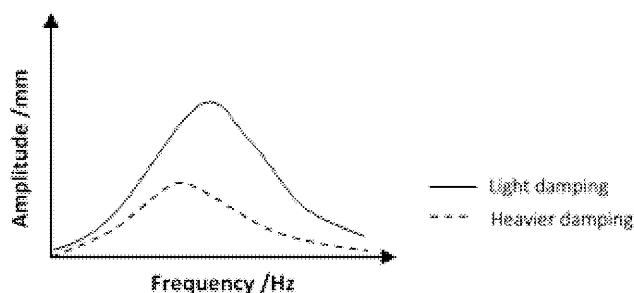
**Displacement**



10. Resonance occurs in the situation in which the driving force of the oscillation is in phase with the oscillation and the amplitude of oscillation increases.
11. **Free oscillation:** an oscillation of a body or system that is moving with its natural frequency without any external influence.

**Forced oscillation:** an oscillation of a body or system that is initiated by an external force.

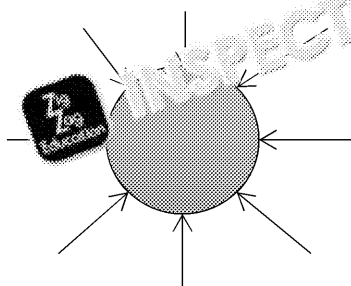
12.



**4: Gravitational fields**

1. **Radial field:** A field that is circular and acts towards a central point. Gravitational fields are approximated by radial fields. **Uniform field:** A field that has no variation. Gravitational fields are approximated by uniform fields near planets.

2. a)



b) A gravitational field line illustrates the path a smaller mass takes towards a larger mass.

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$$3. \quad g = \frac{GM}{r^2}$$

$$g = \frac{6.67 \times 10^{-11} \times 5.97 \times 10^{24}}{(6371000)^2}$$

$$g = 9.81 \text{ N kg}^{-1}$$

$$4. \quad F = \frac{GMm}{r^2}$$

$$F = \frac{6.67 \times 10^{-11} \times 5.97 \times 10^{24} \times 7.35 \times 10^{22}}{(384400000)^2}$$

$$F = 1.98 \times 10^{20} \text{ N}$$

5. 1. A planet orbits the Sun in an elliptical orbit, with the Sun at one of the focal points.  
 2. The area swept out by the line connecting the Sun and a planet sweeps out a constant area in a constant time.  
 3. The period of a planet's orbit squared is proportional to the average radius of the orbit cubed.



$$T^2 \propto r^3$$

$$T^2 = \left( \frac{4\pi^2}{GM} \right) r^3$$

$$6. \quad v = \sqrt{2gr}$$

$$v = \sqrt{2 \times 9.8 \times 6\,371\,000}$$

$$v = 1.12 \times 10^4 \text{ m s}^{-1}$$

$$7. \quad F_{\text{centripetal}} = F_{\text{gravitation}}$$

$$\frac{mv^2}{r} = \frac{GMm}{r^2}$$

$$v^2 = \frac{GM}{r}$$

$$v = \frac{2\pi r}{T}$$

$$\frac{(2\pi r)^2}{T^2} = \frac{GM}{r}$$

$$\frac{r^3}{T^2} = \frac{GM}{4\pi^2}$$

$$\frac{GM}{4\pi^2} = \text{constant} = \text{same for all planets}$$

$$T^2 \propto r^3$$

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8.  $\frac{r^3}{T^2} = \frac{GM}{4\pi^2}$

$$T^2 = \frac{4\pi^2 r^3}{GM}$$

$$T^2 = \frac{4\pi^2 (6\,371\,000 + 35\,786\,000)^3}{6.67 \times 10^{-11} \times 5.97 \times 10^{24}}$$

$$T^2 = 7\,427\,944\,755$$

$$T = 86\,185.53 \text{ seconds}$$

$$T = \frac{86\,185.53}{60 \times 60}$$

$$T = 2.39 \text{ hrs}$$

9. **Gravitational potential energy** ( $E_p$ ): the energy possessed by an object due to its position in a gravitational field.

**Gravitational potential** ( $V$ ): the work required to move an object from infinity to a point in a gravitational field.

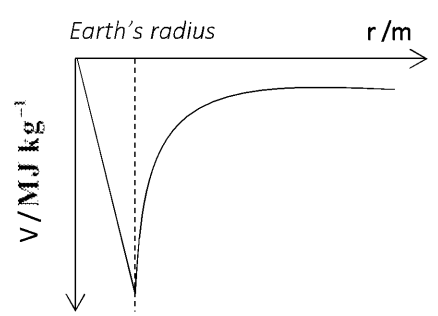
10. Zero

11.  $V = \frac{-GM}{r}$

$$V = \frac{-6.67 \times 10^{-11} \times 5.97 \times 10^{24}}{(35\,786\,000 + 6\,371\,000)}$$

$$V = -9.45 \times 10^6 \text{ J kg}^{-1}$$

12. a)



b) From the gradient of the graph.

13. Equipotentials are surfaces of constant potential.

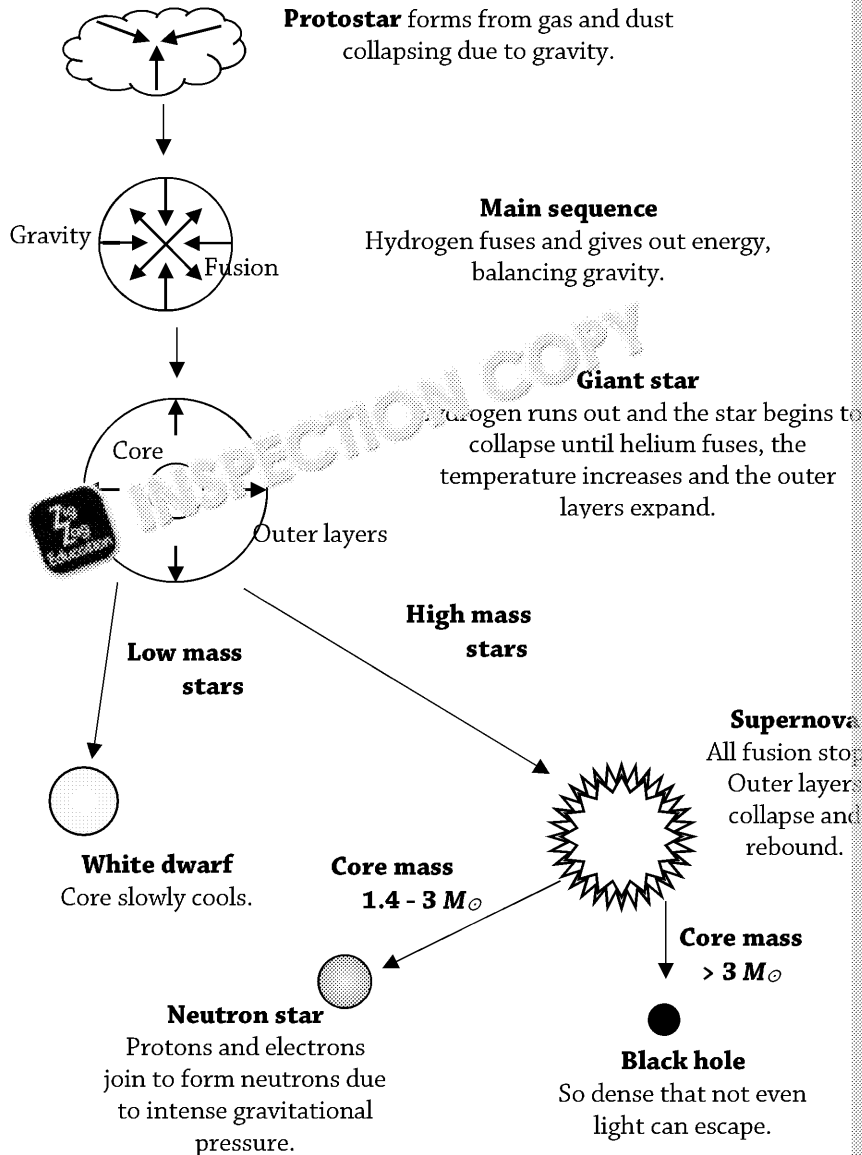
14. No work would be done since  $\Delta W = m\Delta V$  and  $\Delta V = 0$  when travelling along the equipotential.

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## 5: Stars

1.



2. a) A white dwarf is the leftover core of a star, which no longer undergoes fusion. White dwarfs gradually cool and radiate all their heat, and become black dwarfs.
- b) If the core left over after a supernova has a mass of  $1.4 \times$  to  $3.0 \times$  solar masses, it forms a neutron star. The radius of a neutron star is about 10 km.
- In the core of a neutron star, gravity is so great that protons and electrons join to form neutrons.
- c) If the core left over after a supernova has a mass of more than  $3 \times$  solar masses, it forms a black hole. A black hole is so dense that not even light can escape. The region around a black hole from which nothing can escape is called the event horizon.

3. Photons from stars are absorbed by atoms in the outer layers of stars. This causes electrons to jump to higher energy levels. These energy levels are specific to the atom, so each atom absorbs specific wavelengths. The missing wavelengths in a spectrum can be used to identify the composition of a star.

4. 
$$E = \frac{hc}{\lambda}$$

$$\lambda = \frac{hc}{E} = \frac{6.63 \times 10^{-34} \times 3.00 \times 10^8}{(-0.9 + 3.4) \times 1.60 \times 10^{-19}}$$

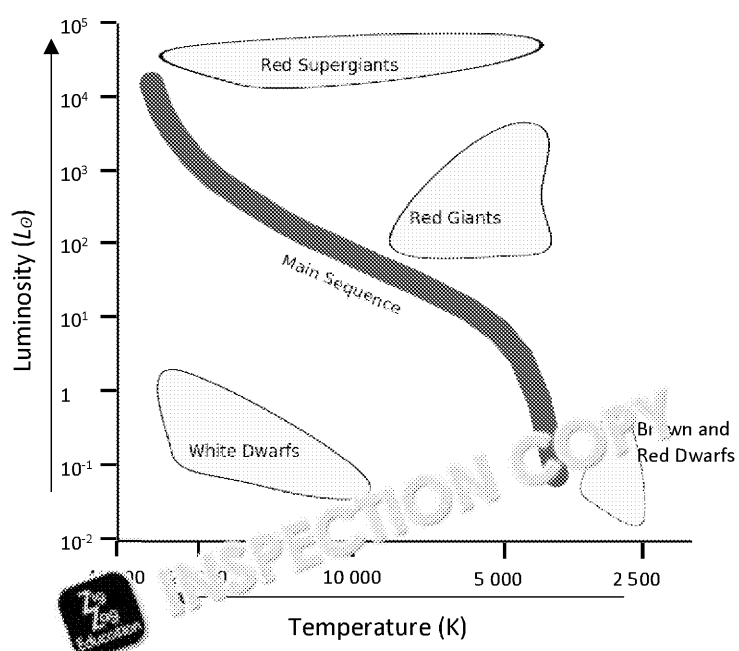
$$\lambda = 497 \text{ nm}$$

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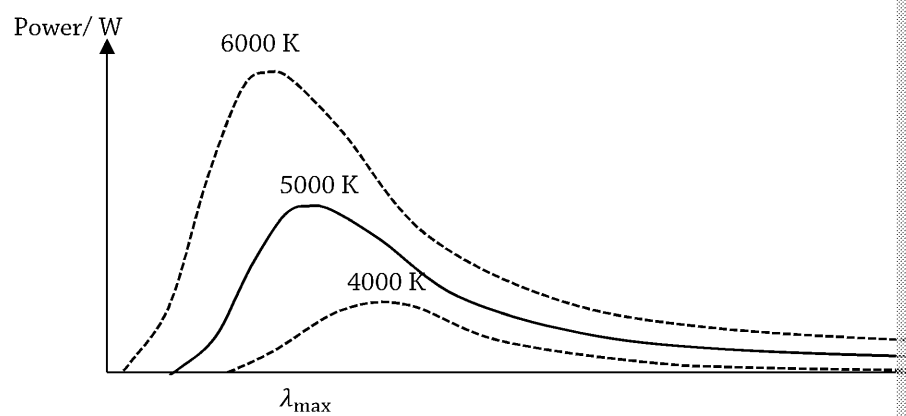


5.



6. a) Brown dwarfs are starlike objects with masses too low to fuse hydrogen.  
 b) Giant stars are large and bright. Red giants fuse helium in their cores after they run out of hydrogen to fuse.  
 c) All stars spend most of their lives in the main sequence. This is when they fuse hydrogen into helium. Most stars, including the Sun, are on the main sequence.

7.



8.  $\lambda_{\max} T = 2.9 \times 10^{-3} \text{ m K}$   
 $\lambda_{\max} = \frac{2.9 \times 10^{-3}}{T} = \frac{2.9 \times 10^{-3}}{5344}$   
 $\lambda_{\max} = 5.4 \times 10^{-7} \text{ m} (= 540 \text{ nm})$

9.  $P = 4\pi r^2 \sigma T^4$   
 $T = \left( \frac{P}{4\pi r^2 \sigma} \right)^{\frac{1}{4}} = \left( \frac{5.67 \times 10^{-8} \times 10^{32}}{4\pi \times (2.0 \times 10^{10})^2} \right)^{\frac{1}{4}}$   
 $T = 5.84 \times 10^4 \text{ K}$

10.  $T = \frac{2.9 \times 10^{-3}}{\lambda} = \frac{2.9 \times 10^{-3}}{115 \times 10^{-9}}$   
 $T = 2.52 \times 10^4 \text{ K}$

$4\pi r^2 = \frac{P}{\sigma T^4}$   
 $r = \sqrt{\frac{P}{4\pi \sigma T^4}} = \sqrt{\frac{2.15 \times 10^{25}}{4\pi \times 5.67 \times 10^{-8} \times (2.52 \times 10^4)^4}}$   
 $r = 8.65 \times 10^6 \text{ m}$

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## 6: Cosmology

1. a)  $4.37 \text{ ly} = 4.37 \times 9.46 \times 10^{15} = 4.13 \times 10^{16} \text{ m}$   
 b)  $779 \times 10^6 \text{ km} = \frac{779 \times 9}{1.50 \times 10^{11}} = 5.19 \text{ AU}$   
 c)  $30 \text{ kpc} = 30 \times 10^3 \times 2.06 \times 10^5 = 6.2 \times 10^9 \text{ AU}$   
 d)  $2.53 \times 10^6 \text{ ly} = \frac{2.53 \times 10^6}{3.26} = 7.76 \times 10^5 \text{ pc}$

2.  $p = \frac{1}{d}$   
 $d = \frac{1}{p}$   
 $d = \frac{1}{0.415}$   
 $d = 2.409 \text{ pc}$   
 $d = 2.409 \times 3.26 = 7.86 \text{ ly}$

3. The cosmological principle states:
  - The universe is **isotropic** – its density is relatively uniform on a large scale
  - The universe is **homogeneous** – it looks the same when looking in any direction and from any point
  - The laws of physics are **universal**.

4. 1. a)  $z = \frac{\Delta\lambda}{\lambda} = \frac{\lambda_{\text{observed}} - \lambda}{\lambda}$   
 $\lambda = \frac{\lambda_{\text{observed}}}{1+z} = \frac{435.530 \times 10^{-9}}{1+0.003416}$   
 $\lambda = 434.047 \text{ nm}$

- b)  $z = \frac{v}{c}$   
 $v = zc = 0.003416 \times 3.00 \times 10^8$   
 $v = 1.02 \times 10^6 \text{ m s}^{-1}$

5.  $v = \frac{\Delta f}{f} \times c = \frac{6.9747 \times 10^{14} - 6.9639 \times 10^{14}}{9.9639 \times 10^{14}} \times 3.00 \times 10^8$   
 $v = 4.652 \times 10^5 \text{ m s}^{-1}$

$$d = \frac{v}{H} \approx \frac{4.652 \times 10^5}{70 \times 10^3}$$

$$d \approx 6.65 \text{ Mpc} = 21.7 \times 10^{17} \text{ ly}$$

6. Assume  $H_0$  is constant  
 $d$  is the distance the furthest galaxies have been able to move away from the initial point  
 $v$  is the velocity at which these galaxies have moved away  
 This gives

$$t_{\text{universe}} = \frac{d}{v} = \frac{1}{H_0}$$

$$t_{\text{universe}} = \frac{1}{2.27 \times 10^{-18}} = 4.4 \times 10^{17} \text{ s} = 13.9 \text{ billion years}$$

7.
  - **Red shift of distant galaxies**
    - Implies all galaxies are expanding from a single point
  - **Cosmic microwave background (CMB)**
    - Radiation left over from the Big Bang
    - Its spectrum changes over time and is now equivalent to  $\sim 2.7 \text{ K}$
  - **Abundance of hydrogen and helium in the universe**
    - The matter in the universe is about 74 % hydrogen, 24 % helium and trace amounts of other elements
    - A short, intense period of high energy (such as the Big Bang) would only produce hydrogen and helium
    - All heavier elements have been produced in stars since then

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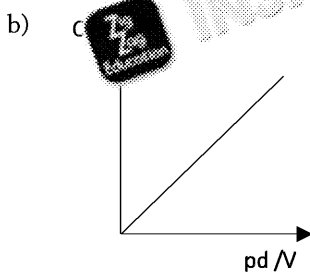


## 7: Capacitors

1. **Capacitance** of a capacitor is defined as the charge stored per unit pd.
2. A **capacitor** is an electrical device that stores charge.
3. A **parallel plate capacitor** is comprised of two parallel conducting plates. If the power source, then as electrons flow through the power source they are forced from the negative terminal to one of the plates.

Due to the interaction between like charges, an equal number of electrons leave the positive terminal of the power supply and the plate gains an equal but positive charge.

4. a)  $Q = CV$   
 $Q = 5 \times 10^{-6} \times 4$   
 $Q = 2 \times 10^{-5} \text{ C}$



5. a)  $C_T = C_1 + C_2 + C_3$   
 $C_T = 3 + 4 + 9$   
 $C_T = 16 \mu\text{F}$

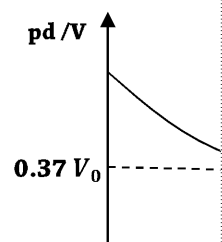
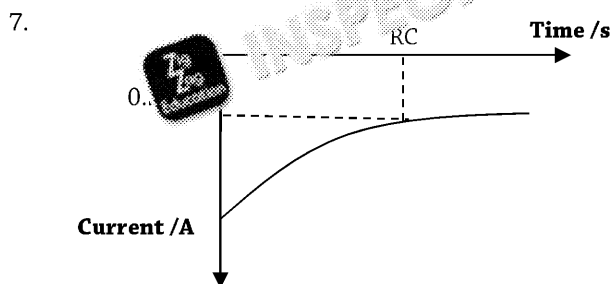
b)  $\frac{1}{C_T} = \frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3}$   
 $\frac{1}{C_T} = \frac{1}{3} + \frac{1}{6} + \frac{1}{9} = 0.611 \mu\text{F}^{-1}$   
 $C_T = 1.6 \mu\text{F}$

c)  $\frac{1}{C_T} = \frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3 + C_4}$   
 $\frac{1}{C_T} = \frac{1}{55.9} + \frac{1}{23.3} + \frac{1}{72.7 + 39.1} = 0.06975 \mu\text{F}^{-1}$   
 $C_T = 14.3 \mu\text{F}$

6.  $E = \text{area under graph} = \frac{1}{2} QV$

$$E = \frac{1}{2} \times 5.70 \times 6.00 \times 10^{-6}$$

$$E = 1.70 \times 10^{-5} \text{ J}$$



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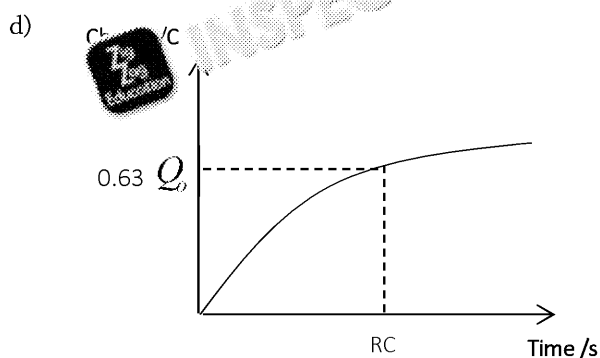
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8. a)  $Q = 0.37Q_0$   
 $Q = 0.37 \times 4 \times 10^{-6}$   
 $Q = 1.5 \times 10^{-6} \text{ C}$

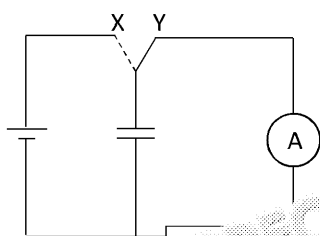
b)  $t_{1/2} = 0.69RC$   
 $t_{1/2} = 0.69 \times 10 \times 50 \times 10^{-6}$   
 $t_{1/2} = 3.5 \times 10^{-4} \text{ s}$

c)  $Q = Q_0 e^{-\frac{t}{RC}}$   
 $Q = 4 \times 10^{-6} \times e^{-\frac{0.1 \times 10^{-3}}{10 \times 50 \times 10^{-6}}}$   
 $Q = 3.3 \times 10^{-6} \text{ C}$



9.  $V = V_0 \left( 1 - e^{-\frac{t}{RC}} \right)$   
 $V = 0.5 \times \left( 1 - e^{-\frac{0.2 \times 10^{-3}}{12 \times 500 \times 10^{-6}}} \right)$   
 $V = 0.0164 \text{ V}$

10.



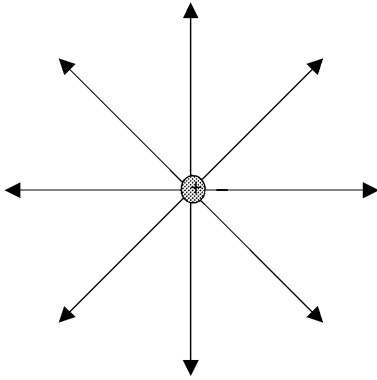
11.  $\frac{\Delta Q}{\Delta t} = -\frac{Q}{RC}$   
 $Q_0 = 28.3 \text{ mC}$   
 $Q_1 = 28.3 \times 10^{-3} - \frac{(28.3 \times 10^{-3})}{44.0 \times 10^{-6} \times 15.5 \times 10^3} \times 0.1 = 0.02415$   
 $Q_2 = 0.02061$   
 $Q_3 = 0.01759$   
 ...  
 $Q_9 = 6.793 \times 10^{-3} \text{ C}$   
 $Q_{10} = \mathbf{5.797 \text{ mC}}$

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## 8: Electric fields

1.



$$E = \frac{1}{4\pi\epsilon_0} \frac{Q}{r^2}$$

$$E = \frac{1}{4\pi \times 8.85 \times 10^{-12}} \frac{1.0 \times 10^{-6}}{0.03^2}$$

$$E = 3.0 \times 10^{12} \text{ V m}^{-1} \text{ (or N C}^{-1}\text{)}$$

3. Electric field strength is defined as the force per unit charge on a positive test charge.

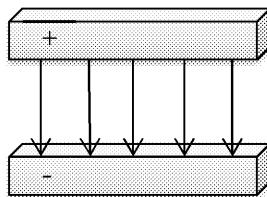
4. The direction of the force on a positive test charge placed in the electric field.

$$E = \frac{F}{Q}$$

$$E = \frac{50.0 \times 10^{-3}}{2.10 \times 10^{-3}}$$

$$E = 23.8 \text{ V m}^{-1} \text{ (or N C}^{-1}\text{)}$$

6. a)



$$b) \quad \frac{F}{Q} = \frac{V}{d}$$

$$F = \frac{VQ}{d}$$

$$F = \frac{5 \times 1.1 \times 10^{-3}}{0.02}$$

$$F = 0.275 \text{ N}$$

7. a) The force between the charges will decrease.

b) Since the force follows the inverse square law, the force will decrease to a quarter.

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8.

	Gravitational	
Source of force field	Mass	
Force	Inverse square law relationship with respect to distance between masses $F = \frac{GMm}{r^2}$	Inverse square
Field strength	Force per unit mass	
Potential in radial field	Always less than zero	Sign

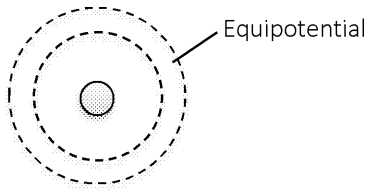
9. **Electric potential:** the work done per unit charge on a unit positive charge when it is moved from infinity to a point in the field.

10.  $\Delta W = Q\Delta V$

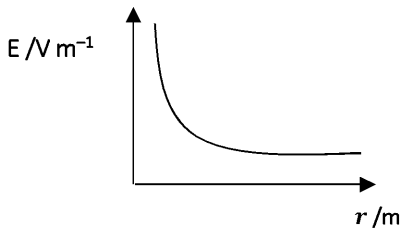
$\Delta W = 4.3 \times 10^{-6} \times 12$

$\Delta W = 5.16 \times 10^{-5} \text{ J}$

11.



12. a)



b) The area enclosed by two points on the E-R graph.

13. **Dielectrics** are electrically insulating materials.

14. Capacitor 1,  $C = \frac{A\epsilon_0\epsilon_r}{d}$

15.  $C = \epsilon_r C_0$

$C = 7 \times 42 \times 10^{-6}$

$C = 2.9 \times 10^{-4} \text{ F}$

16. a)  $C = \frac{A\epsilon_0\epsilon_r}{d}$

$C = \frac{0.03 \times 8.85 \times 10^{-12} \times 2.3}{0.01}$

$C = 6.11 \times 10^{-11} \text{ F}$

b) The capacitance would be greater because capacitance is directly proportional to the area in a larger area.

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## 9: Electromagnetism

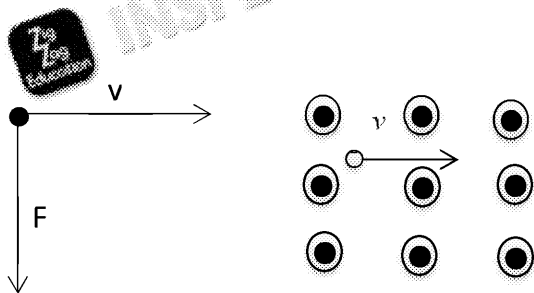
1. **Magnetic flux density:** is magnetic field strength acting through a unit area.

2. a)  $F = BIL$   
 $F = 0.3 \times 0.6 \times 3.2$   
 $F = 0.6 \text{ N}$

b) To the left

3.  $F = BIL \sin \theta$   
 $\theta = \sin^{-1} \frac{F}{BIL}$   
 $\theta = \sin^{-1} \frac{3.8 \times 10^{-3}}{82 \times 10^{-3} \times 510 \times 10^{-3} \times 1.5}$   
 $\theta = 37^\circ$

4. a)



b)  $F = QvB$   
 $F = -3 \times 10^{-3} \times 1.6 \times 10^4 \times 1.2$   
 $F = 58 \text{ N}$

5. a) Into page

b)  $r = \frac{mv}{QB}$   
 $r = \frac{9.11 \times 10^{-31} \times 2.5 \times 10^7}{1.6 \times 10^{-19} \times 0.16}$   
 $r = 8.9 \times 10^{-4} \text{ m}$

6. **Lenz's law:** the direction of the induced current is always such that it is opposed to the change in magnetic flux that causes it.

7.  $\mathcal{E} = N \frac{\Delta \phi}{\Delta t}$   
 $\mathcal{E} = 50 \times \frac{1.3 \times 0.07}{10}$   
 $\mathcal{E} = 0.455 \text{ V}$

8. a)  $\phi = BA$   
 $\phi = 0.6 \times 0.05 \times 0.1$   
 $\phi = 3 \times 10^{-3} \text{ Wb}$

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b)  $\text{magnetic flux linkage} = BAN$

$$\text{magnetic flux linkage} = 0.6 \times (0.05 \times 0.1) \times 10$$

$$\text{magnetic flux linkage} = 0.03 \text{ Wb}$$

c) The magnetic flux linkage would become  $BAN \cos \theta$ , where  $\theta$  is the angle between the cross-section of the coil.

9.  $\varepsilon = N \frac{\Delta \phi}{\Delta t}$

$$\varepsilon = 50 \times \frac{1.3 \times 0.07}{10}$$

$$\varepsilon = 0.46 \text{ V}$$

10. a)  $\frac{N_s}{N_p} = \frac{V_s}{V_p}$

$$V_s = \frac{N_s}{N_p} \times V_p$$

$$V_s = 25\,000 \times \frac{11\,000}{1000}$$

$$V_s = 275 \text{ kV}$$

b) The electricity can be transmitted at a low current which reduces the power lost to transmit.

- c)
- Resistance in the coils
  - Eddy currents
  - Work done to produce magnetic field

d)  $\text{efficiency} = \frac{I_s V_s}{I_p V_p} \times 100 \%$

$$\text{efficiency} = \frac{2.9 \times 275\,000}{40 \times 25\,000} \times 100 \%$$

$$\text{efficiency} = 79.8 \%$$



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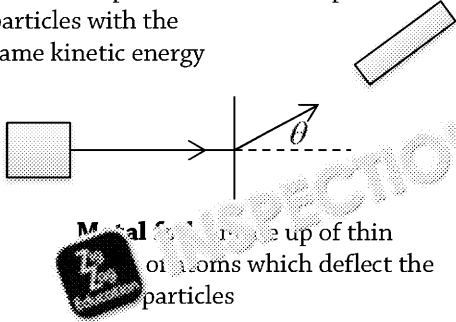


## 10: Nuclei

- The plum pudding model suggested that an atom is a ball of positive charge that is negatively charged. The positive charge balances the negative charge of the electrons.
- Rutherford completed a scattering experiment, the finds of which contradicted J J Thomson's model. It provided evidence that J J Thomson's model was inaccurate.

- Alpha source** – source of alpha particles with the same kinetic energy

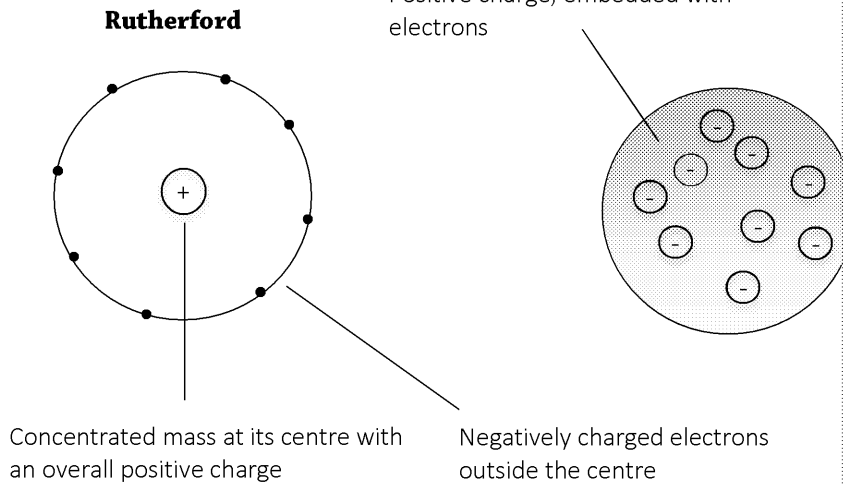
**Microscope** – used to observe the light emitted as particles hit a fluorescent screen



- Most of the alpha particles that came into contact with the gold foil travelled right through. This showed that the majority of the mass isn't distributed throughout the atom but in a very small region.

- Rutherford**

Positive charge, embedded with electrons



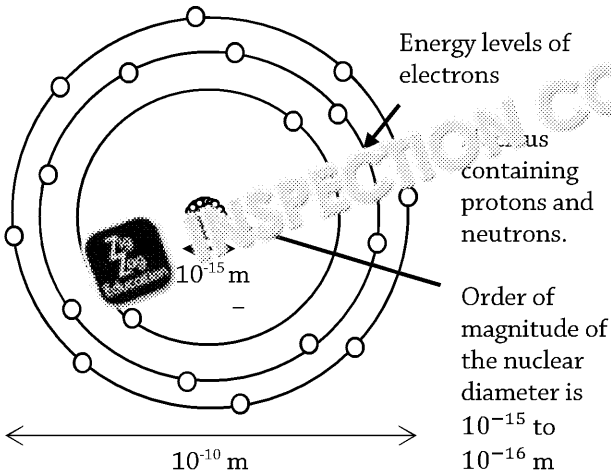
- Energy levels of electrons

Nucleus containing protons and neutrons.

Order of magnitude of the nuclear diameter is  $10^{-15}$  to  $10^{-16}$  m

$10^{-15}$  m

$10^{-10}$  m



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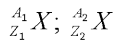


7.

	Charge	Mass
<b>Electron</b>	$-1.6 \times 10^{-19} \text{ C}$	$9.11 \times 10^{-31} \text{ kg}$
<b>Proton</b>	$+1.6 \times 10^{-19} \text{ C}$	$1.67(3) \times 10^{-27} \text{ kg}$
<b>Neutron</b>	$0 \text{ C}$	$1.67(5) \times 10^{-27} \text{ kg}$

8. a) Protons: 92  
Neutrons:  $238 - 92 = 146$   
b) Protons: 2  
Neutrons:  $4 - 2 = 2$

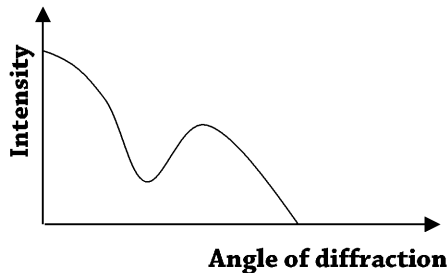
9. Any two nuclei of the same element that have the same proton number, e.g.



where  $Z_1 = Z_2$  and  $A_1 \neq A_2$

10.  $\sim 10^{-15} \text{ m}$

11.



12. Alpha particles are directed towards a nucleus. As the alpha particles approach the nucleus, they gain potential energy. The deflection of the alpha particles can be used to determine the size of the nucleus using Coulomb's law.

13. a)  $V = \frac{4}{3} \pi R^3$

$$V = \frac{4}{3} \pi R_o^3 A$$

$$\rho = \frac{m}{V}$$

$$\rho = \frac{Au}{\frac{4}{3} \pi R_o^3 A}$$

$$\rho = \frac{u}{\frac{4}{3} \pi R_o^3}$$

b)  $\rho = \frac{1.661 \times 10^{-27}}{\frac{4}{3} \pi (1.25 \times 10^{-15})^3}$

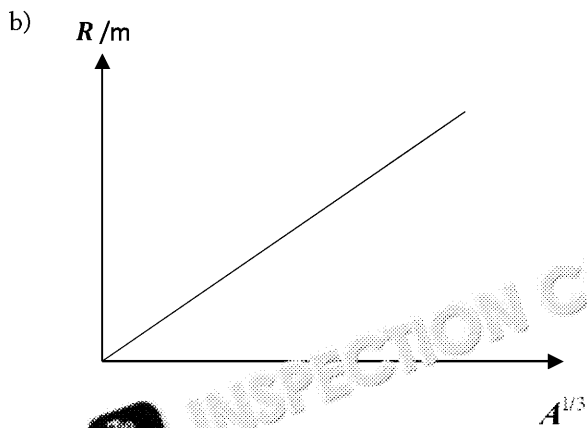
$$\rho = 2.03 \times 10^{17} \text{ kg m}^{-3}$$

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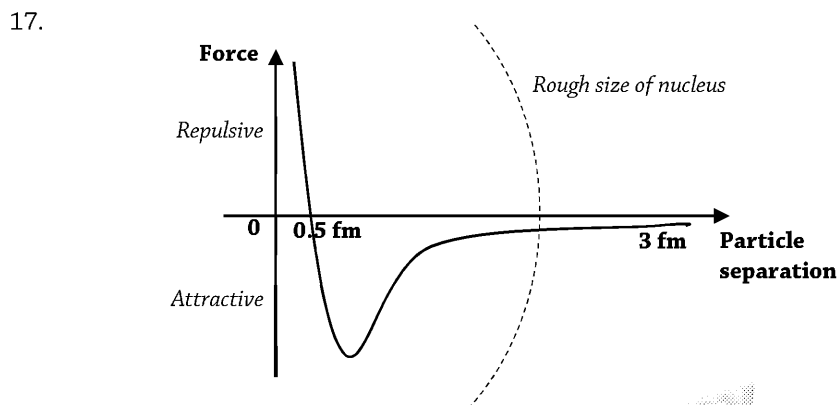
14. a)  $R = r_0 A^{1/3}$   
 $R = 1.25 \times 10^{-15} \times 12^{1/3}$   
 $R = 2.86 \times 10^{-15} \text{ m}$



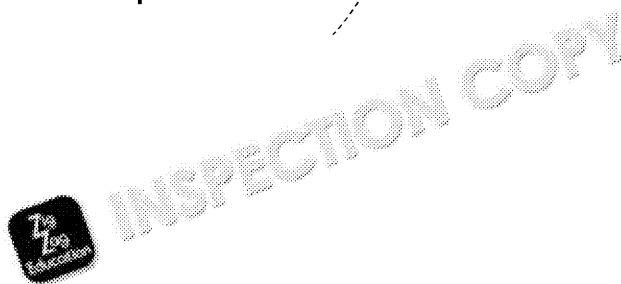
15. **Strong nuclear force:** the attractive force between nucleons, which binds them together

**Unstable nucleus:** a nucleus that has an imbalance of neutrons and protons, creates strong nuclear forces to hold the nucleus together

- 16.
- The strong nuclear force compensates for the repulsive electrostatic force between protons
  - It has a range of 3–4 fm.
  - It has the same effect between two protons as it does between a proton and neutron
  - It is an attractive force from 3–4 fm to 0.5 fm.
  - It is a repulsive force at separation less than 0.5 fm.
  - It is a repulsive force at this separation to ensure that neutrons and protons are not too close together



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## 11: Particles

1. The rest mass of an antiparticle is the same as the rest mass of its corresponding particle. The charge of an antiparticle is equal and opposite to that of its corresponding particle.

2.

	Particle	Charge	Rest mass
<b>Positron</b>	<b>Electron</b>	$+1.6 \times 10^{-19} \text{ C}$	$9.11 \times 10^{-31} \text{ kg}$
<b>Antineutron</b>	<b>Neutron</b>	$0 \text{ C}$	$1.67(5) \times 10^{-27} \text{ kg}$
<b>Antiproton</b>	<b>Proton</b>	$-1.6 \times 10^{-19} \text{ C}$	$1.67(3) \times 10^{-27} \text{ kg}$
<b>Antineutrino</b>	<b>Neutrino</b>	$0 \text{ C}$	$0 \text{ kg}$

3.  $E = hf$

$$f = \frac{E}{h}$$

$$f = \frac{2.0 \times 10^{-18} \text{ J}}{6.63 \times 10^{-34} \text{ J s}}$$

$$f = 4.22 \times 10^{15} \text{ Hz}$$

4. Energy of photon = Rest energy of proton + Rest energy of antiproton

$$hf_{\min} = 2E_o$$

$$2E_o = 2 \times 1.67 \times 10^{-27} \times (3 \times 10^8)^2$$

$$2E_o = 3.01 \times 10^{-10} \text{ J}$$

$$hf_{\min} = 3.01 \times 10^{-10} \text{ J}$$

5. Energy of positron + Energy of electron = Energy of two photons

$$2E_o = 2hf_{\min}$$

$$E_o = hf_{\min}$$

$$E_o = 9.11 \times 10^{-31} \times (3 \times 10^8)^2$$

$$E_o = 8.2 \times 10^{-14} \text{ J}$$

$$hf_{\min} = 8.2 \times 10^{-14} \text{ J}$$

$$f_{\min} = \frac{8.2 \times 10^{-14}}{6.63 \times 10^{-34}}$$

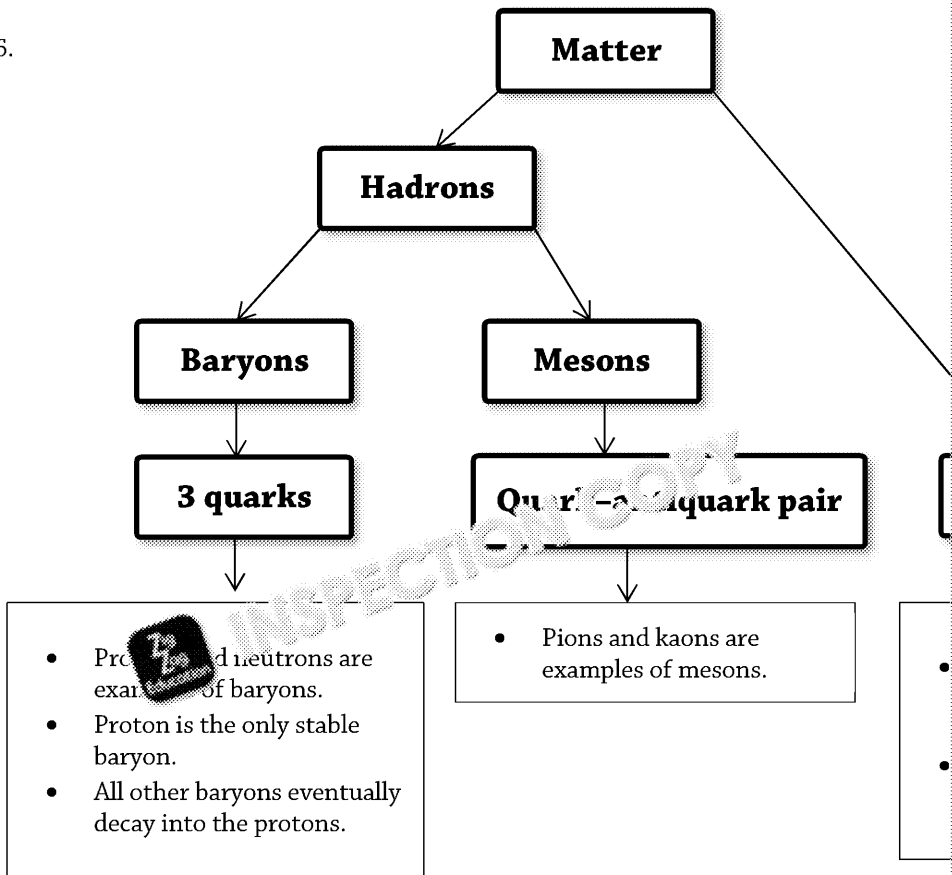
$$f_{\min} = 1.2 \times 10^{20} \text{ Hz}$$

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6.



7. A quark is an elementary particle that is the smallest known constituent that makes

8. a) uud  
 b)  $\bar{u}\bar{d}\bar{d}$   
 c)  $u\bar{s}$   
 d)  $d\bar{d}$  or  $u\bar{u}$

9. a) Up, down, strange

b)  $\frac{1}{3}$

c) Charge of antiquarks: antiup, antidown, antistrange, is  $-\frac{2}{3}, +\frac{1}{3}, +\frac{1}{3}$  respectively

10. a) Valid: Charge, strangeness, and baryon number are conserved.  
 b) Invalid: Charge and lepton number are not conserved.  
 c) Invalid: Baryon number is not conserved

11. a)  $\mu^- \rightarrow e^- + \bar{\nu}_e + \nu_\mu$

b)  $K^0 + p \rightarrow n + \pi^+$

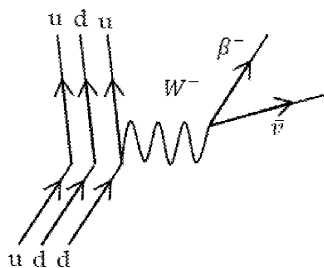
12. a) Strong nuclear interaction  
 b) Weak nuclear interaction  
 c) Indistinguishable particles are always created in pairs  
 d)
  - $uds$
  - $uds$

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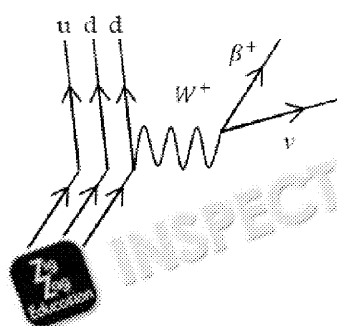
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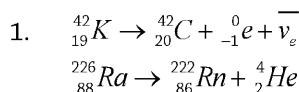
13. a)



b)



**12: Radioactive decay**



2.

Type of radiation	Nature	Range in air	Ionisation	Absorption
<b>Alpha</b>	Two protons + two neutrons	<100 mm	Creates around $10^4$ ions per cm in air	Stopped by metal foil or paper
<b>Beta</b>	Electron or positron	<1 m	Creates around 100 ions per mm in air	Stopped by 3-5 mm aluminium
<b>Gamma</b>	Photon of energy	Obeys inverse square law	Weakly ionising	Stopped by several cm lead

3. Mass before =  $m_U + m_n = (235.0439 + 1.0087) \text{ u} = 236.0526 \text{ u}$   
 Mass after =  $m_{Kr} + m_{Ba} + 3 \times m_n = (93.9198 + 142.9206 + 3 \times 1.0087) \text{ u} = 235.8662 \text{ u}$   
 $\Delta m = m_{\text{before}} - m_{\text{after}} = (236.0526 - 235.8662) \text{ u} = 0.1864 \text{ u}$   
 $\Delta E = 0.1864 \times 931.5 \text{ MeV} = 173.6 \text{ MeV}$

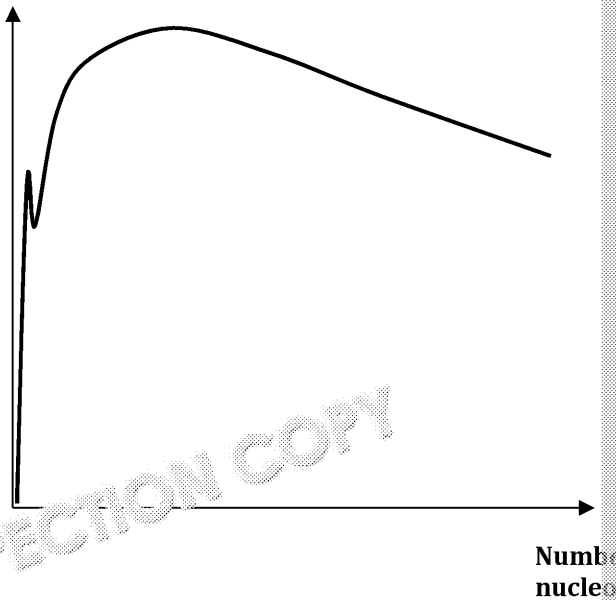
4.  $\Delta m = Z m_p + (A - Z)m_n - M_{\text{nucleus}}$   
 $\Delta m = 38 \times 1.0073 \text{ u} + (90 - 38) \times 1.0087 \text{ u} - 89.9077 \text{ u} = 0.8221 \text{ u}$   
 $\Delta E = 765.8 \text{ MeV}$

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5. Binding energy per nucleon /MeV



6. Nuclear fission is the process of a larger nucleus splitting into two smaller nuclei, while separate nuclei fusing together to produce a larger nucleus.
7. It cannot be determined when the next decay will occur, or which atoms will be the next to decay.

8. a)  $N = N_0 e^{-\lambda t}$   
 $N = 4.7 \times 10^{24} \times e^{-2.5 \times 10^{-4} \times 2400}$   
 $N = 2.6 \times 10^{24}$

b)  $A = \lambda N$   
 $A = 2.5 \times 10^{-4} \times 2.6 \times 10^{24}$   
 $A = 6.5 \times 10^{20} \text{ Bq}$

c)  $A = A_0 e^{-\lambda t}$   
 $A_0 = \frac{A}{e^{-\lambda t}}$   
 $A_0 = \frac{6.5 \times 10^{20}}{e^{-2.5 \times 10^{-4} \times 2400}}$   
 $A_0 = 1.2 \times 10^{21} \text{ Bq}$

9. a) 5 days

b)  $T_{1/2} = \frac{\ln 2}{\lambda}$   
 $\lambda = \frac{\ln 2}{T_{1/2}}$   
 $\lambda = \frac{\ln 2}{5 \times 24 \times 60 \times 60}$   
 $\lambda = 1.6 \times 10^{-6} \text{ s}^{-1}$

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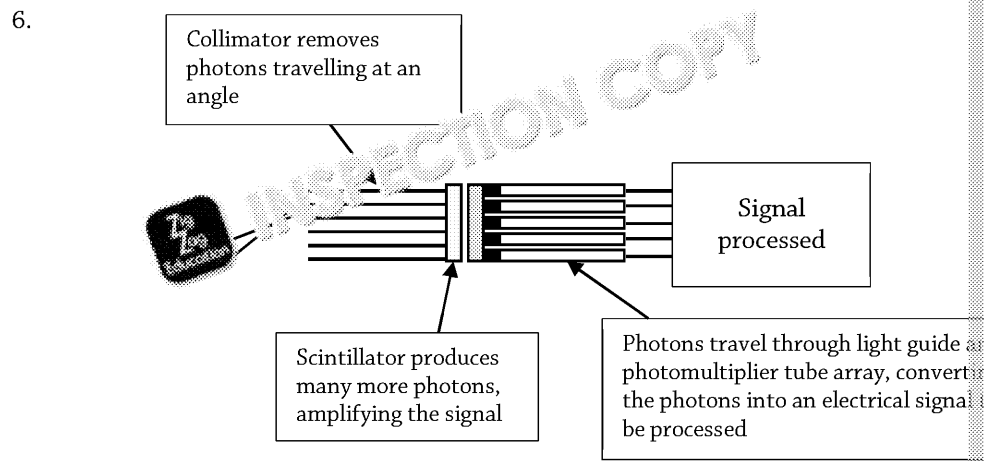


10. • Fission can be induced by hitting the uranium isotope  ${}^{235}_{92}\text{U}$  with neutrons.
  - The uranium isotope is split roughly into two equal smaller nuclei and two or three neutrons are released.
  - Fission (thermal) neutrons can be harnessed and used to cause more fission events to be induced.
11. The critical mass of a fissile material is the minimum mass required to sustain fission during fission events going on to induce fission in other nuclei.
12. • The moderator keeps the neutrons at a low enough speed to be able to induce fission.
  - The control rods absorb neutrons, stopping runaway fission events. They can be moved in and out of the situation.
  - The coolant extracts the heat and allows it to be transferred to be used to produce electricity.

**13: Medical imaging**

1. X-rays are produced by accelerating electrons through a potential and colliding them with a metal target. As the electrons hit the target and suddenly decelerate, their kinetic energy is converted to X-rays.
 

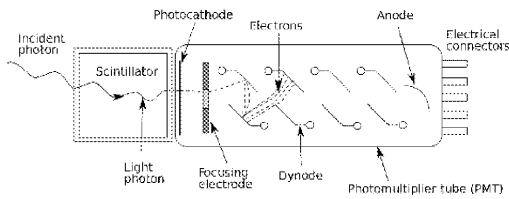
Electrons are released via thermionic emission – the cathode heats up and releases electrons. As the electrons are accelerated, they gain energy,  $E = eV$ .
2.  $I = I_0 e^{-\mu x}$   
 $\mu = -\frac{1}{x} \ln \frac{I}{I_0} = -\frac{1}{3.50} \times \ln 0.122 = 0.6011 \text{ cm}^{-1}$   
 $\mu_m = \frac{\mu}{\rho} = \frac{0.6011}{1.8} = 0.334 \text{ cm}^2 \text{ g}^{-1}$
3. **Simple scatter:** 1–20 keV. X-rays are absorbed and re-emitted by atoms without changing energy.  
**Photoelectric effect:** < 100 keV. X-rays are absorbed by an electron which then leaves the atom.  
**Compton effect:** 0.5–5.0 MeV. X-rays are partly absorbed by an electron leaving the electron with reduced energy.  
**Pair production:** > 1.02 MeV. X-rays are converted into an electron–positron pair.
4. A CT scan involves a series of narrow beams of X-rays passed over the patient. Each beam produces a 360° image of a ‘slice’ of the patient, and the camera then moves to the next ‘slice’. CT scans are much slower and more expensive than traditional X-rays, but produce better images. CT scans can also pose the risk of higher X-ray doses to the patient.
5. Gives off gamma rays so can be detected by a gamma camera. Half-life of around six hours so can be made to go to a specific site.



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7.



In a photomultiplier tube, an incident photon is converted into a burst of light photons, which are then amplified into a large number of electrons.

8. Ultrasound scans use sound energy to look inside the body non-invasively.
- At each tissue boundary, some energy is reflected back.
  - The amount of energy reflected back depends on the specific acoustic impedance of the tissues.
  - The reflections can be used to build up an image.

9. Piezoelectric materials expand and contract when an AC current is applied to them.
- Current oscillations cause contractions and expansions.
  - Pressure differences caused by these rapid contractions create sound waves.
  - The sound waves are used to perform the ultrasound scan.
  - Piezoelectric materials can also work in reverse, by converting sound energy to electrical energy.
  - This electrical signal is detected and used to build up a picture.

10. A-scans are single short pulses of sound.  
B-scans are a rapid series of A-scans.

11. Advantages
- Non-invasive
  - Useful for soft tissues
  - Inexpensive and portable

Disadvantages

- Can't see behind hard tissue
- Needs a skilful technician

12.  $Z = \rho c$   
 $\rho = \frac{Z}{c} = \frac{6.48 \times 10^6}{3500}$   
 $\rho = 1850 \text{ kg m}^{-3}$

13.  $Z_{fat} = 952 \times 1450 = 1.380 \times 10^6 \text{ kg m}^{-3}$   
 $\frac{I_r}{I_i} = \left( \frac{Z_{fat} - Z_{skin}}{Z_{fat} + Z_{skin}} \right)^2 = \left( \frac{1.380 \times 10^6 - 1.99 \times 10^6}{1.380 \times 10^6 + 1.99 \times 10^6} \right)^2$   
 $\frac{I_r}{I_i} = 0.0328$

14. Ultrasound can be used to measure the blood flow velocity by using the Doppler effect. The sound waves are sent into the blood, and it is reflected back, with the change in frequency giving the velocity.

15.  $\frac{\Delta f}{f} = \frac{2v \cos \theta}{c}$   
 $v = \frac{c \Delta f}{2f \cos \theta} = \frac{1570 \times 9.16 \times 10^{-4}}{2 \times 6.00 \times 10^6}$   
 $v = 0.209 \text{ m s}^{-1}$

16. In a PET scan, a positron-emitting tracer is injected into the patient. The positron emitted quickly interacts with an electron, and the two annihilate. Two gamma rays are emitted at 180° from one another. The two gamma rays are detected by the scanner, and the annihilation is calculated.

17.  $^{18}\text{F}$  is used as it can form a molecule called fludeoxyglucose (FDG), which is treated by the body. This means that FDG quickly moves towards areas of the body with high rates of metabolism.  $^{18}\text{F}$  also emits positrons; therefore, the gamma rays produced by them annihilating with electrons. The two-hour half-life means little risk is posed to the patient.

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