

Mastering Maths for AS and A Level Physics

Basic Maths Skills

Second Edition, May 2024

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Teacher's Introduction

The following exam boards have a published list of the mandatory mathematical skills requirement for each of their Physics courses:

- AS and A Level AQA Physics (7407 and 7408)
- AS and A Level OCR Physics A (H156 and H556)
- AS and A Level OCR Physics B (H157 and H557)
- AS and A Level Edexcel Physics (8PH0 and 9PH0)
- AS and A Level WJEC Eduqas Physics (B420QS and A420QS)
- AS and A Level WJEC Physics (2420 series and 1420 series)

The required mathematical skills are driven by the Department for Education. The assessment marks of quantitative skills in both AS and A Level papers will comprise a minimum of 40% of the required mathematical skills for Physics (Level 2 or above).

Physics students sometimes find the mathematical skills required for success a challenge, especially when expected to apply them to the context of physics. This Mastering Maths skills resource has been designed with the intention of providing them with the opportunity to review the mathematical skills familiar to them from GCSE higher-tier courses, and practise them in the context of the specific topics in the Physics course that require an understanding of them. This pack outlines the basic maths skills required (see mapping document in Chapter 1) and allows students to become comfortable and competent with the basics before teaching the Physics course.

The resource is split into **three chapters**:

Chapter One: Mapping Table

This section includes a table mapping each basic maths skill outlined in the exam boards' published list to each specification point where the skill is found.

Chapter Two: Diagnostic Test

This section includes two diagnostic tests, of the same format, that cover all the basic mathematical skills outlined by the exam board. Both tests have the same format and therefore can act as an effective comparison tool, and each has questions increasing in difficulty and therefore accessible to varying abilities.

It is recommended that the students are given the first diagnostic test to complete before the AS Physics course has been taught, with the purpose of highlighting any gaps in their knowledge and assessing their competency.

The second test is slightly harder and can be given at any point during the course. The second test works on two levels; it is a useful positive reinforcement tool for the students, where they can see how their knowledge has improved, and can also assess where the areas of difficulty and gaps in the knowledge still remain.

Both tests indicate the mathematical skills tested in each question, and therefore specific skills with which the students are still struggling can be particularly identified.

Chapter Three: Basic Maths Skills

This section covers all the basic mathematical skills mentioned in the exam boards' published requirements list, which students should be familiar with from their GCSE Maths courses.

Students have the opportunity to complete both short and structured questions that will help develop the necessary numerical skills and consolidate understanding. These questions should build students' confidence in having the required ability to demonstrate their full potential in AS and A Level Physics, in both class and examination conditions.

Each basic maths skill is structured as follows:

- **Part A: Specification Overview** – this provides an overview of the skill and explains to the student what the exam board requires them to demonstrate in the exam with the skill.
- **Part B: Theoretical Overview** – a brief summary recapping the skill and demonstrating how the student is to apply the skill to the context of their physics topics.
- **Part C: Example** – detailed numerical example with worked solution of the skill in context of a topic where the skill will be found.
- **Part D: Practice Activity** – each skill is concluded with practice questions that increase in difficulty. All the physics knowledge needed to complete the question will be provided and the question focuses on testing the student's understanding of the maths skill itself.

This is followed by:

- The **Mark Scheme for Diagnostic Test**, which provides a mark scheme with worked solutions for the diagnostic test.
- Suggested **Answers to Part D: Practice Questions**, which provides worked solutions for each set of practice questions.

October 2016

Second edition, May 2024

A number of improvements have been made from the first edition.

CHAPTER 1: MAPPING MATHS SKILLS TO SPECIFICATION POINTS

AQA	OCR (A/B)	Edexcel	WJEC/ Eduqas	Skills in bold font are only tested in the full A Level course	Basic skills	Further skills
Arithmetic and numerical computation						
MS 0.1	M 0.1	C.0.1	No reference numbers	Recognise and make use of appropriate units in calculations	B1	
MS 0.2	M 0.2	C. 0.2		Recognise and use expressions in decimal and standard form	B2	
MS 0.3	M 0.3	C.0.3		Use ratios, fractions and percentages	Tested throughout skills	
MS 0.4	M 0.4	C 0.4		Estimate results	B3	
MS 0.5	M 0.5	C.0.5		Use calculators to find and use power functions, exponential and logarithmic functions	B7	F10, F11
MS 0.6	M 0.6	C.0.6		Use calculator to handle sin x, cos x, tan x when x is expressed in degrees or radians	B6	
Handling data						
MS 1.1	M 1.1	C.1.1	No reference numbers	Use an appropriate number of significant figures	B4	
MS 1.2	M 1.2	C.1.2		Find arithmetic means	B5	
MS 1.3	M 1.3	C.1.3		Understand simple probability	B16	
MS 1.4	M 1.4	C.1.4		Make order of magnitude calculations	B1	
MS 1.5	M 1.5	C.1.5		Identify uncertainties in measurements and use simple techniques to determine uncertainty when data are combined by addition, subtraction, multiplication, division and raising to powers	B10, B11	
Algebra						
MS 2.1	M 2.1	C.2.1	No reference numbers	Understand and use the symbols: =, <, <<, >>, >, α, ≈, Δ	B15	
MS 2.2	M 2.2	C.2.2		Change the subject of an equation, including non-linear equations	B8	
MS 2.3	M 2.3	C.2.3		Substitute numerical values into algebraic equations using appropriate units for physical quantities	B9	
MS 2.4	M 2.4	C.2.4		Solve algebraic equations, including quadratic equations	B9	
MS 2.5	M 2.5	C.2.5		Use logarithms in relation to quantities that range over several orders of magnitude		F11
Graphs						
MS 3.1	M 3.1	C.3.1	No reference numbers	Translate information between graphical, numerical and algebraic forms		F5
MS 3.2	M 3.2	C. 3.2		Plot two variables from experimental or other data		F4
MS 3.3	M 3.3	C.3.3		Understand that $y = mx + c$ represents a linear relationship	B8	F5
MS 3.4	M 3.4	C.3.4		Determine the slope and intercept of a linear graph		F5
MS 3.5	M 3.5	C.3.5		Calculate rate of change from a graph showing a linear relationship		F6
MS 3.6	M 3.6	C.3.6		Draw and use slope of tangent to curve as a measure of rate of change		F6
MS 3.7	M 3.7	C.3.7		Distinguish between instantaneous rate of change and average rate of change		F6
MS 3.8	M 3.8	C.3.8		Understand the possible physical significance of the area between a curve and the x-axis and be able to calculate it or estimate it by graphical methods as appropriate		F8
MS 3.9	M 3.9	C.3.9		Apply concepts underlying calculus (but without requiring the explicit use of derivatives or integrals) by solving equations involving rates of change, e.g. $\frac{\Delta x}{\Delta t} = -\lambda x$ using graphical method or spreadsheet modelling		F7
MS 3.10	M 3.10	C.3.10		Interpret logarithmic plots		F12
MS 3.11	M 3.11	C.3.11		Use logarithmic plots to test exponential and power law variations		F12
MS 3.12	M 3.12	C.3.12		Sketch relationships which are modelled by $y = \frac{k}{x}$, $y = kx^2$, $y = \frac{k}{x^2}$, $y = kx$, $y = \sin x$, $y = \cos x$, $y = e^{ax}$ and $y = \sin^2 x$, $y = \cos^2 x$ as applied to physical relationships		F9

Geometry and trigonometry						
MS 4.1	M 4.1	C.4.1	No reference numbers	Use angles in regular 2D and 3D structures	B12	
MS 4.2	M 4.2	C.4.2		Visualise and represent 2D and 3D forms including two-dimensional representations of 3D objects	B14	
MS 4.3	M 4.3	C.4.3		Calculate areas of triangles, circumferences and areas of circles, and surface areas and volumes of rectangular blocks, cylinders and spheres	B14	
MS 4.4	M 4.4	C. 4.4		Use Pythagoras's theorem, and the angle sum of triangle		F1
MS 4.5	M 4.5	C. 4.5		Use sin, cos, and tan in physics problems		F2
MS 4.6	M 4.6	C.4.6		Use small angle approximations including $\sin \theta \approx \theta$, $\tan \theta \approx \theta$, $\cos \theta \approx 1$ for small θ where appropriate		F3
MS 4.7	M 4.7	C.4.7		Understand the relationship between degrees and radians and translate from one to the other	B13	

Maths skill in this resource	Maths skill in specification
Skill B1	Skills 0.1/1.4
Skill B2	Skill 0.2
Skill B3	Skill 0.4
Skill B4	Skill 1.1
Skill B5	Skill 1.2
Skill B6	Skill 0.6
Skill B7	Skill 0.5
Skill B8	Skill 2.2
Skill B9	Skills 2.3/2.4
Skill B10	Skill 1.5
Skill B11	Skill 1.5
Skill B12	Skill 4.1
Skill B13	Skill 4.7
Skill B14	Skills 4.2/4.3
Skill B15	Skill 2.1
Skill B16	Skill 1.3

Diagnostic Test 1

1. Write the following number in standard form: 4,580,000
2. Write the following number as a whole number: 9.37×10^4
3. Convert 151° into radians
4. Convert 0.15 radians into degrees
5. State the equation for determining the area of the following shapes:
 - a) Circle
 - b) Right-angled triangle
6. Write the following numbers to 4 significant figures:
 - a) 402,369.2
 - b) 0.2048539
7. State the SI units of the following physical quantities:
 - a) Mass
 - b) Length
 - c) Current
 - d) Power
8. Evaluate x in the following equations. Assume that each equation is
 - a) $\sin x = 0.630$
 - b) $\cos 32 = x$
 - c) $\tan 156 = x$
9. The temperature of the sun is 5778 K.
 - a) Write the temperature of the sun in standard form
 - b) Write the value for the temperature of the sun to 3 significant figures
10. Explain in words the following mathematical statements:
 - a) $A \propto \Delta B$
 - b) $C \leq D < E$
 - c) $F \gg G \geq H$

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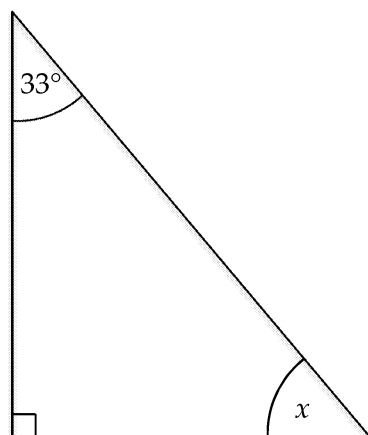
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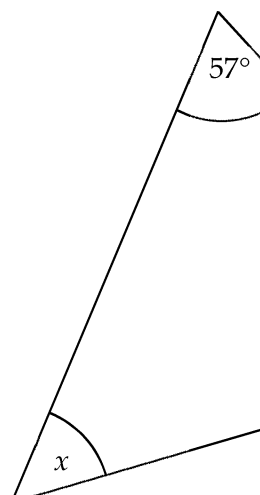
11. Find the missing angle x in the following triangles.

Note: the following diagrams are not to scale.

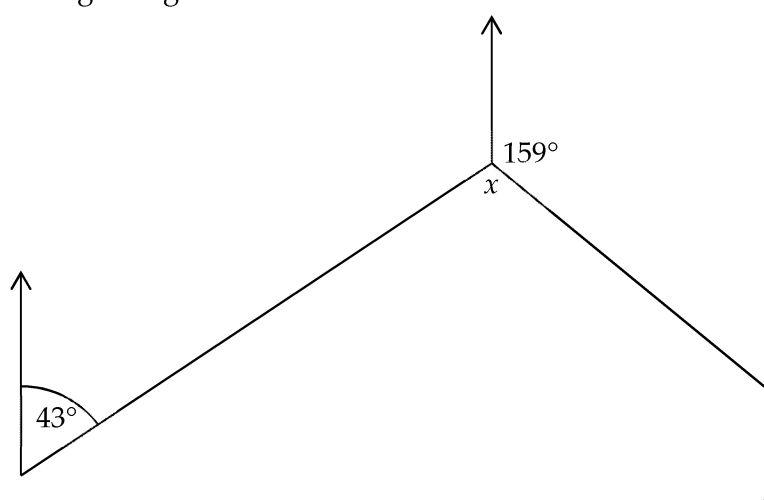
a)



b)



12. A boat is travelling on an initial bearing of 43° and then changes course. The boat bearing changes to 159° .



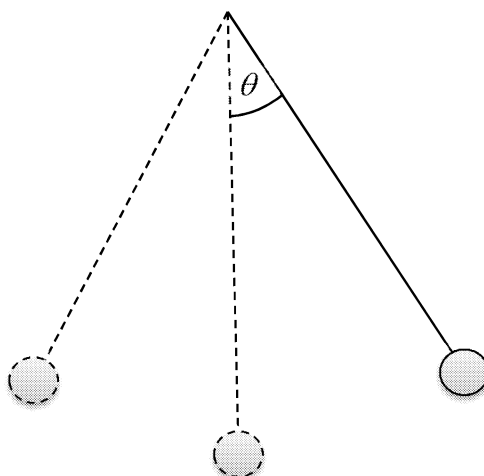
Determine the angle x .

13. Given that $P = I^2 R$ and $I = 3.00 \text{ A}$ and $R = 14.0 \Omega$, find P .
14. Given the following results for frequency f and wavelength λ
- $$f = 2.3 \pm 0.1 \text{ Hz}; \lambda = 0.02 \pm 0.01 \text{ m}$$
- State the absolute uncertainty of f
 - State the absolute uncertainty of λ
 - Determine the velocity of the wave with the equation $v = f \lambda$, including the uncertainty
15. A Physics student measured value for density of a block to be $56.9 \pm 0.5 \text{ g cm}^{-3}$. Determine the percentage uncertainty in the value for density.

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16. A lab technician measures the length of an electrical wire to be 0.21 m. The lab technician measures the length of the wire again a few hours later. Determine the percentage change in the measured value for length of the wire.
17. When we discuss a pendulum swinging, we don't discuss the distance in metres m but through an angle θ .



The equation for determining the angle the pendulum has swung through is:

$$\theta = A \sin(xt)$$

where $A = 3.40$ m, $x = 1.60$ rads^{-1} and $t = 1.70$ s.

Calculate the angle the pendulum has swung through using the equation in degrees.

18. In physics, we use the equations of motion to determine how an object moves. The equation for determining the final velocity of an object is:

$$v^2 = u^2 + 2as$$

where v is the final velocity of an object, u is the initial velocity, a is the acceleration and s is the displacement travelled by the object.

If a cyclist is initially cycling at 5.8 ms^{-1} , and begins to accelerate at 0.5 ms^{-2} .

d) What will the final velocity (v) of the cyclist be after 10 m?

19. An astronomer is attempting to determine the velocity of our galaxy. She obtains the following measurements:

Velocity (kmh^{-1})				
v_1	v_2	v_3	v_4	
828×10^3	827×10^3	824×10^3	827×10^3	

Calculate the mean of the astronomer's results.

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20. Using your knowledge of probability, explain how the process of three successive decays of a radioactive nucleus is a random process of radioactive decay.

21. A charged particle gains energy as it travels between two electrically charged parallel plates. The equation for the kinetic energy gained by an initially stationary particle is

$$E_k = \frac{1}{2}mv^2$$

a) State the SI base unit for energy.

A charged particle of mass 1.67×10^{-27} kg reaches a maximum velocity of 1.5×10^6 m s⁻¹ between two charged plates.

b) Use the energy equation to determine the energy gained by the particle between the plates. Give your answer in standard form.

c) Write your answer to (b) using a prefix.

22. A spring with a spring constant $k = 3.0 \times 10^4$ N m⁻¹ is extended by 20 cm. A force must have been acting on the spring in order to extend it. The equation for the force exerted on the spring is

$$F = kx$$

where x is the extension length and k is the spring constant.

a) Calculate the force exerted on the spring.

b) Convert your answer to (a) into kN.

23. The equation for the gravitational potential energy of an object of mass m at a distance r from the centre of a massive body with mass M is given by:

$$E_{\text{grav}} = -\frac{GMm}{r}$$

a) In a system where the massive body is the Sun and the object orbiting it is a satellite, calculate the gravitational potential energy of the system.

Note:

G is a gravitational constant given by 6.67×10^{-11} N m² kg⁻²

The mass of the Sun is 1.99×10^{30} kg

The mass of Earth is 6.00×10^{24} kg

The distance between Earth and the Sun is 1.50×10^{11} m

b) What is your answer to (a) in kJ?

c) Write your answer to (a) to 1 significant figure.

Similarly, the force of attraction (gravitational force) between two bodies is given by the following formula:

$$F = -\frac{Gm_1m_2}{r^2}$$

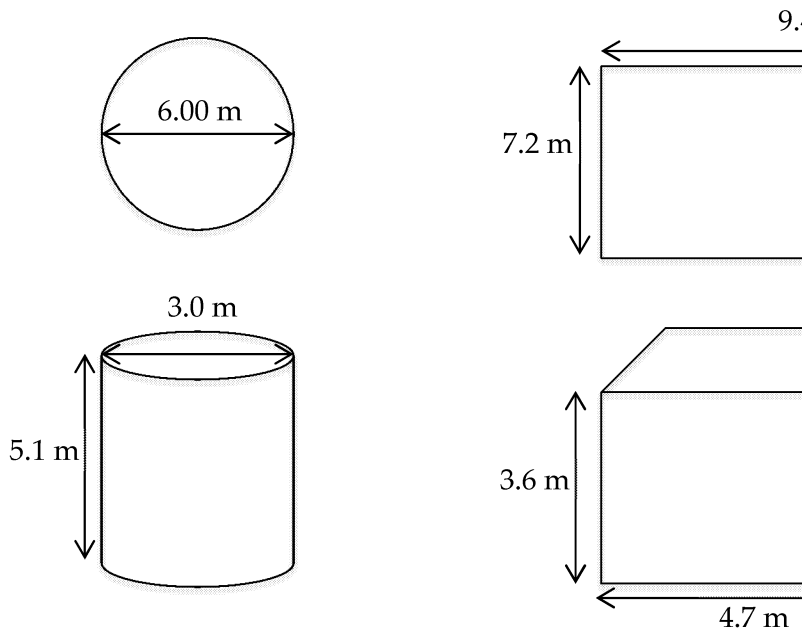
d) Using this formula, estimate the force of attraction between an object of mass 1 kg and the Earth at a distance of one metre, in the absence of any other objects. Apply your answer to (d) to the force of attraction between two objects of mass 1 kg each at a distance of one metre. (Skills)

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Diagnostic Test 2

1. Write the following number in standard form: 236,900,000
2. Write the following number as a whole number: 6.31×10^{-3}
3. Convert 68° into radians
4. Convert 1.28 radians into degrees
5. Determine the area/volume of the following shapes:



6. Write the following numbers to 6 significant figures:
 - a) 53021.59
 - b) 0.0365821
 - c) 0.00000023 (provide an answer with the fewest number of decimal places)
7. State the SI units of the following physical quantities:
 - a) Amount of a substance
 - b) Resistance
 - c) Volume
 - d) Time
8. Evaluate x in the following equations. Assume that each equation is in degrees.
 - a) $\cos x = 0.69$
 - b) $\sin 89 = x$
 - c) $\tan x = 0.47$

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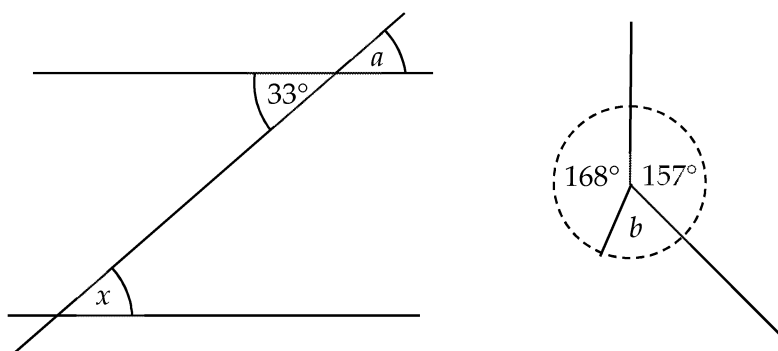
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9. The universe is 13,820,000,000 years old.
- Write the age of the universe in standard form.
 - Write the value for the age of the universe to 3 significant figures
10. Explain in words the following mathematical statements:
- $A \ll B \ll \Delta C$
 - $C \leq \frac{\Delta D}{\Delta E}$
 - $F \propto x$ if $x \geq 3$

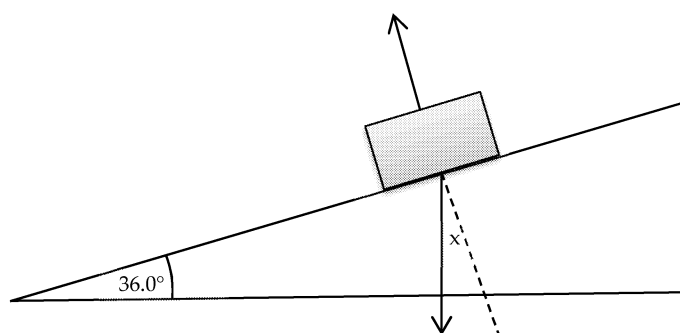
11. Find the missing angles:

Note: the following diagrams are not to scale.



12. A rally car company draws a force diagram of the forces acting on the car to assess its movement.

The angle x is missing from the force diagram.



- Using your knowledge of angles, evaluate the missing angle x .

If the rally car parks on a slope without its handbrake on it will slide down the slope due to gravity. The acceleration at which it slides due to gravity is given by

$$a = g \sin x$$

- Using your answer to (a) determine the acceleration down the slope.

Note: You can assume that the friction between the tyres and the slope is negligible.

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13. Given that $s = ut + \frac{1}{2}at^2$ and $u = 2.50 \text{ ms}^{-1}$, $t = 150 \text{ s}$ and $a = 0.200 \text{ m}$

14. Given the following results for frequency f and wavelength λ :

$$f = 150 \pm 1 \text{ Hz}; \lambda = 3.3 \pm 0.1 \text{ m}$$

- State the absolute uncertainty of f
- State the absolute uncertainty of λ
- Determine the velocity of the wave with the equation $v = f\lambda$

15. A Physics student obtains the following measurement for resistance:

Determine the percentage uncertainty of the value for resistance.

16. A research group is completing experimental tests into the correlation

The group exerts a constant force on a table and measures the resulting pressure. The first reading is $30 \pm 2 \text{ Pa}$.

The group increases the force exerted and the measurement for pressure is $45 \pm 3 \text{ Pa}$.

Determine the percentage increase from the first reading in the measurement of pressure.

17. Charged particles accelerate between electrically charged plates.

The potential difference V between the plates is determined using the final velocity of an initially stationary charged particle:

$$V = \frac{mv^2}{2e}$$

An electron ($m_e = 9.11 \times 10^{-31} \text{ kg}$; $e = 1.6 \times 10^{-19} \text{ C}$) reaches a final velocity of $5.0 \times 10^6 \text{ ms}^{-1}$ between two charged plates.

Determine the potential difference between the plates.

18. An energy company completes operational testing into the efficiency of its power stations.

It repeated the test a number of times and achieved the following results:

E_1	E_2	E_3	E_4	
98.6%	98.9%	98.7%	98.9%	

Calculate the mean of the energy company's results for energy efficiency.

19. The kinetic energy of a moving object can be calculated using the following formula:

$$E_k = \frac{1}{2}mv^2$$

Using this formula, estimate the kinetic energy of a car driven on a motorway. Apply sensible estimations where necessary.

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20. Ohm's law states that, for any electrical component:

$$V \propto I$$

if the temperature of the component is constant.

- a) Explain the mathematical statement ($V \propto I$) given for Ohm's law.

The equation form of Ohm's law is:

$$V = IR$$

A bulb in an electrical circuit has 2.30 A flowing through it and has a resistance of 10.0 Ω.

- b) Calculate the potential difference across the bulb.

21. A student has a set of 140 square dice. The student rolls the dice and records the number of dice with the number 4 facing upwards. The student rolls the remaining dice.

Explain why this process is a useful model for representing the random nature of radioactive decay.

22. All masses produce a gravitational field and this field exerts a force on any mass that enters this field.

The force between two masses can be determined using the following equation:

$$F = -\frac{GMm}{r^2}$$

where M is the mass of the larger of the two masses, m is the mass of the smaller mass, r is the distance between the two masses and G is the gravitational constant.

- a) Estimate the gravitational force between Earth and the Moon
($m_M = 7.35 \times 10^{22}$ kg, $M = 6.00 \times 10^{24}$ kg, $r = 4.00 \times 10^8$ m).
b) Give your answer to (a) in kN.
c) Write your answer to (a) to 2 significant figures.

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CHAPTER 3: BASIC MATHS SKILLS

This chapter will simply recap the basic maths skills required for this course. You should be comfortable with these skills before tackling the further maths skills that are more familiar from GCSE, Year 9 and Year 8 Maths courses.

SKILL B1: UNITS, CONVERSION BETWEEN UNITS AND ORDER OF MAGNITUDE

Part A: Specification Overview

The course will expect you to be able to identify and use appropriate units for different physical quantities.

This skill will be tested throughout every topic in this course.

Part B: Theoretical Overview

International System (SI) of Base Units

SI base units are a set of units of measure. The set of units can then be used to derive other units.

When calculating physical quantities in this course you will need to include units. The units will not be given to you and you will be expected to recall the SI base units.

Any calculation involving quantities with units that aren't SI base units will require you to convert the units or be able to derive them from the SI base units.

The following SI base units and their corresponding physical quantities are listed below.

Physical Quantity	SI Base Units	Common Abbreviations
Mass	kilogram	kg
Time	second	s
Luminous intensity	candela	cd
Thermodynamic temperature	kelvin	K
Length	metre	m
Electric current	ampere	A
Amount of a substance	mole	mol

You will be expected to present physical quantities in their SI base units unless otherwise stated. For example, if you are using distance and time to determine velocity, the distance must be in metres and seconds respectively to perform the calculation.

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Conversion between units

You will also have to be able to convert between units. You may be given magnitude and need to convert back to the SI unit in order to perform the

Prefixes can be used to convert between units in different orders of magnitude which is used before the unit to let you know the order of magnitude.

Prefix	Order
pico (p)	
nano (n)	
micro (μ)	
milli (m)	
centi (c)	
deci (d)	
kilo (k)	
mega (M)	
giga (G)	
tera (T)	

Part C: Worked Example

A family car travels 8.00 km in 10.0 minutes. The velocity of the car is given by $v = \frac{s}{t}$. Calculate the velocity of the car during the 10.0 minutes, giving your answer in SI base units.

Solution:

- First, you will have to notice that the time and the displacement are not in SI base units, therefore you will have to convert the units before performing the calculation.

$$s = 8.00 \text{ km}$$

$$k = 10^3$$

$$\text{therefore, in SI base units, } s = 8.00 \times 10^3 \text{ m}$$

$$t = 10.0 \text{ minutes}$$

$$1 \text{ minute} = 60 \text{ seconds}$$

$$\text{therefore, in SI base units, } t = (10.0 \times 60) = 600 \text{ s}$$

- Now all the quantities used in the calculation are in SI units and the calculation can be performed.

$$v = \frac{s}{t}$$

$$v = \frac{8 \times 10^3}{600}$$

$$v = 13.333... = 13.3 \text{ ms}^{-1} \text{ (3 s.f.)}$$

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Part D: Practice Questions

1. Select the SI base unit for mass from the following options:
 - A. cd
 - B. kg
 - C. K
 - D. M

2. State the SI units for the following physical quantities:
 - a) Mass
 - b) Thermodynamic temperature
 - c) Length
 - d) Amount of substance

3. The National Grid supplies electricity to our homes.
The cables used to transmit electricity lose around 188 kW of power.
Convert the power loss into watts (W).

4. A cylindrical canister is used in a physics investigation into the properties of gases.
The physicist needs to calculate the volume of the cylinder to carry out the experiment.
 - The radius of the cylinder's circular face is 10 cm and it has height 20 cm.
 - The volume for a cylinder is given by the equation $V = \pi r^2 h$.Calculate the volume of the cylinder in cubic metres.

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SKILL B2: USE AND CALCULATE QUANTITIES IN DIFFERENT FORMS

Part A: Specification Overview

The exam board will expect you to be able to identify and work with expressions in standard form.

You will be tested on your ability to use, calculate and present physical quantities in standard form.

This knowledge and skill will be tested throughout each of the topics for the exam.

Part B: Theoretical Overview

Decimal Form:

A decimal is a fraction written in an alternative form. It can be identified by the presence of a decimal point.

An example of a decimal form would be:

$$3.4$$

where the 3 is in the units column and the 4 is in the 10th column. It can be identified as '3 and 4 10^{ths}'.

Standard Form:

The number N can be said to be in standard form if it is written in the following form:

$$N = S \times 10^x.$$

S represents a number no smaller than 1, and less than 10, and x , if positive, represents the number of times the number N has been multiplied by 10 and, if negative, how many times it has been divided by 10.

Standard form is used as a more convenient way of representing numbers that are very large or very small.

For example:

- The number 147,000,000,000 could be written more conveniently in its standard form as 1.47×10^{11} .
- The number 0.00000000236 could be written more conveniently in its standard form as 2.36×10^{-9} .

You will be expected to recognise and convert numbers into these two forms for calculations.

To convert to standard form:

1. Identify the first non-zero digit of your number and place a decimal point after it.
e.g. 70,000
7.
2. Then determine how many times your first digit has been multiplied by 10 to get the original number.
e.g. $7 \times 10 \times 10 \times 10 \times 10 = 70\,000$
Therefore, 7 has been multiplied by 10 four times.

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- To write it in standard form, you take the number of times your digit
- by 10 and multiply your digit by 10 to the power of this:

e.g. 7×10^4

The same method works for a decimal.

To convert a decimal to standard form:

1. Identify the first non-zero digit of your decimal and place a decimal at that position (if you include any non-zero terms after it also).

e.g. 0.0045

4.5

2. Then determine how many times our first non-zero digit has been divided by 10 to get the original number:

$$4.5 \div 10 \div 10 \div 10 = 0.0045$$

Therefore, 4.5 has been divided by 10 three times.

- To write the decimal in standard form, you take the number of times 10 and multiply your digit by 10 to the power of this number.

In this case, however, we include a minus to indicate we have divided like before.

e.g. 4.5×10^{-3}

Part C: Worked Example

- The mass of Earth is $M = 5\,972\,000\,000\,000\,000\,000\,000\,\text{kg}$ and
 $r = 6.37 \times 10^6\,\text{km}$.

The gravitational constant G is given by $G = 6.67 \times 10^{-11} \text{ Nm}^2 \text{ kg}^{-2}$.

The equation for the gravitational potential is $E_{\text{grav}} = -\frac{GM}{r}$

- Write Earth's mass, M , in standard form.
- Calculate the gravitational potential at Earth's surface, ensuring standard form, including your answer.

Solution:

- [illegible]

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b) $E_{\text{grav}} = -\frac{GM}{r}$

$$E_{\text{grav}} = -\frac{(6.67 \times 10^{-11}) \times (5.97 \times 10^{24})}{(6.37 \times 10^6)}$$

$$E_{\text{grav}} = -62511616.95 \text{ J}$$

$$6.25 \times 10 \times 10 \times 10 \times 10 \times 10 \times 10 \times 10$$

6.25 has been multiplied by 10 seven times

$$E_{\text{grav}} \approx -6.25 \times 10^7 \text{ J}$$

Part D: Practice Questions

- Give the following numbers in standard form:
 - 2,570,000
 - 0.00236
 - 369
 - 0.0581
- Convert the following numbers out of standard form to a decimal number:
 - 4.78×10^7
 - 1.2×10^{-3}
 - 7.63×10^4
 - 6.33×10^{-14}
- The kinetic energy of an object is determined by the following equation:

$$E_k = \frac{1}{2}mv^2$$

A $8.30 \times 10^3 \text{ kg}$ lorry travels with velocity of 11.0 ms^{-1} .

- Give the mass of the lorry as a whole number.
- Calculate the kinetic energy of the lorry travelling at 11.0 ms^{-1} , give your answer in standard form.

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SKILL B3: ESTIMATION

Part A: Specification Overview

This Physics course will require making appropriate estimates of physical quantities within your calculations. Additionally, your estimation skills will be further tested in exam questions when you will be expected to estimate the effects of varying experimental conditions.

This skill is tested throughout the course.

Part B: Theoretical Overview

In the course you might not always be provided with the numerical value required for a calculation. The exam board, in this case, would then expect you to demonstrate your understanding of the course by making appropriate estimates of quantities.

The exam board won't expect you to be able to estimate a physical quantity from first principles.

Estimates of typical quantities are in the table below:

Quantity	Estimate
Mass of a car	1,000 kg
Mass of an adult	70–80 kg
Weight of an adult	700–800 N
Height of an adult	2 m
Speed of sound	300 ms ⁻¹
Pressure of the atmosphere	100,000 Pa
Density of water	1,000 kg m ⁻³
Speed on motorway	30–40 ms ⁻¹
Speed of plane	300 ms ⁻¹
Power of a car	60 kW
Power of a person	100 W
Distance to Sun	150,000,000 km
Distance to Moon	400,000 km
Mass of Earth	6×10^{24} kg
Radius of Earth	6,000 km

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Part C: Worked Example

1. The equation for gravitational potential energy is:

$$E_{\text{grav}} = mgh$$

where m is the mass of the object, g is the acceleration due to gravity, and h is the height the object is lifted through.

The gravitational potential energy is defined as the energy stored by an object when it is lifted through a height h .

A diver is standing at the end of a 5 m diving board. The acceleration due to gravity is $g = 9.81 \text{ ms}^{-1}$.

- Estimate the mass of an average adult
- Based on a), estimate the gravitational potential energy E_{grav}
- Predict what would happen to your answer to (b) if the diver was on a 10 m board instead.

Solution:

- 70–80 kg
 - $E_{\text{grav}} = mgh$
 $E_{\text{grav}} = (70 - 80) \times 9.81 \times 5$
 $E_{\text{grav}} = 3000 - 4000 \text{ J}$
 - Since $E_{\text{grav}} \propto h$, if h doubles then we can estimate that E_{grav} will double.

Part D: Practice Questions

- A car is travelling for 10,000 seconds at an average speed on a motorway. The equation to determine the distance travelled by the car is $d = s \times t$. Estimate how far the car has travelled in 10,000 seconds.
- Two planes are travelling with average speed to their respective destinations. Plane 1 travels for 10,800 seconds and Plane 2 travels for 14,400 seconds. Estimate the difference between the distances travelled by Plane 1 and Plane 2.

Note: $d = s \times t$

3. The gravitational potential at a distance r from a planetary object is:

$$E_{\text{grav}} = -\frac{GM}{r}$$

where M is the mass of the planetary object, r is the distance from its centre, and G is a gravitational constant $6.67 \times 10^{-11} \text{ Nm}^2/\text{kg}^2$.

Estimate the gravitational potential at Earth's surface (the distance r is the distance from the centre of Earth to its surface).

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SKILL B4: SIGNIFICANT FIGURES

Part A: Specification Overview

The specification states that you should be able to use an appropriate number of significant figures when presenting numbers or measured values.

Specifically, they want to see you demonstrating ability to:

- present calculations to an appropriate number of significant figures given the numbers of significant figures
- demonstrate that calculated quantities can only be presented to the limit of the least accurate measured value

Part B: Theoretical Overview

Significant figures are used to round numbers. When calculating quantities, you should provide a detailed value for a quantity, and sometimes an approximation. In some cases you will need to use your knowledge of significant figures.

The significant figure of a value is best demonstrated with an example:

23,569	1 st significant figure = 2 2 nd significant figure = 3 3 rd significant figure = 5 and so on
76.5	1 st significant figure = 7 2 nd significant figure = 6 3 rd significant figure = 5
801	1 st significant figure = 8 2 nd significant figure = 0 3 rd significant figure = 1
0.0040	1 st significant figure = 4 2 nd significant figure = 0

You should start to see the pattern, and also realise that the most significant figure is the first non-zero term. If a zero appears in the value between numbers then it counts as part of its value as a placeholder. A zero at the end of a value is also significant.

If you are told to provide a measured quantity to x significant figures you should follow the following steps:

1. Identify your x^{th} significant figure.
2. Round up if the number after the x^{th} significant figure is 5 or above, or round down if the number after the significant figure is 4 or below.
3. Then set all the numbers that follow the significant figure before a decimal point to zero, and any trailing decimal figures after the last significant figure.

For example, if you were given $F = 38.37654 \text{ N}$, you might not need to know the exact accurate degree and might be asked to round it to 3 significant figures:

1. The 3rd significant figure is 3.
2. The number after the significant figure is 7; therefore, you will need to round up.
3. The number to 3 significant figures will then be 38.4 N (since the zero after the decimal point should not write 38.40000 N).

Note: When rounding a measured value to significant figures you cannot give a more accurate measured value than the values you are given to calculate it. More specifically, the number of significant figures given in an answer should be the same as the number of significant figures in any value used in the calculation.

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Part C: Worked Example

- Write 50,214,235.3256 to 4 significant figures.
- A group of engineers are attempting to fix the cables on a suspension bridge. If the bridge is stable and safe they need to determine the stress acting on the cables.

The equation for stress is: $\sigma = \frac{F}{A}$

where σ represents stress, F represents the force exerted on the object and A represents the cross-sectional area of the object.

The group of engineers know that the force acting on one cable is 85,369.234 N and the cross-sectional area of the cable is 0.690 m².

- Calculate the stress felt by one cable.
- Explain why the answer cannot be presented as $\sigma = 123723.5275$ N/m².
- Write your answer to (a) to 3 significant figures.

Solution:

- 50,210,000
- $$\sigma = \frac{F}{A}$$

$$\sigma = \frac{85369.234}{0.690}$$

$$\sigma = 123723.5275$$

$$\sigma = 123723.53 \text{ Pa or N/m}^2$$
 - Since the calculated result σ cannot be more accurate than the measurements used in the calculation, the answer can only be given to 3 significant figures.
 - 124,000

Part D: Practice Questions

- Choose the number below which is 345,700 written to 2 significant figures.
 - 340,000
 - 34
 - 350,000
 - 345,700
- Give the following numbers to 3 significant figures:
 - 30,501
 - 567,843.22
 - 0.0023695
- A sound engineer checking the electrical supply to a speaker system measures the current in the cables to be 1.60 A and a potential difference of 2.63 V across them. From these measurements the engineer calculates the resistance to be 1.64375 Ω . What is wrong with this calculation?
- The Space Shuttle requires an enormous resultant force of 10,500,000 N to launch. The shuttle has a mass of 2,220,000 kg.

Determine the acceleration $\left(a = \frac{F}{m}\right)$ of the shuttle as it launches into space.

Write your value to an appropriate number of significant figures.

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SKILL B5: MEAN VALUE

Part A: Specification Overview

You will need to be able to calculate the mean of experimental values obtained from repeated measurements.

This skill can be tested within any of the course's topics.

Part B: Theoretical Overview

The mean value represents the average of the range of measurements.

It is good experimental practice to take repeated measurements of a value to obtain an accurate measurement of the value by reducing the contribution of errors. A single value (or an average value) would then be required if the measured value was to be used in other physical quantities involved in the experiment.

Let's say you had N measurements. The equation for calculating the mean is:

$$\text{mean} = \frac{x_1 + x_2 + x_3 + \dots + x_N}{N}$$

where $x_1, x_2, x_3, \dots, x_N$ are the N measurements

Part C: Worked Example

A Year 11 physics pupil is carrying out an experiment on various electrical components and measures the resistance of a resistor. The student repeats the measurement 10 times.

Resistance (Ω)						
r_1	r_2	r_3	r_4	r_5	r_6	r_7
2.43	2.24	2.41	2.36	2.33	2.27	2.42

Calculate the mean value for resistance of the pupil's measured values.

Solution:

N = the number of measured values = 10

$$\text{mean} = \frac{r_1 + r_2 + r_3 + r_4 + r_5 + r_6 + r_7 + r_8 + r_9 + r_{10}}{N}$$

$$\text{mean} = \frac{2.43 + 2.24 + 2.41 + 2.36 + 2.33 + 2.27 + 2.42 + 2.56 + 2.32 + 2.29}{10}$$

$$\text{mean} = \frac{23.63}{10}$$

$$\text{mean} = 2.363$$

$$\text{mean} = 2.36$$

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Part D: Practice Questions

1. A physicist obtains the following measured values for the temperature in kelvin:

T_1	T_2	T_3	
77.0	76.0	75.0	7

- a) Explain how the physicist could determine the average value obtained.
 b) Calculate the mean value for the temperature of liquid nitrogen.
2. The transport department released statistics on the speed of cars outside five different cars is given below:

Car 1	Car 2	Car 3	Car 4
30.0 mph	40.0 mph	20.0 mph	22.0 mph

Calculate the mean value for the speed from this sample.

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SKILL B6: USE CALCULATOR TO HANDLE SIN, COS AND TAN

Part A: Specification Overview

The exam board expect you, throughout the course, to be able to use your trigonometric functions ($\sin x$, $\cos x$ and $\tan x$). You will be tested on your ability to use these functions when expressed in both degrees and radians.

Using your calculator to handle the trigonometric functions will be assessed in the context of mechanics, such as with vectors and projectile motion, but expect it to also appear at various points throughout the course.

Part B: Theoretical Overview

When working with calculations involving trigonometric functions always ensure you are aware of whether the question is asking you to work in degrees or radians. Ensure you set your calculator accordingly before continuing with the calculation.

Part C: Worked Example

1. During an investigation into the critical angles of different materials, it was found that the critical angle of Material 1 was 39.9° .

The equation relating the critical angle and the refractive index of a material is given by:

$$\sin C = \frac{1}{n}$$

where C is the critical angle and n is the refractive index of the material.

- a) Use this equation to determine the refractive index n of Material 1.

The refractive index of Material 2 was known to be 1.33.

- b) Calculate the critical angle of Material 2.

Solution:

a) $\sin C = \frac{1}{n}$

$$\sin 39.9 = \frac{1}{n}$$

$$n = \frac{1}{\sin 39.9}$$

To evaluate n , follow the next steps using the buttons on your calculator:

1 \div \sin 39.9 $=$

Following those steps will display an answer of 1.56 on your calculator.

Therefore,

$$n = 1.56$$

Note: Make sure your calculator is set to degrees

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b) $\sin C = \frac{1}{n}$
 $\sin C = \frac{1}{1.33}$
 $\sin C = 0.7518\dots$
 $C = \sin^{-1}(0.7518\dots)$

To evaluate C , proceed with the following steps, using the buttons on



Note: The last answer is stored in the Ans memory.

Following those steps will display the answer 48.7534... on your calculator.

Therefore,

$$C = 48.8^\circ \text{ (3 s.f.)}$$

Part D: Practice Questions

- State the solutions to the following equations. Assume that each equation is in degrees.
 - $\sin 0.56$
 - $\cos 78$
 - $\tan 14$

- Determine x in the following equations. Assume that each equation is in degrees.
 - $\tan x = 0.300$
 - $\cos x = 0.290$
 - $\sin x = 0.830$

- The displacement of an object displaying simple harmonic motion can be written as

$$x = A \cos(\omega t)$$

where x is the displacement, A is amplitude, ω is angular frequency of oscillation.

A bungee jumper will undergo simple harmonic motion during their oscillation.

The angular frequency of the jumper is 1.30 rad s^{-1} and the amplitude is 10 m .

Calculate the displacement of the jumper after 30 seconds.

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SKILL B7: USE CALCULATOR TO WORK WITH POW

Part A: Specification Overview

You will be expected to determine and use power functions during calculation. This skill will be tested in various topics throughout this course; however, in kinetic energy problems, as well as elastic potential energy problems.

Part B: Theoretical Overview

A power function is any function written in the following form:

$$y = x^n$$

where n is any real constant and y and x are two variables.

For example, the following function can be defined as a power function:

$$y = x^5$$

The above function can be read as ' y is equal to x to the power of 5'.

It is simple to determine the value of the variable y if you are given the value of x .

For example, if $x = 4$, then

$$y = x^5$$

$$y = (4)^5$$

$$y = 4 \times 4 \times 4 \times 4 \times 4$$

$$y = 1024$$

Alternatively, you can also determine the variable x if you are given the value of y . However, this proves to be a little harder as you will have to invert the power function.

For example if $y = 32$, then

$$y = x^5$$

$$32 = x^5$$

$$x = \sqrt[5]{32}$$

$$x = 2$$

The second last line can be read as, ' $The 5^{th}$ root of 32'.

To find the 5th root you are essentially looking for a number that has been raised to the power of 5 to equal 32. The calculation can be done two ways:

- Using the root button on your calculator to enter the equation
- From recall of your knowledge of roots

The last method will only be applicable to easy roots such as $\sqrt{16}$. This calculation is for the square root of 16, which essentially means you are looking for a number that equals 16 when squared.

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Part C: Worked Example

1. The equation relating x and y is given by $x = y^3 + 1$

Calculate the value of x when $y = 4$

2. Halley's comet is in orbit round the Sun. The comet reaches its maximum speed when it is closest to the Sun. The maximum speed of Halley's comet is approximately $3.68 \times 10^4 \text{ m s}^{-1}$. The mass of Halley's comet is approximately $2.20 \times 10^{14} \text{ kg}$.

The equation for kinetic energy of a moving object is given by:

$$E_k = \frac{1}{2}mv^2$$

where m is the mass of the object and v is the speed of the object.

- a) Calculate the kinetic energy (E_k) of Halley's comet when it is closest to the Sun.

The kinetic energy of another comet is calculated to be $E_k = 1.37 \times 10^{22} \text{ J}$. The mass of this comet is $1.30 \times 10^{14} \text{ kg}$

- b) Show by calculation whether this comet has a lower or greater speed than Halley's comet when it is closest to the Sun in its orbit.

Solution:

1. $x = y^3 + 1$
 $x = (4)^3 + 1$

To evaluate x , proceed with the following steps using the buttons on the calculator:

4 x^{\square} 3 $+$ 1

Following the steps above will display an answer of 65 in your calculator.

Therefore,
 $x = 65$

2. a) $E_k = \frac{1}{2} \times (2.20 \times 10^{14}) \times (3.68 \times 10^4)^2$
 $E_k = 1.49 \times 10^{23} \text{ J}$

- b) $E_k = \frac{1}{2}mv^2$

$$1.37 \times 10^{22} = \frac{1}{2} \times (1.30 \times 10^{14}) \times v^2$$

$$v = \sqrt{\frac{1.37 \times 10^{22}}{\frac{1}{2} \times 1.30 \times 10^{14}}}$$

$$v = 1.45 \times 10^4 \text{ m s}^{-1}$$

The velocity is less than the velocity of Halley's comet.

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Part D: Practice Questions

1. The equation relating a and b is given by $a = b^2$.

If $b = 3$, calculate the value for a .

2. When a spring is stretched from its rest position it holds elastic potential energy.

The equation for calculate elastic potential energy is:

$$E = \frac{1}{2} kx^2$$

Calculate the elastic potential energy (E) of a spring with a spring constant (k) of 120 N m⁻¹ when it is stretched (x) by 0.020 m.

3. A group of Year 11 physicists were conducting experiments into the effect of resistance on power. The group measured the potential difference (V) across a 10.0 Ω resistor.

The equation for calculating the power is given by:

$$P = \frac{V^2}{R}$$

where P is the power, V is the potential difference and R is the resistance.

Calculate the power dissipated by the resistor.

4. A car accelerates (a) at 2.8 ms⁻² and covers a distance (s) of 15.8 m. Calculate the final velocity (v) of the car if it starts at a velocity (u) of 2.3 ms⁻¹. Calculate the final velocity (v) of the car using the equation $v^2 = u^2 + 2as$.

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SKILL B8: CHANGING THE SUBJECT OF THE

Part A: Specification Overview

Your ability to change the subject of a formula is essential for success in the

The skill is continually assessed throughout each and every topic. A component of the exam is to change the subject of a formula to find your speed and accuracy in answering questions.

The exam board require you to be able to change the subject of a formula to find quantities in the formula.

Part B: Theoretical Overview

To change the subject of the formula you will use inverse operations to make the quantity you are trying to find the subject.

An example would be the equation for a straight line:

$$y = mx + c$$

You may already know a point (x, y) and the gradient m of the line, and the y-intercept c .

In its current form, the equation is not useful as a means to determine the value of c . It needs to be rearranged so c is the subject:

1. Initially you would want to bring all the variables that aren't c to one side using inverse operations.

In this case it would mean taking away the term mx :

$$y - mx = c$$

2. If the unknown variable is still not the subject of the formula, further operations need to be carried out to remove it from the other variables.

In our case, c is the subject of the formula and we have now done everything we need to do.

$$c = y - mx$$

The equation can now be used as a tool to determine the value for the y-intercept c .

Note: If the unknown variable is still not the subject of the formula, further operations need to be carried out to get it by itself.

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Part C: Worked Example

Particle accelerators are used by hospitals in radiotherapy treatment to accelerate particles between charged plates that increase their speed.

The equation relating the work done on the particle and the kinetic energy is given below:

$$eV = \frac{1}{2}mv^2$$

where e is the charge of the particle, V is the potential of the charged plates, m is the mass of the particle and v is the final speed of the particle.

To ensure accelerators are operating correctly, a medical physicist wants to determine the final speed of the particles.

Rearrange the formula so that it is in a more appropriate form to determine the final speed of the particle.

Solution:

We would need to make v the subject of the formula:

- To make v the subject, we need to move all other variables to one side of the equation.
 - v is initially divided by 2, and therefore to move 2 to the other side we need to perform the inverse operation to multiply each side by 2

$$2eV = mv^2$$

- v is multiplied by m , and therefore to move m to the other side we need to perform the inverse operation of dividing each side of the equation by m

$$\frac{2eV}{m} = v^2$$

- All the other variables are now on one side, but v is still not by itself; we need to perform a further inverse operation:

- v is squared in its current form, and therefore to get v by itself we need to perform the inverse operation of taking the square root of both sides

$$v = \sqrt{\frac{2eV}{m}}$$

Now v is the subject of the formula and the formula is now in a form that can be used to determine the final speed of the particles.

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Part D: Practice Questions

1. Choose which of the equations below shows the equation $tx = 2 + p$ rearranged so that the subject is x :

- A. $x = (2 + p)t$
- B. $x = 2 + p - t$
- C. $x = 2 + \frac{p}{t}$
- D. $x = \frac{(2 + p)}{t}$

2. Given the following equation:

$$P = I^2 R$$

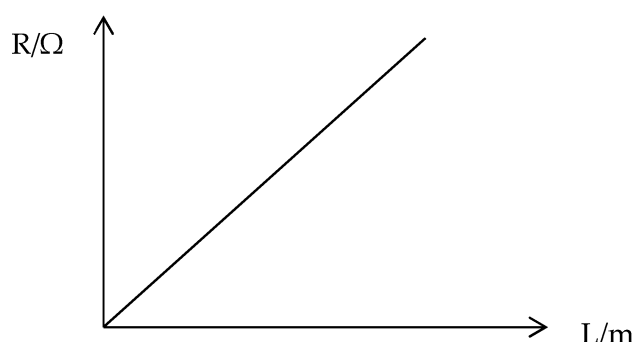
where P is power, I is current and R is resistance,
rearrange the formula so that I is the subject.

3. The equation for the resistivity of a metal ρ is usually given in the form

$$R = \frac{\rho L}{A}$$

where R is resistance, ρ is resistivity, L is length and A is the cross-sectional area.

- a) Rearrange the equation to make the resistivity ρ of a material the subject.



The resistive properties of a material were investigated in a laboratory.

Physicists used the graph to determine that the gradient (m) of the line was

- b) Rearrange the equation for the gradient to solve for ρ .

4. The equation for determining the intensity of radiation from a point source is

$$I = \frac{P}{4\pi r^2}$$

where P is power, and r is distance from point source.

A physicist wants to determine how far away (r) the star she is studying is.

Rearrange the equation so it is in a more convenient form to calculate r .

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SKILL B9: SOLVING ALGEBRAIC EQUATIONS, INCLUDING

Part A: Specification Overview

Solving algebraic equations forms the basis to solving all calculations in the course. It is required to substitute values for variables into algebraic equations and solve for the unknown.

The skill is assessed in every topic of the course specification.

Part B: Theoretical Overview

The method for solving algebraic equations is simple. It will require you to rearrange the equation by changing the subject of the formulas.

An algebraic equation simply refers to any equation where one or more variables are unknown.

To solve the algebraic equation:

1. Change the subject of the equation to the variable you are trying to find.

This will require you to use inverse operations.

Note: If the variable you want to find is already the subject then you do not need to rearrange the equation.

2. Secondly, insert in the values for variables you have and work through the equation to find the unknown.

Part C: Worked Example

1. The mass of Earth is $M_E = 5.98 \times 10^{24} \text{ kg}$ and the mass of a geostationary satellite is $M_S = 250 \text{ kg}$.

The orbital radius of a geostationary satellite is roughly $42,157 \text{ km}$ and the gravitational constant G is $6.67 \times 10^{-11} \text{ Nm}^2\text{kg}^{-2}$.

The equation for gravitational potential energy for the system is:

$$E_{\text{grav}} = -G \frac{M_1 M_2}{r},$$

where M_1 is the mass of object 1, M_2 is the mass of object 2, G is the gravitational constant and r is the distance between the objects.

Calculate the gravitational potential energy for the system (E_{grav}) of the Earth and the satellite.

Solution:

1. We do not need to rearrange the formula as E_{grav} is already the subject of the equation.
2. Insert in the numerical values for the variables into the equation and solve for the unknown.

$$E_{\text{grav}} = -G \frac{M_E M_S}{r}$$

$$E_{\text{grav}} = -(6.67 \times 10^{-11}) \times \left(\frac{(5.98 \times 10^{24}) \times (250)}{(42157 \times 10^3)} \right)$$

$$E_{\text{grav}} = -(6.67 \times 10^{-11}) \times (3.546267524 \times 10^{19})$$

$$E_{\text{grav}} = -2\,365\,360\,438 \text{ J} = -2.37 \times 10^9 \text{ J}$$

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Part C: Worked Example

2. A runner in a relay race starts to increase their speed before they receive the baton. They do not start running from standing still. When the baton is passed to them, they accelerate at 0.24 ms^{-2} over 100 m, and cross the finish line with a speed of 8 ms^{-1} .

The equation $v^2 = u^2 + 2as$ relates the runner's final velocity, v , initial velocity, u , and distance travelled, s .

Calculate the speed the runner was travelling at when they received the baton.

Solution:

1. To make u the subject of the equation, we need to rearrange it using it. Starting with $v^2 = u^2 + 2as$, we can subtract $2as$ to isolate u^2 :

$$u^2 = v^2 - 2as$$

Because we have u^2 but need u , we have to take the square root of both sides:

$$u = \sqrt{v^2 - 2as}$$

2. Insert in the numerical values from the question to find u :

$$u = \sqrt{8^2 - 2 \times 0.24 \times 100}$$

$$u = \sqrt{64 - 48}$$

$$u = \sqrt{16}$$

$$u = 4 \text{ ms}^{-1}$$

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Part D: Practice Questions

1. The equation for potential difference is $V = IR$, where I is current and R is resistance.
Calculate the potential difference across a $10\ \Omega$ resistor with a current of 2.5 A .

2. An equation for current flowing in a conductor is given by $I = Anev$, where A is the area of the conductor, n is the number density of copper atoms, e is the charge of an electron and v is the drift velocity of the electrons.

An electrician detects 1.20 A of current flowing in a copper wire with a cross-sectional area of $2.34 \times 10^{-7}\text{ m}^2$. The number density of copper atoms is $8.50 \times 10^{28}\text{ m}^{-3}$.

Calculate the drift velocity of electrons through the copper wire.

3. Newton's second law is $F = m\left(\frac{v-u}{t}\right)$, where F is the net force acting on an object, v is its final velocity, u is its initial velocity and t is the time for which the force is acting.

A $7.1 \times 10^7\text{ kg}$ train leaves the platform at a velocity of 0.44 ms^{-1} . The net force that is applied for 360 seconds.

Calculate the velocity of the train after 360 seconds.

4. The centripetal force is the force that causes an object to travel in a circular path. At a corner the centripetal force is supplied by the frictional force between the tires and the road.

The equation for centripetal force is $F = \frac{mv^2}{r}$, where m is the mass of the object and r is the radius of its circular path.

The centripetal force is 50 N , the mass of the car is 670 kg and the radius of the corner is 10 m .

Determine the speed at which the car would have been travelling as it enters the corner.

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SKILL B10: ABSOLUTE UNCERTAINTY

Part A: Specification Overview

As a Physics student you will have to be able to recognise uncertainties in measurements and use techniques to determine an uncertainty when data is added, subtracted or raised to powers.

Part B: Theoretical Overview

An uncertainty is a value that is associated with a measurement to illustrate how much a measurement can realistically fall within when the experiment errors are taken into account. It gives an indication of the range of values in which the true value lies.

For example, the measurement 2.5 ± 0.1 N indicates that the true values will lie between 2.4 N ($2.5 - 0.1$) and 2.6 N ($2.5 + 0.1$).

Let's say you have measured two parameters a, b and have determined their absolute uncertainties Δa and Δb respectively from the equipment you used to measure them:

$$a \pm \Delta a; b \pm \Delta b$$

Uncertainties can also be represented as a percentage uncertainty ϵ_a and ϵ_b :

$$a \pm \epsilon_a; b \pm \epsilon_b$$

You will learn more about the percentage uncertainty in the following skill.

You may then be asked to calculate further quantities involving these two quantities. When doing so, you not only have to take into consideration the two variables but also their absolute uncertainties and percentage uncertainties.

The following rules illustrate how to combine uncertainties when different operations are performed on the variables:

Two variables added together: $(a \pm \Delta a) + (b \pm \Delta b)$

Two variables subtracted from one another: $(a \pm \Delta a) - (b \pm \Delta b)$

Two variables multiplied together: $(a \pm \epsilon_a) \times (b \pm \epsilon_b)$

Two variables divided by one another: $(a \pm \epsilon_a) \div (b \pm \epsilon_b)$

A variable raised to the power of n : $(a \pm \epsilon_a)^n = (a^n \pm n a^{n-1} \epsilon_a)$

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Part C: Worked Example

1. The equation relating a , b and c is as follows: $a = b + c$. The values $b = 30.5 \pm 0.2 \text{ N}$ and $c = 5.3 \pm 0.1 \text{ N}$.

Calculate the value of a , including its absolute uncertainty.

2. A pupil wants to know the length of wire used in a circuit; he measures and obtains the following measurements:

$$l_1 = 13 \pm 1 \text{ cm}; l_2 = 12 \pm 1 \text{ cm}$$

Determine the total length of the wire.

3. A medical physicist wants to know the combined volume of the two lungs. The medical physicist measures the volume of the right lung to be $V_r = 6100 \pm 100 \text{ cm}^3$ and the volume of the left lung to be $V_l = 5950 \pm 250 \text{ cm}^3$.

Determine the combined volume of both lungs.

Solution:

1. $a = (b \pm \Delta b) + (c \pm \Delta c)$
 $a = (b + c) \pm (\Delta b + \Delta c)$

In this case, you can simply use the absolute uncertainties when combining b and c since they both have the same units.

$$\begin{aligned} a &= (30.5 \pm 0.2) + (5.3 \pm 0.1) \\ a &= (30.5 + 5.3) \pm (0.2 + 0.1) \\ a &= 35.8 \pm 0.3 \text{ N} \end{aligned}$$

2. a) $l = l_1 + l_2$
 $l = (13 \pm 1) + (12 \pm 1)$
 $l = (13 + 12) \pm (1 + 1)$
 $l = 25 \pm 2 \text{ cm}$

In this case, you can simply use the absolute uncertainties when combining l_1 and l_2 since they both have the same units.

3. $V = (V_r \pm \Delta V_r) + (V_l \pm \Delta V_l)$
 $V = (V_r + V_l) \pm (\Delta V_r + \Delta V_l)$
 $V = (6100 + 5950) \pm (100 + 250)$
 $V = 12050 \pm 350 \text{ cm}^3$

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Part D: Practice Questions

1. State the absolute uncertainties of the following measurements:

- a) $4.55 \pm 0.05 \text{ A}$
- b) $16.2 \pm 0.1 \text{ ms}^{-1}$
- c) $3626 \pm 4 \text{ J}$

2. The equation for total potential difference across a circuit is given by

A student measures the potential difference across a resistor to be V_1 :
difference across a bulb to be $V_2 = 230 \pm 0.1 \text{ V}$.

Calculate the total potential difference across the circuit using the equation
account the absolute uncertainties.

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SKILL B11: PERCENTAGE UNCERTAINTY AND PERCENTAGE CHANGE

Part A: Specification Overview

The exam board will expect you to be able to work with percentage uncertainty and absolute uncertainty.

Part B: Theoretical Overview

Percentage Uncertainty

A percentage uncertainty is simply an alternative way of illustrating the uncertainty in a measurement. A percentage uncertainty displays the absolute uncertainty of a measured value as a percentage of the measured value.

The equation for determining the percentage uncertainty of a measured value is:

$$\text{percentage uncertainty} = \frac{\text{absolute uncertainty}}{\text{measured value}} \times 100\%$$

In other words,

$$\% \text{ uncertainty in } A = \frac{\Delta A}{A} \times 100\%$$

Conversely, you can also determine the absolute uncertainty of a measured value if you know the percentage uncertainty:

$$\text{absolute uncertainty} = \frac{\text{percentage uncertainty}}{100\%} \times \text{measured value}$$

In other words,

$$\Delta A = \frac{\% \text{ uncertainty in } A}{100\%} \times A$$

The percentage uncertainty is important when combining uncertainties. If the uncertainties are in different units, e.g. joules and watts, you cannot combine them directly, but you can combine their percentage uncertainties.

For example, if you were asked to determine the value for power P given voltage V and current I , you would combine the uncertainties of I and V to find the uncertainty in P .

However, in this case I and V do not share the same units, so you will have to convert the uncertainties to percentage uncertainties, using the combination rule (see previous skills) for combining percentage uncertainties.

Percentage Change

The percentage change is different to the percentage uncertainty; it represents the change in a measured value between an original measurement and a repeated measurement to indicate the decrease or increase in measurements as a percentage.

The equation for determining the percentage change between two measurements is:

$$\text{percentage change} = \frac{|\text{new value} - \text{original value}|}{\text{original value}} \times 100\%$$

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Note: The modulus sign ($| |$) on the top of the fraction simply takes into account the sign of the difference, ensuring you are dealing with a negative if there has been a decrease (new value < original value).

The modulus sign ensures you take the absolute value of the difference, and the top of the fraction will always be positive.

Part C: Worked Example

- The mass of an object is measured to be 0.30 ± 0.05 kg, using a set of scales. Calculate the percentage uncertainty of this measurement.
- A Year 11 student is carrying out an experiment to investigate the motion of a trolley down a frictionless ramp. The student calculates the final velocity of the trolley at the bottom of the ramp, to be $v = 2.4 \pm 0.1$ ms⁻¹. The student increases the steepness of the ramp and calculates the final velocity again, this time obtaining $v = 2.8 \pm 0.1$ ms⁻¹.
 - Calculate the percentage uncertainty of the student's initial measurement.
 - Calculate the percentage change in the measurements of final velocity.

Solution:

$$1. \quad \text{percentage uncertainty} = \frac{0.05}{0.3} \times 100\%$$

$$\text{percentage uncertainty} = 16.7\%$$

$$2. \quad \text{a) } \text{percentage uncertainty} = \frac{0.1}{2.4} \times 100\%$$

$$\text{percentage uncertainty} = 4.2\%$$

$$\text{b) } \text{percentage change} = \frac{|2.8 - 2.4|}{2.4} \times 100\%$$

$$\text{percentage change} = 16.7\%$$

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Part D: Practice Questions

1. Calculate the percentage uncertainty of 2.6 ± 0.2 .
2. Calculate the percentage change between the two values, with the new value 4.6.
3. The frequency of an oscillating pendulum was measured in an investigation due to gravity (g). The value for frequency obtained was 5.2 ± 0.05 Hz.
 - a) Calculate the percentage uncertainty of this measurement.

The length of the pendulum was altered and the experiment repeated. The frequency was now measured as 6.4 Hz after this alteration.

- b) Calculate the percentage change in the frequency.
4. Power in a circuit can be determined by the equation $P = IV$. During an investigation, a technician measured the current, I , to be 0.21 ± 0.05 A and the potential difference across the electrical component in the circuit to be 5.6 ± 0.1 V.

Calculate the power in the electrical component.

5. A tennis ball is measured to travel at an average speed of $v = 157 \pm 1$ m/s. The mass of the tennis ball is given by $m = 0.059 \pm 0.001$ kg. The kinetic energy of an object is $E_k = \frac{1}{2}mv^2$, where m is the mass of the object.

Calculate the kinetic energy of the tennis ball.

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SKILL B12: ANGLES

Part A: Specification Overview

The exam board will expect you to be able to use angles in 2D and 3D structures in physical problems.

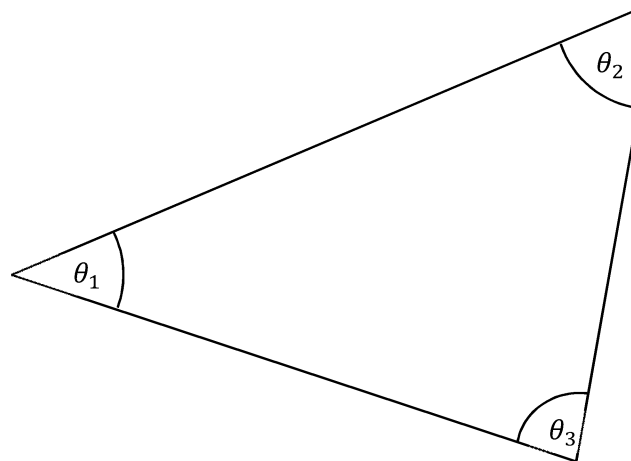
You will be required to make use of this skill throughout the course but this skill is only tested when working with force diagrams and vector resolution questions.

Part B: Theoretical Overview

To interpret and understand physical problems and applications, you will need a knowledge of angle rules within circles and triangles.

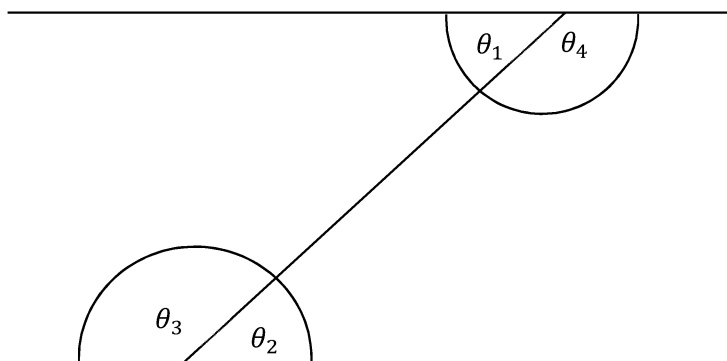
Knowledge of the following angle rules is essential when analysing physics problems:

- The angles inside a triangle



$$\theta_1 + \theta_2 + \theta_3 = 180^\circ$$

- Angles in relation to parallel lines
 - the alternate angles are equal



$$\theta_1 = \theta_2$$

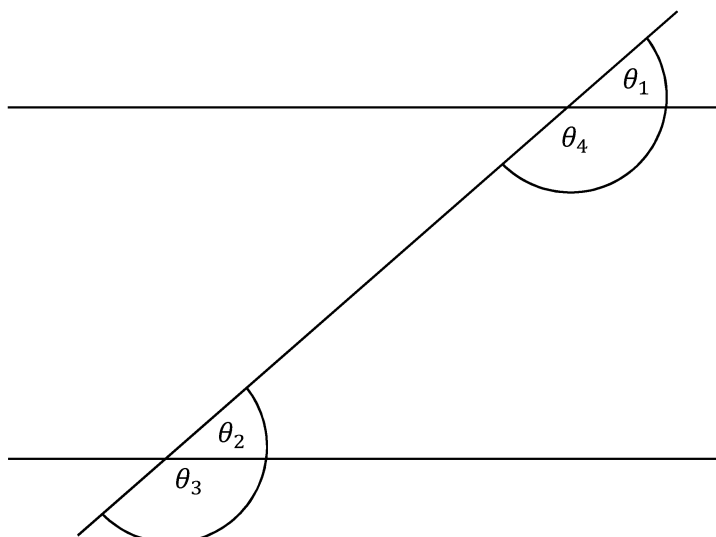
$$\theta_3 = \theta_4$$

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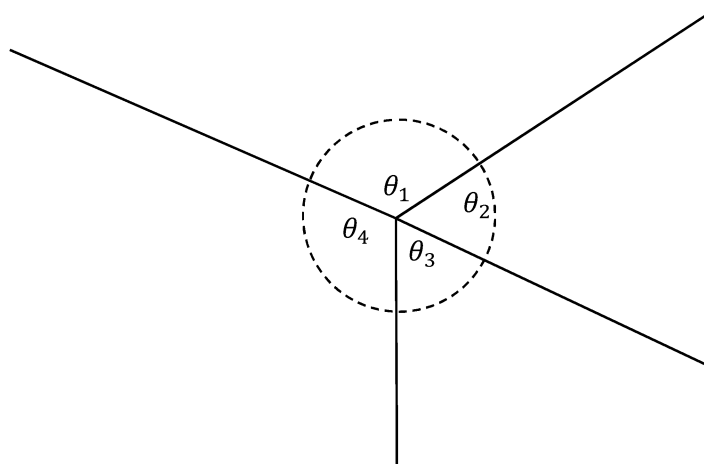
- the corresponding angles are equal



$$\theta_1 = \theta_2$$

$$\theta_3 = \theta_4$$

- All angles that meet at a point must add up to 360°



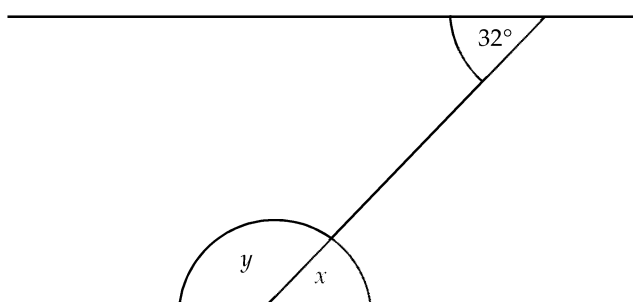
$$\theta_1 + \theta_2 + \theta_3 + \theta_4 = 360^\circ$$

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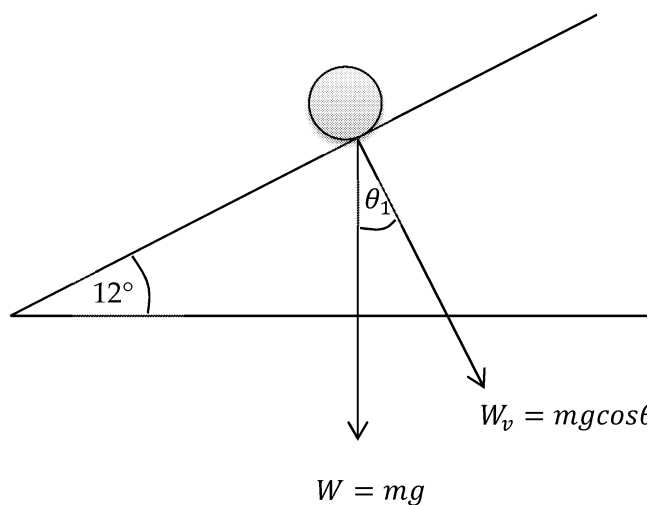


Part C: Worked Example:

1. Calculate the missing angles x and y .



2. A ball is rolling down an inclined plane as demonstrated below:

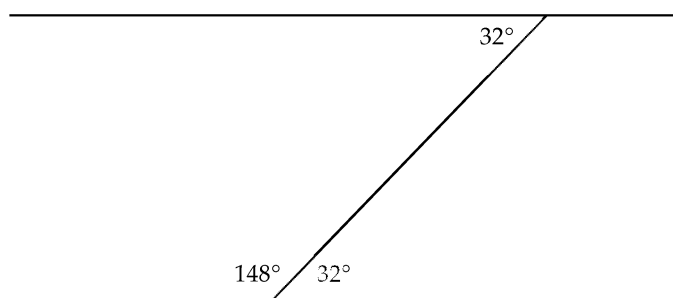


In order to calculate the component of weight perpendicular to the plane, the angle θ_1 has to be evaluated.

- a) Calculate the value of θ_1 using your knowledge of angles on parallel lines.
- b) Write the expression for W_v in terms of θ_1 found in (a).

Solution:

- 1.



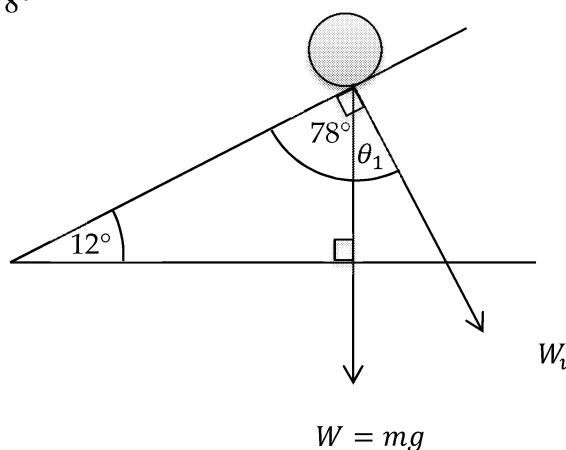
- The rule of alternate angles on parallel lines mean that $x = 32^\circ$
- Since x and y are on a parallel line they have to add to 180° . Therefore $y = 180 - x = 180 - 32 = 148^\circ$

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2. a) The angles of a triangle add up to 180° .

Therefore, the remaining angle of the triangle created by W and t is $180^\circ - (12^\circ + 90^\circ) = 78^\circ$



Then, since W_v is perpendicular to the slope of the inclined plane, the angle between W_v and the slope is 90° .

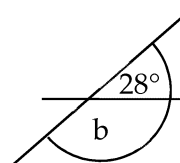
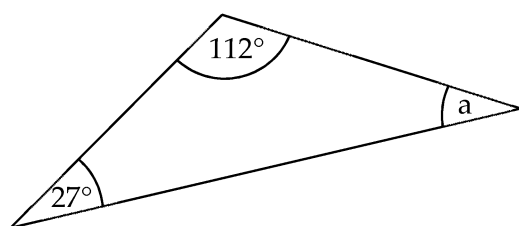
Therefore, θ_1 can be found from,

$$\theta_1 = 90 - 78 = 12^\circ$$

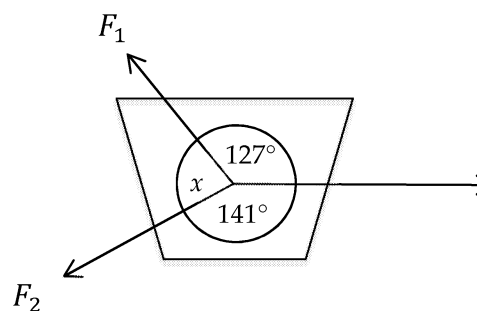
- b) $W_v = mg \cos \theta_1$
 $W_v = mg \cos 12^\circ$

Part D: Practice Questions

1. Determine the missing angles.



2. The following force diagram represents the forces acting on a boat.



Calculate the angle between F_1 and F_2 .

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SKILL B13: CONVERTING BETWEEN RADIANS AND DEGREES

Part A: Specification Overview

The specification states that as a physics student you should be comfortable with degrees and radians and be able to convert from one form to the other.

You will be expected to be able to demonstrate this skill in vector resolution and wave topics. This skill will also be tested in electromagnetic waves and refraction topics.

Part B: Theoretical Overview

Degrees and radians are simply two different units used to describe an angle. You should be comfortable with degrees as the unit of angles in a circle, but radians are simpler to use in calculations. The value of π radians is the same as the value of 180° .

It is similar to measuring the length of a variable; we can measure in miles or metres. Let's say you have an angle in degrees and you want to convert it into radians. Use the following equation to do so:

$$\text{radians} = \text{degrees} \times \frac{\pi}{180}$$

In a similar fashion, if you had your angle in radians and wanted to convert it into degrees, you would use the following equation:

$$\text{degrees} = \text{radians} \times \frac{180}{\pi}$$

Note: When dealing with angles greater than 360° or 2π , just divide the angle by 360° or 2π and take the remainder as your new angle to keep it within the standard range.

Part C: Worked Example

A light ray hits the window of a car and refracts as it travels from air to glass.

The angle of refraction is measured to be 67° .

a) Calculate the angle of refraction in radians.

Another light ray hits the car window, and this time the angle of incidence is measured to be 0.64 radians.

b) Calculate the angle of incidence in degrees.

Solution:

a) $\text{angle in radians} = 67 \times \frac{\pi}{180}$
 $1.169... = 1.2 \text{ radians (2 s.f.)}$

b) $\text{angle in degrees} = 0.64 \times \frac{180}{\pi}$
 $= 36.67^\circ$
 $= 37^\circ$

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Part D: Practice Questions

1. Choose the angle below which is equal to 32° :
 - A. 1833 radians
 - B. 0.56 radians
 - C. 5760 radians
 - D. 0.17 radians

2. Convert the following angles into radians:
 - a) 45°
 - b) 126°
 - c) 542°

3. Convert the following angles into degrees:
 - a) 5.6 radians
 - b) 1.22 radians
 - c) 0.23 radians

4. When light travels across the boundary of two materials it will change direction. The critical angle, given by $\sin C = \frac{1}{n}$, is the specific incident angle at which light travels from refraction to total internal reflection, changing direction and reflecting back into the same medium.
 The refractive index (n) is 1.52.
 Calculate the critical angle in degrees.

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SKILL B14: VISUALISING AND REPRESENTING STRUCTURE

CALCULATING AREAS AND VOLUME

Part A: Specification Overview

The exam board states that a requirement for this course is an ability to calculate the areas of triangles, circumferences and areas of circles, and the surface areas of rectangles, cylinders and spheres. Additionally, you will be expected to know how to calculate the volumes of cylinders and spheres.

This skill will be crucial when working on physical problems. The skill will be used in determining physical properties of the problem. You will see this skill tested in topics such as pressure, and resistivity topics.

Part B: Theoretical Overview

Area

This course will require you to calculate the following areas using the following formulas:

Circle:

- The circumference of a circle is given by:

$$C = \pi \times d$$

or

$$C = \pi \times (2 \times r)$$

where r is the radius and d is diameter

- The area of a circle is given by:

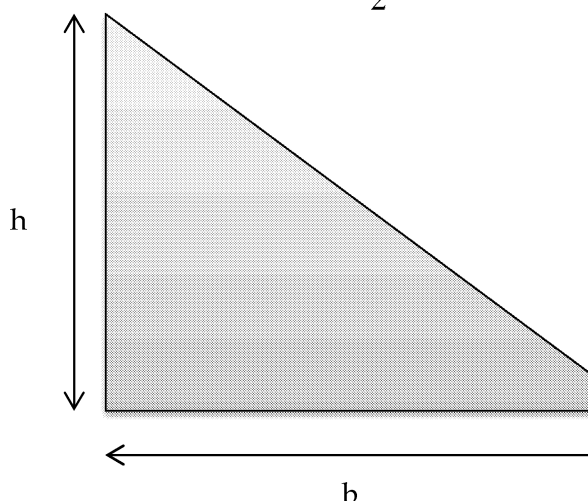
$$A = \pi r^2$$

or

$$A = \pi \left(\frac{d}{2} \right)^2$$

Triangle:

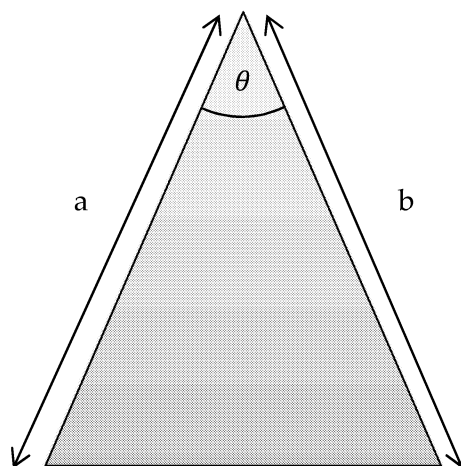
- The area of a right-angled triangle is given by: $A = \frac{1}{2} \times b \times h$



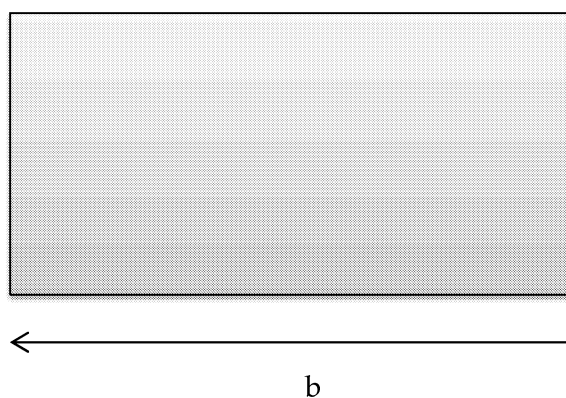
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The area of a non-right-angled triangle is given by: $A = \frac{1}{2}ab \sin \theta$



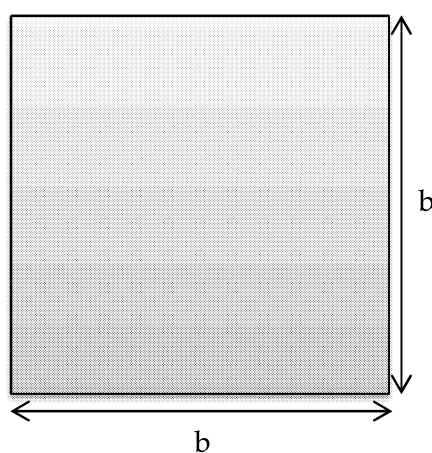
Square/Rectangle:



The area of a rectangle is given by:

$$A = b \times w$$

The special case for this is the case of the square when $b = w$



The area is then given by:

$$A = b \times b$$

$$A = b^2$$

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Surface Area:

The surface area of a 3D shape is the sum of all the areas on the outer face flat, while some are curved for shapes such as cylinders and spheres.

Note: The equation for surface area depends on the shape; for a cylinder, the surface area will include the equation for the area of a circle, whereas area of a rectangular block will include the equation for the area of differ

Volume:

The general equation for the volume of any prism is given by:

$$V = A \times h$$

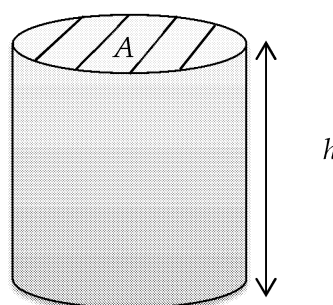
where A is the surface area of one of the sides of the shape and h is the height

Cylinder

If we apply the general volume equation to the cylinder we obtain:

$$V = A \times h$$

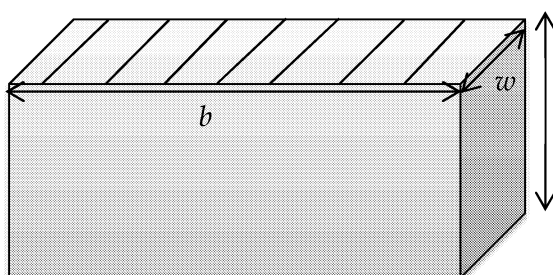
$$V = (\pi r^2) \times h$$



Rectangular block

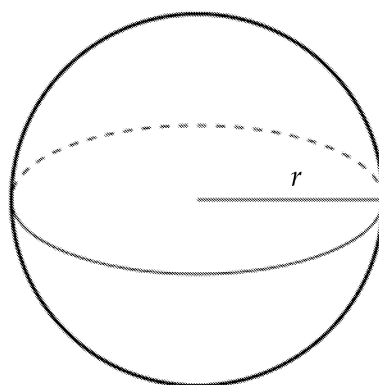
$$V = A \times h$$

$$V = (b \times w) \times h$$



Sphere

$$V = \frac{4}{3} \pi r^3$$



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Part C: Worked Example

1. Calculate the cross-sectional area of a cylinder with radius $r = 1.6$ m
2. An energy company is wanting to determine the resistivity of the wires used in its machines.

The resistivity of a wire can be determined using the following equation:

$$\rho = \frac{RA}{L}$$

where ρ is the resistivity of the material, R is the resistance of the wire, A is the cross-sectional area and L is the length of the material.

The wires used are cylindrical in shape, with a radius of 2.0 mm and a length of 100 m. If the resistance of the wires is known to be 0.01Ω , calculate the resistivity of the material.

Solution:

1. Cross-sectional area = area of a circle:

$$A = \pi r^2$$

$$A = \pi \times (1.6)^2$$

$$A = 8.0424... = 8.0 \text{ m}^2 \text{ (2 s.f.)}$$

2. $\rho = \frac{RA}{L}$

$$\rho = \frac{0.01 \times A}{(100 \times 10^{-2})}$$

Therefore, before the equation can be used to determine ρ , the cross-sectional area A must first be evaluated.

The cross-sectional area of a cylindrical object is a circle. Therefore:

$$A = \pi r^2$$

$$A = \pi \times (2 \times 10^{-3})^2$$

$$A = 1.2566 \times 10^{-5} \text{ m}^2$$

Therefore, the resistivity of the wire is:

$$\rho = \frac{0.01 \times (1.2566 \times 10^{-5})}{(100 \times 10^{-2})}$$

$$\rho = 1.3 \times 10^{-7} \Omega \text{m}$$

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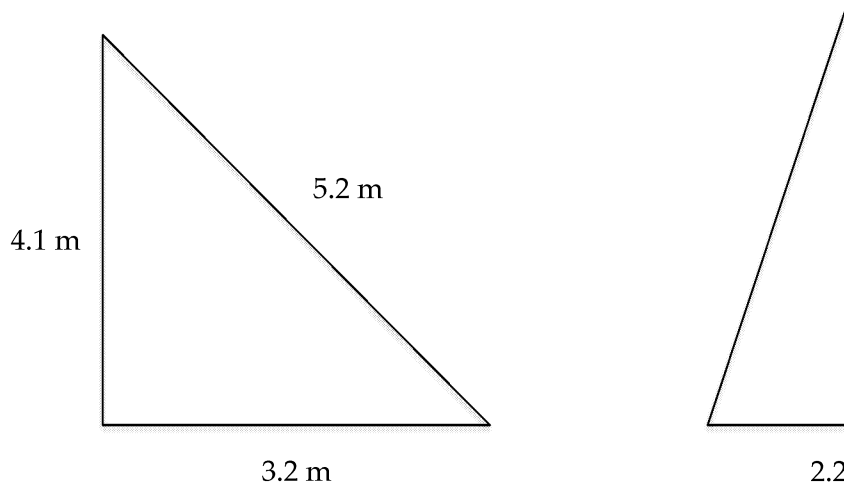


Part D: Practice Questions

1. A cylindrical barrel is being used in an experiment that investigates the effect of the volume of the barrel on the rate of diffusion. To carry out the experiment, the volume of the barrel needs to be known and a length of 0.63 m.
 - a) Calculate the volume of the barrel.
 - b) Calculate the circumference of the barrel.

The experiment is repeated with a rectangular trunk with dimensions 1.2 m by 0.8 m by 0.5 m.

- c) Calculate the area of one of its faces.
 - d) Calculate the volume of the trunk.
2. Determine the area of the following two triangles:



3. A rectangular box, used for recording animal sounds in the sea, is floating in seawater. The rectangular box has the dimensions 0.300 m \times 0.500 m \times 0.600 m. The equation for determining the buoyancy force (B) acting on the box is

$$B = \rho Vg$$

where V is the volume of the displaced fluid (in this case seawater), g is the gravitational field strength, and $\rho = 1020 \text{ kg m}^{-3}$ is the density of the seawater. Using the equation, calculate the buoyancy force acting on the box, using $g = 9.8 \text{ N kg}^{-1}$.

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SKILL B15: MATHEMATICAL SYMBOLS

Part A: Specification Overview

The exam board will expect you to understand and use the symbols: $=$, $<$, and \approx . You will be tested on your ability to recognise the significance of these symbols in mathematical expressions and work with the expressions to find numerical solutions.

This skill will be tested in every topic in this course; therefore, a grasp of this skill is essential.

Part B: Theoretical Overview

You will be expected to know what the following symbols mean and add to the context of mathematical expressions.

Symbol	Meaning	Context
$=$	Equal to	$x = 3$
$<$	Less than	$5 < 7$
\ll	Much less than	$1 \ll 10,000$
\gg	Much greater than	$785 \gg 0.02$
$>$	Greater than	Velocity 1 $>$ Velocity 2
\propto	Proportional	Force \propto acceleration
\approx	Approximately equal	$1.234 \approx 1.233$
Δ	Change in	ΔT

Part C: Worked Example

It can be said that during a collision or impact the net force exerted is given by $F = \frac{\Delta p}{\Delta t}$, where p is momentum and t is the time of the impact of collision.

Using your knowledge of mathematical symbols, indicate what effect a larger net force will have during impact.

Solution:

The equation $F \propto \frac{\Delta p}{\Delta t}$ reads 'Net force is proportional to the change in momentum divided by change in time'. Therefore, it can be said that if there is a greater net force, there will be a proportionally greater change in momentum divided by change in time.

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Part D: Practice Questions

1. State if each of the following statements is true or false:
 - A. $a \ll D$; 'D is much greater than a'
 - B. $F \approx m$; 'F is approximately equal to m'
 - C. $x > 7$; '7 is greater than x '
 - D. $a = \Delta v$; 'a is approximately equal to the change in v '
2. Write down the following statements in terms of their mathematical symbols:
 - a) Pressure is proportional to force
 - b) V_1 is much less than V_2
 - c) B is greater than C

3. Researchers at CERN are carrying out experiments with subatomic particles and use quantum mechanics to explain their properties.

A key concept underpinning quantum mechanics is that, for a photon, the energy E of a photon and f is the frequency of the photon.

Explain what is meant by this statement.

Deduce what you think might happen to f if E was increased, based on the statement above.

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SKILL B16: UNDERSTANDING SIMPLE PRO

Part A: Specification Overview

The exam board expects students to be able to recall their knowledge of basic GCSE Mathematics course and apply it to the context of physics.

In particular, students will be expected to understand the concepts of probability and radioactive decay of nuclei in radioactive sources.

Part B: Theoretical Overview

The probability of an event is said to range from impossible to certain, or 0 to 1 respectively.

The equation for determining the probability of a repeated **fair event** is

$$\text{probability of an event} = \left(\frac{\text{number of ways this particular outcome can occur}}{\text{total number of outcomes}} \right)^N$$

where N is the number of times the event is repeated.

Note:

The probability of an event lies in between 0 and 1 (0% probability to 100% probability).

The probability will only ever be 1 (100%) if the outcome of the event can be predicted with absolute certainty.

This can be visualised easily using a probability scale:

(Impossible)
0

An event can also be described as being spontaneous.

An event is **spontaneous** if:

- the existence of other outcomes does not affect the outcome
- the existence of external factors does not affect the outcome

An event can also be described as being random.

An event is **random** if:

- the outcome of an event cannot be predicted

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Independent, mutually exclusive and dependent events

Independent Events

Two events are **independent** if the outcome of one event has no effect on

For example, if you flip a coin and then flip it again, the outcome of the first flip has no effect on the outcome of the second flip; you will have the same chance of getting a head on the second flip as you did on the first flip.

The probability of the outcome of an event X can be written as $P(X)$.

The combined probability of **multiple independent events** occurring can

If X and Y are both **independent events** then the probability of event X and

$$P(X \text{ and } Y) = P(X) \times P(Y)$$

Mutually Exclusive Events

Two events are **mutually exclusive** if it is **impossible** for them to both happen.

The combined probability of **multiple mutually exclusive events** occurring is as follows:

If X and Y are **mutually exclusive** then the probability of event X OR event

$$P(X \text{ or } Y) = P(X) + P(Y)$$

A tree diagram can be used as a method to determine how to combine the probabilities of **independent** and **mutually exclusive** outcomes, as discussed above.

Take our coin flip example.

The rules for tree diagrams is that you:

- add vertically across the branches (mutually exclusive outcomes)

Note: This is what we had before, the probability that X or Y will occur is $P(X \text{ or } Y) = P(X) + P(Y)$

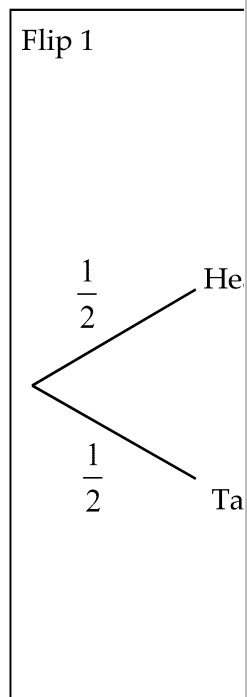
e.g. $P(\text{Head, Flip 1 or Tail, Flip 1})$

$$= P(\text{Head, Flip 1}) + P(\text{Tail, Flip 1}) = \frac{1}{2} + \frac{1}{2} = 1$$

- multiply horizontally across the branches (independent outcomes)

Note: This is what we had before, the probability that X and Y will occur is $P(X \text{ and } Y) = P(X) \times P(Y)$

e.g. $P(\text{Head, Flip 1 and Head, Flip 2}) = P(\text{Head, Flip 1}) \times P(\text{Head, Flip 2})$



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For example:

Q1. What is the probability of flipping the coin once and the outcome being heads and then flipping the coin a second time and the outcome being tails?

A1: $P(H \text{ and } T) = \left(\frac{1}{2} \times \frac{1}{2}\right) = \frac{1}{4}$

Q2. What is the probability of flipping the coin twice and getting opposite outcomes?

A2: It is important to remember that there could be two cases for this as there are two possible outcomes (heads or tails) you get first and second, just that the outcomes are opposite.

Therefore:

- You flip first to get heads **and** then flip again to get tails

OR

- You flip first to get tails **and** then flip again to get heads

So you could flip either a head or a tail first and get a tail and a head respectively. Both options would satisfy the condition stated in the question

$$P(H \text{ and } T) \text{ OR } P(T \text{ and } H) = (P(H) \times P(T)) + (P(T) \times P(H))$$

$$P(H \text{ and } T) \text{ OR } P(T \text{ and } H) = \left(\frac{1}{2} \times \frac{1}{2}\right) + \left(\frac{1}{2} \times \frac{1}{2}\right) = \frac{1}{2}$$

Dependent Events

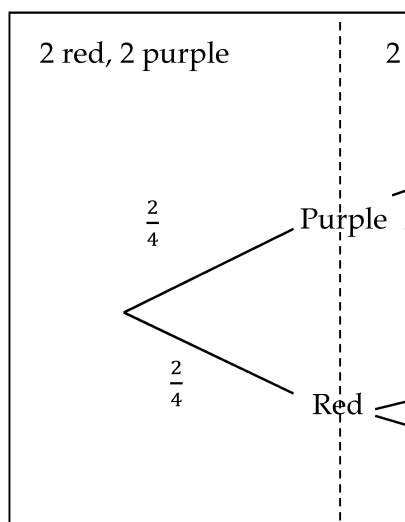
If an event is **dependent** then it means that the outcome of one event is affected by the outcome of another.

For example:

Let's say you had 4 sweets in a bag, 2 red and 2 purple. If you picked one sweet out of the bag, the colour of the second sweet you pick will be dependent on or affected by the colour of the first sweet you pick.

This is because before picking any sweets you had 2 red and 2 purple. However, after picking one sweet out of the bag, depending on whether it was red or purple you will have 1 red and 1 purple left respectively. The selection you have when picking the second sweet is different from the selection you have when picking the first sweet. The outcome of the second pick will therefore depend on what colour of sweet you choose first.

It is a lot easier to visualise this with a tree diagram. The same rules apply for tree diagrams of dependent outcomes. The only difference will be that the selection of your second outcome will be different to your first.



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Part C: Worked Example

1. If you flip a coin to get a head and then flip the coin again, what is the probability of getting another head?
2. There are 2 blue marbles and 3 green marbles in a bag.

Determine the probability of a blue marble being picked and then a green marble.

The blue marble is not placed back in the bag after it is picked out.

3. A Year 12 physics student used a set of dice to mimic the radioactive decay process. She used 168 square dice with six faces to represent the decay process.

She rolls the dice and removes any dice that land with the number 1 or 2. She then rolls the remaining dice again and repeats this process a number of times.

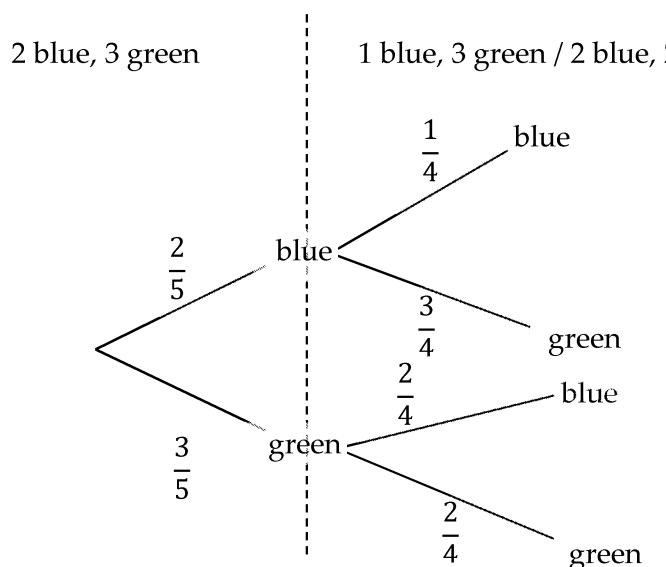
- a) State what the remaining dice and throws represent in reference to the radioactive decay process.
- b) Explain why this experiment is a useful model for representing radioactive decay.
- c) By indicating how many dice would remain after n throws, explain how this experiment proves that the number of undecayed nuclei will decay exponentially.

Solution:

1. These are independent events; therefore, the outcome of the first flip of the coin does not affect the outcome of the second flip, and therefore the probability of flipping a head in the second flip is the same as the first flip.

$$P(H) = \frac{1}{2}$$

- 2.



$$P(\text{blue and green}) = \frac{2}{5} \times \frac{3}{4}$$

$$P(\text{blue and green}) = \frac{6}{20} = \frac{3}{10}$$

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3. a) Dice = undecayed nuclei
Throw = fixed time interval
- b) • The student cannot predict when a dice will roll a 5 or which next, which mimics not being able to predict which nuclei will decay next in radioactive decay.
• Each dice has the same chance of rolling a 5 as any of the other dice, just as each undecayed nucleus has equal chance of decaying.
- c) On average, the number of dice removed (decayed) after the first throw is $\frac{1}{6}$ of the total number of dice.
Therefore, if 28 dice show a 5 on the first throw, the number of dice remaining is $28 \times \frac{5}{6} = 23\frac{1}{3}$ (remaining undecayed).
- The number of dice removed (decayed) after n throws will be approximately $28 \times \left(\frac{1}{6}\right)^n$.
- As the number of rolls (n) increases, the value of $\left(\frac{5}{6}\right)^n$ decreases, so the rate of decay slows over time, but there is never a point where it reaches zero.
This mirrors the behaviour of radioactive substances, where the number of undecayed nuclei decreases exponentially over time.

Part D: Practice Questions

- Explain what is meant by a random event.
- The sketch below is of the probability scale; label the missing numbers.



- A child is holding a paper bag which contains 6 blue sweets and 3 green sweets. The child picks a sweet at a time from the bag.
 - What is the probability that the child's first sweet is blue?
 - The child eats the blue sweet. What is the probability that the second sweet picked is green?
- An experiment investigating the radioactive decay process of nuclei was carried out using popcorn kernels.

A bag of unpopped kernels was placed in a microwave and allowed to heat for 1 minute.

 - State what the unpopped kernels represent in the comparison to radioactive decay.
 - Explain how the popcorn experiment mimics the radioactive decay process.
 - Sketch a graph of number of kernels against time, including on the graph the number of unpopped kernels and a line representing kernels that have popped.

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Skill B1: Units and conversion between units

1. B
2. a) kg
b) K
c) m
d) mol
3. $188 \text{ kW} = 188 \times 10^3 \text{ W} = 188\,000 \text{ W}$
4. since $1 \text{ m} = 10^2 \text{ cm}$
 $10 \text{ cm} = 0.1 \text{ m}$ and $200 \text{ cm} = 2 \text{ m}$
 $V = \pi r^2 h$
 $V = \pi \times 0.1^2 \times 2$
 $V = 0.06283... = 0.063 \text{ m}^2$ (2 s.f.)

Skill B2: Use and calculate quantities in different forms

1. a) 2.57×10^6
b) 2.36×10^{-3}
c) 3.69×10^2
d) 5.81×10^{-2}
2. a) 47,800,000
b) 0.0012
c) 76,300
d) 0.00000000000000633
3. a) 8,300 kg
b) $E_k = \frac{1}{2}mv^2$
 $E_k = \frac{1}{2}(8300) \times (11)^2$
 $E_k = 502150 \text{ J}$
 $E_k = 5.02 \times 10^5 \text{ J}$ (3 s.f.)

Skill B3: Estimation

1. $v \approx 30 \text{ ms}^{-1}$
 $d = v \times t$
 $d = 30 \times 10\,000$
 $d = 300\,000 \text{ m}$

2. $v \approx 300 \text{ ms}^{-1}$
Plane 1:
 $d = v \times t$
 $d = 300 \times 10\,800$
 $d = 3\,240\,000$
Plane 2:
 $d = v \times t$
 $d = 300 \times 14\,400$
 $d = 4\,320\,000$
difference = 4

3. $M \approx 6 \times 10^{24} \text{ kg}$
 $E_{\text{grav}} = -\frac{GM}{r}$
 $E_{\text{grav}} = -\frac{6.67 \times 10^{-11} \times 6 \times 10^{24}}{1.5 \times 10^7}$
 $E_{\text{grav}} = -6.67 \times 10^6 \text{ J}$
 $E_{\text{grav}} = -7 \times 10^6 \text{ J}$

Skill B4: Signifi

1. C
2. a) 30,500
b) 568,000
c) 0.00237
3. The calculate
the measured
Resistance sh
4. $a = \frac{F}{m}$
 $a = \frac{10\,500\,000}{2\,210\,000}$
 $a = 4.751131$
 $a = 4.75 \text{ ms}^{-2}$

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Skill B5: Mean value

1. a) You would add up all the measured values for temperature and divide this by the number of measured values.

$$b) \text{ mean} = \frac{T_1 + T_2 + T_3 + T_4 + T_5}{N}$$

$$\text{mean} = \frac{77 + 76 + 75 + 78 + 77}{5}$$

$$\text{mean} = 76.6 \text{ K}$$

$$2. \text{ mean} = \frac{v_1 + v_2 + v_3 + v_4 + v_5}{N}$$

$$\text{mean} = \frac{30 + 40 + 20 + 22 + 25}{5}$$

$$\text{mean} = 27.4 \text{ mph}$$

Skill B6: Use calculator to handle sin, cos and tan

1. Determine the solutions to the following equations:
- 9.77×10^{-3}
 - 0.21
 - 0.25
2.
 - 16.7
 - 73.1
 - 56.1
3. $x = 10.3 \cos(1.3 \times 30)$
 $x = 2.7464... = 2.75 \text{ m (3 s.f.)}$

Skill B7: Use calculator to work with power functions

1. $a = b^2$
 $a = (3)^2$
 $a = 3 \times 3$
 $a = 9$
2. $E = \frac{1}{2} kx^2$
 $E = \frac{1}{2} \times (2.2 \times 10^4) \times (0.02)^2$
 $E = 4.4 \text{ J}$

$$3. P = \frac{V^2}{R}$$

$$P = \frac{(2.4)^2}{10.0}$$

$$P = 0.576$$

$$P = 0.58 \text{ W (2 s.f.)}$$

$$4. v^2 = u^2 + 2as$$

$$v^2 = (2.3)^2 + 2 \times 9.8 \times 2.0$$

$$v^2 = 93.77$$

$$v = \sqrt{93.77}$$

$$v = 9.683... = 9.68 \text{ m s}^{-1} \text{ (3 s.f.)}$$

Skill B8: Change formula

1. D
2. $P = I^2 R$
 $\frac{P}{R} = I^2$
 $\sqrt{\frac{P}{R}} = I$
 $I = \sqrt{\frac{P}{R}}$
3. a) $R = \frac{\rho L}{A}$
 $RA = \rho L$
 $\frac{RA}{L} = \rho$
 $\rho = \frac{RA}{L}$
- b) $m = \frac{\rho}{A}$
 $mA = \rho$
 $\rho = mA$

$$4. I = \frac{P}{4\pi r^2}$$

$$Ir^2 = \frac{P}{4\pi}$$

$$r^2 = \frac{P}{4\pi I}$$

$$r = \sqrt{\frac{P}{4\pi I}}$$

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Skill B9: Solving algebraic equations, including quadratics

$$\begin{aligned}
 1. \quad V &= IR \\
 V &= 0.2 \times 10 \\
 V &= 2 \text{ V} \\
 \\
 2. \quad I &= Anev \\
 \frac{I}{Ane} &= v \\
 v &= \frac{I}{Ane} \\
 v &= \frac{1.2}{(2.34 \times 10^{-7}) \times (8.5 \times 10^{28}) \times (1.6 \times 10^{-19})} \\
 v &= 3.77 \times 10^{-4} \text{ ms}^{-1}
 \end{aligned}$$

$$\begin{aligned}
 3. \quad F &= m \left(\frac{v-u}{t} \right) \\
 \frac{F}{m} &= \frac{v-u}{t} \\
 \left(\frac{F}{m} \right) t &= v-u \\
 \left(\frac{F}{m} \right) t + u &= v \\
 v &= u + \left(\frac{F}{m} \right) t \\
 v &= 0.44 + \left(\frac{1.5 \times 10^6}{7.1 \times 10^7} \right) 360 \\
 v &= 8.0456... = 8.0 \text{ ms}^{-1} \text{ (2 s.f.)}
 \end{aligned}$$

$$\begin{aligned}
 4. \quad F &= \frac{mv^2}{r} \\
 Fr &= mv^2 \\
 \frac{Fr}{m} &= v^2 \\
 v^2 &= \frac{Fr}{m} \\
 v &= \sqrt{\frac{Fr}{m}} \\
 v &= \sqrt{\frac{50 \times 13.0}{670}} \\
 v &= 1.0074...
 \end{aligned}$$

Skill B10: Absolute

$$\begin{aligned}
 1. \quad a) \quad &0.05 \text{ A} \\
 &b) \quad 0.1 \text{ ms}^{-1} \\
 &c) \quad 4 \text{ J} \\
 \\
 2. \quad V_T &= V_1 + V_2 \\
 V_T &= (1.2 \pm 0.1) + (2.1 \pm 0.2) \\
 V_T &= (1.2 + 2.1) \pm (0.1 + 0.2) \\
 V_T &= 3.3 \pm 0.3
 \end{aligned}$$

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Skill B11: Percentage uncertainty (including percentage difference)

1. $V_T = V_1 + V_2$

$$\text{percentage uncertainty} = \frac{0.2}{2.6} \times 100\%$$

$$\text{percentage uncertainty} = 7.7\%$$

2. $\text{percentage change} = \frac{|\text{new value} - \text{original value}|}{\text{original value}} \times 100\%$

$$\text{percentage change} = \frac{|3.9 - 4.6|}{4.6} \times 100\%$$

$$\text{percentage change} = \frac{0.7}{4.6} \times 100\%$$

$$\text{percentage change} = 15.217... = 15\% \text{ (2 s.f.)}$$

3. a) $\text{percentage uncertainty} = \frac{\text{absolute uncertainty}}{\text{measured value}} \times 100\%$

$$\text{percentage uncertainty} = \frac{0.05}{5.2} \times 100\%$$

$$\text{percentage uncertainty} = 0.9615... = 0.96\% \text{ (2 s.f.)}$$

b) $\text{percentage change} = \frac{|\text{new value} - \text{original value}|}{\text{original value}} \times 100\%$

$$\text{percentage change} = \frac{|6.4 - 5.2|}{5.2} \times 100\%$$

$$\text{percentage change} = 23.076... = 23\% \text{ (2 s.f.)}$$

4. $P = (I \pm \Delta I) \times (V \pm \Delta V)$

$$P = (IV) \pm (\Delta I + \Delta V)$$

$$\% \text{ uncertainty } I = \frac{\Delta I}{I} \times 100\% = \frac{0.05}{0.21} \times 100\% = 23.8\%$$

$$\% \text{ uncertainty } V = \frac{\Delta V}{V} \times 100\% = \frac{0.1}{5.6} \times 100\% = 1.8\%$$

$$\% P = (23.8 + 1.8) = 25.6\%$$

$$\% P = \frac{\Delta P}{P} \times 100\%$$

$$\Delta P = \frac{\% P}{100\%} \times P$$

$$\Delta P = \frac{25.6}{100} \times (5.6 \times 0.21)$$

$$\Delta P = 0.301 = 0.3$$

$$P = 0.21 \times 5.6 = 1.176 = 1.2$$

$$P = 1.2 \pm 0.3 \text{ W}$$

The rounding of the final values is due to the number of significant figures provided with.

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$$5. \quad E_k = \frac{1}{2}(m \pm \Delta m) \times (v \pm \Delta v)^2$$

$$E_k = \frac{1}{2}mv^2 \pm \Delta m + (2\Delta v)$$

$$E_k = \frac{1}{2} \times 0.059 \times 57^2 = 95.8455 \text{ J}$$

$$\% \text{ uncertainty in } m = \frac{\Delta m}{m} \times 100\% = \frac{0.001}{0.059} \times 100\% = 1.7\%$$

$$\% \text{ uncertainty in } v = \frac{\Delta v}{v} \times 100\% = \frac{1}{57} \times 100\% = 1.8\%$$

$$\% E_k = (\%m + 2 \times \%v) = 1.7 + (2 \times 1.8) = 5.2\%$$

$$\% E_k = \frac{\Delta E_k}{E_k} \times 100\%$$

$$\Delta E_k = \frac{\% E_k}{100\%} \times E_k = \frac{5.2}{100} \times 95.8455 = 4.9875$$

$$E_k = 95.8455 \pm 4.9875 \text{ J}$$

$$E_k = 96 \pm 5.0 \text{ J (2 s.f.)}$$

Skill B12: Angles

1. $a: 41^\circ$
 $b: 152^\circ$
 $x: 28^\circ$
 $y: 28^\circ$
 $z: 152^\circ$

2. $x = 360 - (127 + 141) = 92^\circ$

Skill B13: Converting between radians and degrees

1. B
2. a) 0.79 radians
b) 2.2 radians
c) 9.46 radians
3. a) 320°
b) 69.9°
c) 13°

4. $\sin C = \frac{1}{n}$
 $\sin C = \frac{1}{1.52}$
 $\sin C = 0.657...$
 $C = 41.1395... = 41.1^\circ \text{ (3 s.f.)}$

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Skill B14: Calculating areas and volumes

1. a) $V = \text{Area} \times h$

$$V = (\pi r^2) \times h$$

$$V = \pi \times \left(\frac{d}{2}\right)^2 \times h$$

$$V = \pi \times \left(\frac{0.36}{2}\right)^2 \times 0.63$$

$$V = 0.06412... = 0.064 \text{ m}^3 \text{ (2 s.f.)}$$

b) $C = \pi \times d$

$$C = \pi \times 0.36$$

$$C = 1.1 \text{ m}$$

c) $\text{Area of face} = 0.20 \times 0.30$

$$A = 0.06 \text{ m}^2$$

OR $\text{Area of face} = 0.20 \times 0.60$

$$A = 0.12 \text{ m}^2$$

OR $\text{Area of face} = 0.30 \times 0.60$

$$A = 0.18 \text{ m}^2$$

d) $V = b \times w \times h$

$$V = 0.20 \times 0.30 \times 0.60$$

$$V = 0.036 \text{ m}^3$$

$$V = 3.6 \times 10^{-2} \text{ m}^3$$

2. $\text{Area of right-angled triangle} :$

$$A = \frac{1}{2} \times l \times b$$

$$A = \frac{1}{2} \times 3.2 \times 4.1$$

$$A = 6.56 = 6.6 \text{ m}^2 \text{ (2 s.f.)}$$

$\text{Area of isosceles triangle} :$

$$A = 2 \times (\text{Area of right-angled triangle})$$

$$A = 2 \times \left(\frac{1}{2} \times l \times b\right)$$

$$A = 2 \times \left(\frac{1}{2} \times 1.1 \times 4.6\right)$$

$$A = 5.06 = 5.1 \text{ m}^2 \text{ (2 s.f.)}$$

3. $B = \rho V g$

$$B = 1020 \times (0.300 \times 0.500 \times 0.600) \times 9.81$$

$$B = 900.558 = 901 \text{ N (3 s.f.)}$$

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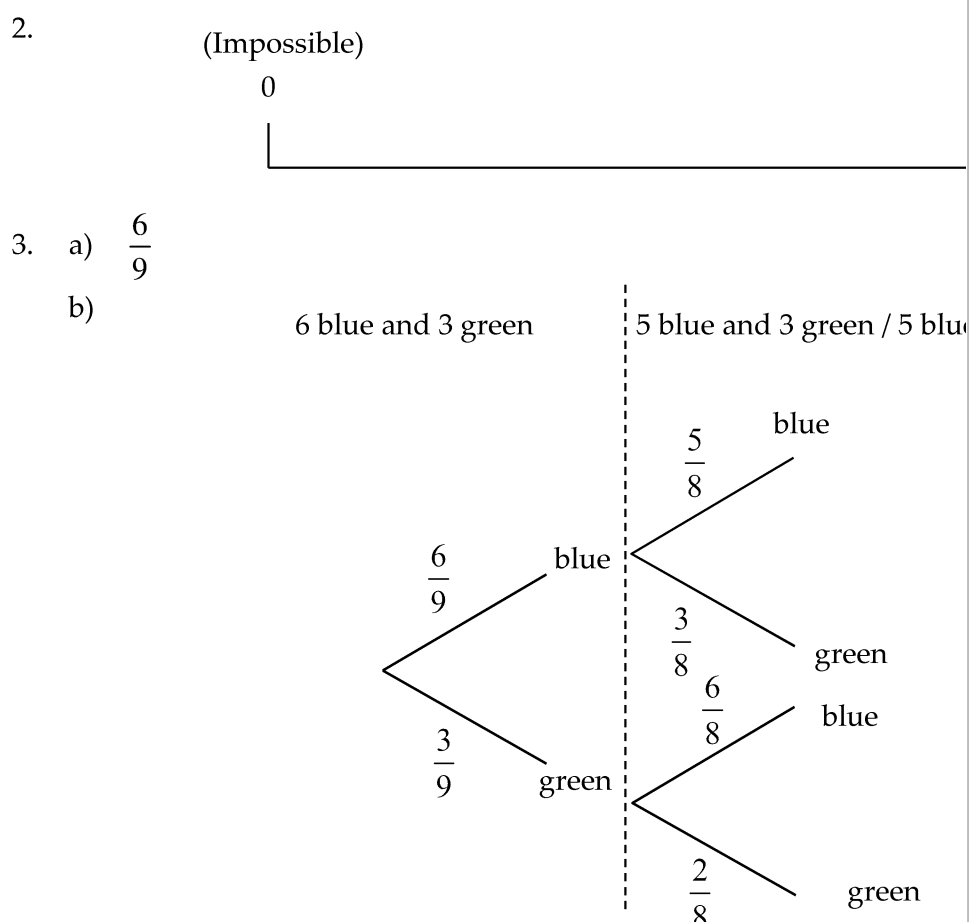


Skill B15: Mathematical symbols

- True
 - True
 - False
 - False
- $P \propto F$
 - $V_1 \ll V_2$
 - $B > C$
- The statement means that energy (E) is proportional to frequency (f)
This would therefore mean that if E was increased then f would increase

Skill B16: Understanding simple probability

- An event where:
 - the set of outcomes cannot be known
 - the order in which they occur cannot be known



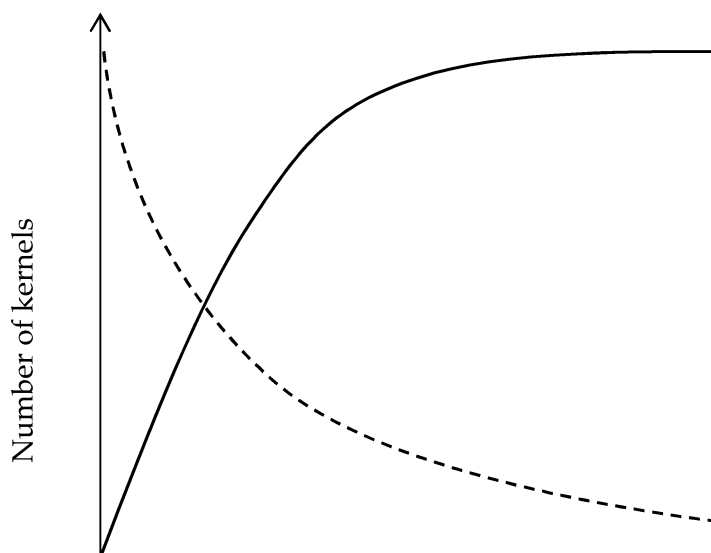
After the child has taken out the blue sweet and eaten it then there are 5 blue and 3 green sweets left (8 sweets)

$$P(\text{blue and green}) = P(\text{blue}) \times P(\text{green}) = \frac{6}{9} \times \frac{3}{8} = \frac{18}{72} = \frac{2}{8} = \frac{1}{4}$$

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4. a) Undecayed nuclei in a radioactive substance
- b) • When kernels begin to pop they represent a single decay. Which kernel (decay) cannot be predicted, and which kernel (nucleus) will be predicted; therefore, it represents a *random event*, mimicking the manner of decay.
- When and which kernel (nucleus) pops is not affected by the number of undecayed (nuclei), and every kernel (nucleus) has the same chance of popping. The event is a *spontaneous event*, mimicking the manner of decay.
- Initially there is a large number of unpopped kernels and then as time passes the number of unpopped kernels decreases, as does the number of unpopped kernels.



- c) Solid line indicates popped kernels and dashed line indicates unpopped kernels

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Diagnostic Test 1

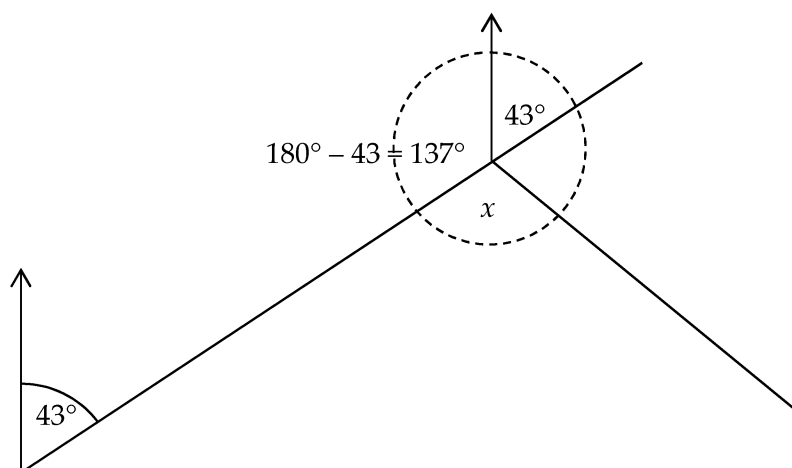
1. 4.58×10^6
2. 93 700
3. $151 \times \frac{\pi}{180} = 2.6354\dots = 2.64$ radians (3 s.f.)
4. $0.15 \times \frac{180}{\pi} = 8.5943\dots = 8.6^\circ$ (2.s.f)
5. a) $A = \pi r^2$
b) $A = \frac{1}{2}lb$
6. a) 402,400
b) 0.2049
7. a) kg
b) m
c) A
d) W
8. a) $x = \sin^{-1}(0.630) = 39.050\dots = 39.1^\circ$ (3 s.f.)
b) $x = 0.8480\dots = 0.85^\circ$ (2.s.f)
c) $x = -0.44522\dots = -0.445^\circ$ (3 s.f.)
9. a) 5.778×10^3 K
b) 5780 K
10. a) A is proportional to the change in B
b) C is equal to or less than D, and D is less than E
c) F is much greater than G, and G is equal to or greater than H
11. a) $x = 33 + 90 = 180$
 $x = 57^\circ$
b) $x + 57 + 63 = 180$
 $x = 180 - (57 + 63)$
 $x = 60^\circ$

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12.



Therefore,

$$x + 137 + 159 = 360$$

$$x = 360 - (137 + 159) = 64^\circ$$

13. $P = I^2 R$

$$P = 3.00^2 \times 14.0$$

$$P = 126 \text{ W}$$

14. a) 0.1 Hz

b) 0.01 m

c) $v = f \lambda$

$$v = (2.3 \times 0.02)$$

$$v = 0.05 \text{ ms}^{-1}$$

$$\frac{\Delta f}{f} = \frac{0.1}{2.3}$$

$$\frac{\Delta f}{f} = 0.09$$

$$\frac{\Delta \lambda}{\lambda} = \frac{0.01}{0.02}$$

$$\frac{\Delta \lambda}{\lambda} = 0.5$$

$$\frac{\Delta v}{v} = \frac{\Delta f}{f} + \frac{\Delta \lambda}{\lambda}$$

$$\frac{\Delta v}{v} = 0.09 + 0.5$$

$$\frac{\Delta v}{v} = 0.59$$

$$\Delta v = 0.59 \times v$$

$$\Delta v = 0.59 \times 0.05$$

$$\Delta v = \pm 0.03 \text{ ms}^{-1}$$

$$\therefore v = 0.05 \pm 0.03 \text{ ms}^{-1}$$

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$$15. \text{ percentage uncertainty} = \frac{\text{absolute uncertainty}}{\text{measured value}} \times 100\%$$

$$\text{percentage uncertainty} = \frac{0.2}{56.9} \times 100\%$$

$$\text{percentage uncertainty} = 0.3514... = 0.35\% \text{ (2.s.f.)}$$

$$16. \text{ percentage change} = \frac{|\text{new value} - \text{original value}|}{\text{original value}} \times 100\%$$

$$\text{percentage change} = \frac{|0.22 - 0.21|}{0.21} \times 100\%$$

$$\text{percentage change} = 4.761... = 4.8\% \text{ (2.s.f.)}$$

$$17. \theta = A \sin(xt)$$

$$\theta = 3.40 \times \sin(1.60 \times 1.70)$$

$$\theta = 3.40 \times \sin 2.72$$

$$\theta = 1.391... \text{ radians}$$

$$1.391... \times \frac{180}{\pi} = 79.717... = 79.7^\circ \text{ (3 s.f.)}$$

$$18. v^2 = u^2 + 2as$$

$$v^2 = 5.8^2 + 2 \times 0.8 \times 10$$

$$v^2 = 49.64$$

$$v = \sqrt{49.64}$$

$$v = 7.0455... = 7.0 \text{ ms}^{-1} \text{ (2 s.f.)}$$

$$19. \text{ mean} = \frac{828 \times 10^3 + 827 \times 10^3 + 824 \times 10^3 + 827 \times 10^3 + 826 \times 10^3 + 824 \times 10^3}{6}$$

$$\text{mean} = 826 \times 10^3 \text{ km h}^{-1}$$

20. Rolling dice can simulate radioactivity decay.

- If you start off with x dice, then each dice can represent a single nucleus and each throw represents an interval of time t .
- If you choose the number, say 3, as the number that represents a probability for decay is $\frac{1}{6}$ for each dice (nucleus); therefore, with x dice, $\frac{x}{6}$ will decay and $\frac{5x}{6}$ remain undecayed.
- Therefore, the number of decays will be determined by change in time, but you cannot know which dice will decay, only their probability of decay.
- This is the same model of the radioactive decay of x undecayed nuclei. The same model can be used to explain radioactive decay.

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21. a) joules

b) $E_k = \frac{1}{2}mv^2$

$$E_k = \frac{1}{2} \times (1.67 \times 10^{-27}) \times (2.30 \times 10^5)^2$$

$$E_k = 4.4171... \times 10^{-17} \text{ J} = 4.42 \times 10^{-17} \text{ J (3 s.f.)}$$

c) Any of the following:

$$E_k = 4.42 \times 10^{-5} \text{ pJ}$$

$$E_k = 4.42 \times 10^{-8} \text{ nJ}$$

$$E_k = 4.42 \times 10^{-11} \text{ μJ}$$

$$E_k = 4.42 \times 10^{-14} \text{ mJ}$$

$$E_k = 4.42 \times 10^{-15} \text{ cJ}$$

$$E_k = 4.42 \times 10^{-16} \text{ dJ}$$

22. a) $F = kx$

$$1 \text{ cm} = 10^{-2} \text{ m}$$

$$F = (3 \times 10^4) \times (20 \times 10^{-2})$$

$$F = 6000 \text{ N}$$

b) $F = 6 \text{ kN}$

23.

a) $m \approx 6 \times 10^{24} \text{ kg}$ and $r \approx 150\,000\,000\,000 \text{ m}$

$$E_{\text{grav}} = -\frac{GMm}{r}$$

$$E_{\text{grav}} = -\frac{6.67 \times 10^{-11} \times 1.99 \times 10^{30} \times 6 \times 10^{24}}{150\,000\,000\,000}$$

$$E_{\text{grav}} = -5.30932 \times 10^{33} \text{ J}$$

$$E_{\text{grav}} = -5.31 \times 10^{33}$$

b) $1 \text{ kJ} = 10^3 \text{ J}$

$$E_{\text{grav}} = -5.31 \times 10^{30} \text{ kJ}$$

c) $E_{\text{grav}} = -5.0 \times 10^{33} \text{ J}$

d) Mass of an adult $\approx 75 \text{ kg}$

Mass of a car $\approx 1200 \text{ kg}$

$$F = -\frac{Gm_1m_2}{r^2}$$

$$F = -\frac{6.67 \times 10^{-11} \times 75 \times 1200}{1^2}$$

So $F \approx 6 \times 10^{-6} \text{ N}$

Diagnostic Test 2

1. 2.369×10^8

2. 0.00631

3. 1.2 radians

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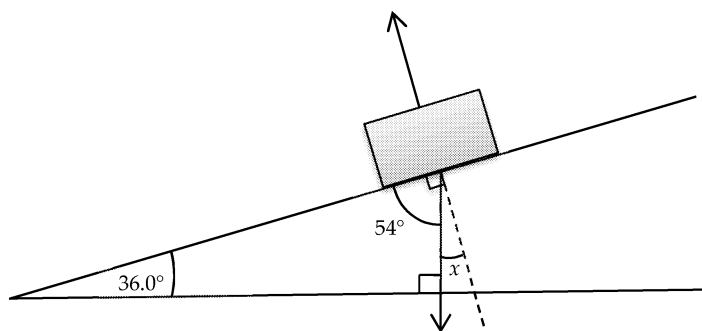
4. 73.3°
5.
 - a) $A = \pi r^2$
 $A = \pi \times (3)^2$
 $A = 28.27$
 $A = 28.3 \text{ cm}^2$
 - b) $A = l \times b$
 $A = 7.2 \times 9.4$
 $A = 68 \text{ m}^2$
 - c) $V = A \times h$
 $V = \pi r^2 \times h$
 $V = \pi \times 1.5^2 \times 5.1$
 $V = 36 \text{ m}^3$
 - d) $V = A \times h$
 $V = l \times b \times w$
 $V = 3.6 \times 4.7 \times 1.1$
 $V = 19 \text{ m}^3$
6.
 - a) 53,021.6
 - b) 0.0365821
 - c) 2.30000×10^{-7}
7.
 - a) mol
 - b) ohm (allow Ω)
 - c) m^3
 - d) s
8.
 - a) $x = \cos^{-1}(0.69)$
 $x = 46.369... = 46^\circ$ (2 s.f.)
 - b) $x = 0.9998...$
 - c) $x = \tan^{-1}(0.47)$
 $x = 25.173... = 25^\circ$ (2.s.f)
9.
 - a) 1.382×10^{10} years
 - b) 1,380,000,000,000,000 years
10.
 - a) A is much less than B and B is much less than the change in C
 - b) C is less or equal to the change in D divided by the change in E
 - c) F is proportional to x if x is greater than or equal to 3
11.

x: 33°
 a: 33°
 b: 35°
 h: 100°

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12.



- a) $x = 36^\circ$
 b) $a = g \sin x$
 $a = 9.81 \times \sin 36$
 $a = 5.7661... = 5.77 \text{ ms}^{-2} \text{ (3 s.f.)}$

13. $s = ut + \frac{1}{2}at^2$
 $s = (2.5 \times 150) + \frac{1}{2} \times 0.2 \times (150)^2$
 $s = 2625 \text{ m} = 2630 \text{ m (3 s.f.)}$

14. a) 1 Hz
 b) 0.1 m
 c) $v = f\lambda$
 $v = (150 \times 3.3)$

$$v = 495 \text{ W}$$

$$\frac{\Delta f}{f} = \frac{1}{150}$$

$$\frac{\Delta f}{f} = 0.00666...$$

$$\frac{\Delta \lambda}{\lambda} = \frac{0.1}{3.3}$$

$$\frac{\Delta \lambda}{\lambda} = 0.0303...$$

$$\frac{\Delta v}{v} = \frac{\Delta f}{f} + \frac{\Delta \lambda}{\lambda}$$

$$\frac{\Delta v}{v} = 0.00666... + 0.0303...$$

$$\frac{\Delta v}{v} = 0.0369...$$

$$\Delta v = 495 \times 0.0369...$$

$$\Delta v = \pm 18.3$$

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$$15. \text{ percentage uncertainty} = \frac{\text{absolute uncertainty}}{\text{measured value}} \times 100\%$$

$$\text{percentage uncertainty} = \frac{0.005}{0.02} \times 100\%$$

$$\text{percentage uncertainty} = 25\%$$

$$16. \text{ percentage change} = \frac{|\text{new value} - \text{original value}|}{\text{original value}} \times 100\%$$

$$\text{percentage change} = \frac{|35 - 30|}{30} \times 100\%$$

$$\text{percentage change} = 16.66... = 17\% \text{ (2 s.f.)}$$

$$17. V = \frac{(9.11 \times 10^{-31}) \times (2.98 \times 10^6)^2}{2 \times (1.6 \times 10^{-19})}$$

$$V = 25.2813... = 25 \text{ V (2 s.f.)}$$

$$18. \text{ mean} = \frac{98.6 + 98.9 + 98.7 + 98.9 + 98.2 + 98.5}{6}$$

$$\text{mean} = 98.633... = 98.6\% \text{ (3 s.f.)}$$

19. Mass of a car $\approx 1200 \text{ kg}$

Speed of a car on a motorway $\approx 30 \text{ m/s}$

$$E_k = \frac{1}{2}mv^2$$

$$E_k = \frac{1}{2} \times 1200 \times 30^2$$

$$E_k \approx 5.4 \times 10^5$$

20. a) V is proportional to I when T is constant.

b) $V = IR$

$$V = (2.3) \times (100)$$

$$V = 230 \text{ V}$$

21. The student cannot predict when a dice will roll a 4 or which dice out mimics not being able to predict which nuclei will decay or which nu radioactive decay.

Each dice has the same chance of rolling a 4 as any of the other 139 di decay as each undecayed nucleus has equal chance of decaying.

$$22. \text{ a) } F = -\frac{GMm}{r^2}$$

$$F = -\frac{(6.67 \times 10^{-11}) \times (6 \times 10^{24}) \times (7.35 \times 10^{22})}{(400\,000\,000)^2}$$

$$F = -1.83841875 \times 10^{20} \text{ N}$$

$$F = -1.84 \times 10^{20} \text{ N (3 s.f.)}$$

b) $F = -1.84 \times 10^{17} \text{ kN}$

c) $F = -1.8 \times 10^{20} \text{ N}$

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