

Topic Tests: Challenge Tests – Set A

For A Level Year 2 AQA

Statistics and Mechanics

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Contents

Thank You for Choosing ZigZag Education	ii
Teacher Feedback Opportunity.....	iii
Terms and Conditions of Use	iv
Teacher’s Introduction.....	1
Cross-referencing Grid	2
Tests	
Test 1 – Regression and Correlation	
Test 2 – Conditional Probability	
Test 3 – The Normal Distribution	
Test 4 – Moments	
Test 5 – Forces and Friction	
Test 6 – Kinematics and Projectiles	
Solutions	

Teacher's Introduction

Content

This pack contains 6 challenge level topic tests and solutions for the AQA Applied Mathematics Year 2 A Level content.

These topic tests have been **fully cross-referenced** to the Pearson, Hodder and Collins textbooks for your convenience (see reference sheet on page 2). Each test has been designed to reflect the specification fully.

About the challenge tests

These **challenge** tests have been designed to **stretch and challenge** your students. 50% of the marks come from questions similar in style to our fundamentals tests. These questions isolate and test the core skills in each topic. The other 50% of the marks come from questions of increased difficulty that progress and start to combine the concepts in the topic. Due to the increased challenge they pose, we recommend these tests for students who have already mastered the fundamentals by scoring 70% or more on our fundamentals tests.

Each test comes with fully worked solutions, containing helpful tips, hints, and technique boxes to help students who may have made a mistake or who are struggling on a particular question.

Timings

The recommended times for students to complete each test are given at the top of individual tests.

Calculator use

The effective use of a calculator is one of the objectives of the new specification and is encouraged for all the enclosed tests. In particular, students should be comfortable using the statistical functions on their calculator.

The large data set

As part of their assessment, students will be tested on data from the **large data set** provided by AQA. This data set contains data on household food and drink purchases from various locations in England between 2001 and 2014. Familiarity with the large data set is assumed in these topic tests, but a copy of it is not needed to take the tests themselves.

Also available from ZigZag Education

The perfect starting point for students of all abilities are our **fundamentals** tests. These isolate and test the core skills in each topic so that your students can show what they can do. They get a confidence boost and you can see at a glance where each student's weaknesses lie.

To prepare students for the exam itself, our **expert** tests contain 25% repeated marks from the fundamentals and challenge tests, and 75% exam-style material with compound/multistep questions.

For each collection of Set A tests we also offer a corresponding collection of Set B duplicated tests with the same styles of questions but different numbers. This allows for a variety of **flexible** uses including:

- **Test → Homework:** Students use test B as a homework to consolidate on areas of weakness identified from completing test A under test conditions in class.
- **Homework → Test:** Students revise as homework using test A before doing test B in class under test conditions.
- **Test → Classwork:** Students work through test B with teacher input to consolidate on areas of weakness identified from completing test A under test conditions in class.
- **Classwork → Test:** Students work through test A with teacher input, before checking their learning by completing test B under test conditions.

For total flexibility, the Set A and Set B tests of all three levels can be run on a rolling basis, using the fundamentals tests as starters, with a time interval between them, leaving one expert level test to use at the end of the course for topic revision.

Free Updates!

Register your email address to receive any future free updates* made to this resource or other Maths resources your school has purchased, and details of any promotions for your subject.

* resulting from minor specification changes, suggestions from teachers and peer reviews, or occasional errors reported by customers

Go to zzed.uk/freeupdates

Cross-referencing Grid

Topic	AQA spec. points	Sub-topics
Regression and Correlation	L2, O1	Exponential models, measuring correlation, hypothesis testing for zero correlation
Conditional Probability	M1–M3	Set notation, conditional probability, conditional probabilities in Venn diagrams, probability formulae, tree diagrams
The Normal Distribution	N2–N3, O3	The normal distribution, finding probabilities, the inverse normal distribution, the standard normal distribution, finding μ and σ , approximating a binomial distribution, hypothesis testing with the normal distribution
Moments	P1, S1	Moments, resultant moments, equilibrium, centres of mass, tilting
Forces and Friction	R2, R4–R6	Resolving forces, inclined planes, friction, modelling with statics, friction and static particles, dynamics and inclined planes, connected particles
Kinematics and Projectiles	Q1, Q3–Q5	Horizontal projection, projection at any angle, projection motion formulae, vectors in kinematics, variable acceleration in one dimension, differentiating vectors, integrating vectors

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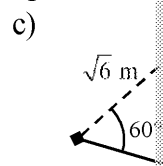
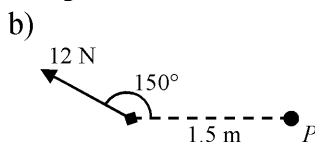
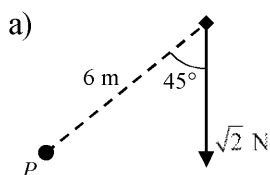
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Moments – Test A (55 mins)

Subtopics: moments, resultant moments, equilibrium, centres of mass

1. Calculate the **moment about the point P** of the forces acting on a lamina.



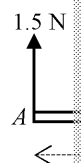
2. The diagram to the right shows vertical forces acting on a **light horizontal rod AB** . Calculate the **resultant moment** about:

- a) the point A
b) the point B
c) the point C

[2]

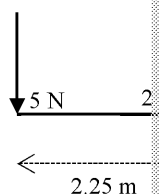
[2]

[2]



3. The diagram to the right shows vertical forces acting on a light rod that is resting horizontally on a support at P .

- a) Show that the resultant moment about P is zero. [2]
b) Does this prove that the rod is in a state of equilibrium? [1]



4. The light rod in the diagram to the right is resting on supports at points P and Q . The rod is in a state of **equilibrium**. By taking moments about P and about Q , find the magnitudes of the reaction forces marked R_P and R_Q . [6]



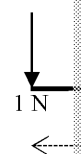
5. A uniform rod AB of length 2 m and mass 1.5 kg is resting horizontally on a support at A . At B the rod is attached to a light, inextensible string that is at an angle of 75° to the horizontal, as shown in the diagram to the right. For this question take $g = 9.8 \text{ m s}^{-2}$.

- a) Draw a force diagram showing the forces acting on the rod. [3]
The rod is in **equilibrium**.
b) By taking moments about a suitable point, find the tension in the string to **3 significant figures**.

6. A **non-uniform** rod AB of mass 25 kg and length 100 cm is resting horizontally on its endpoints, A and B . The centre of mass of the rod is d cm from A .
a) Draw a force diagram showing the forces acting on the rod. The reaction force from the support at B has a magnitude 73.5 N.
b) By taking moments about A , find the value of d .

7. A light rod is supported horizontally at the two points C and D . Forces of magnitude 1 N and 2 N are applied vertically to the rod, while a force of magnitude 20 N is applied at an acute angle of θ to the rod, as shown in the diagram to the right. The rod is on the point of tilting about D .

- a) Find the angle θ . [4]
b) A mass of 1.5 kg is added to the left-hand end of the rod and, at the same time, the force of magnitude 20 N is changed, but remains acute. The rod is now on the point of tilting about C . Find the new value of θ to **3 significant figures**. You should take $g = 9.8 \text{ m s}^{-2}$.



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Preview of Questions Ends Here

This is a limited inspection copy. Sample of questions ends here to avoid students previewing questions before they are set. See contents page for details of the rest of the resource.

Solutions to The Normal Distribution – Test A

1. 217, 6 **A1A1** [2 Marks] **Tip:** then the standard root
2. a) $P(H < 175) = 0.5$ **A1**
 b) $P(H = 175) = 0$ **A1**
 c) $P(H \geq 175) = 0.5$ **A1** [3 Marks] **Tip:** the half prob occurs
3. a) $n = 1250$ is large **A1**
 and
 $p = 0.48$ is close to 0.5 **A1**
 b) $\mu = np$
 $= 1250 \times 0.48$ **M1**
 $= 600$ **A1**
 $\sigma^2 = np(1-p)$
 $= 1250 \times 0.48 \times (1-0.48)$ **M1**
 $= 312$ **A1** [6 Marks]
4. $H_0 : \mu = 314$, $H_1 : \mu < 314$, so test is one-tailed
 Sample size = 50
 Level of significance = 0.01
 Assume H_0 is true, so $X \sim N(314, 128)$ **M1**
 Sample mean \bar{X} is normally distributed with $\bar{X} \sim N\left(314, \frac{128}{50}\right)$ i.e. $\bar{X} \sim N(314, 2.56)$
 $P(\bar{X} < 310.2) = 0.00877447...$ **M1**
 $0.00877447... < 0.01$ so there is sufficient evidence at the 1% level of significance to conclude that the mean of the whole population is less than 314 **A1** [4 Marks]
5. 68% of the data in a normal distribution lies within 1 standard deviation of the mean
 So $0.91 = 1.12 - \sigma$ and $1.33 = 1.12 + \sigma$
 Hence $\sigma = 0.21 \text{ m s}^{-1}$ **A1** [2 Marks]
6. $Y \sim N(\mu, \sigma^2)$ approximates $B(350, 0.54)$
 a) mean = $\mu = np$
 $= 350 \times 0.54$ **M1**
 $= 189$ **A1**
 b) standard deviation = $\sigma = \sqrt{np(1-p)}$
 $= \sqrt{350 \times 0.54 \times (1-0.54)}$ **M1**
 $= \sqrt{86.94}$
 $= 9.32416... = 9.32$ (3 s.f.) **A1**
 c) $P(190 < X < 200) \approx P(190.5 < Y < 199.5)$ **M1**
 $= 0.30602...$ (3 s.f.) **A1** [6 Marks] **Test:** a b normal a co subs vari the
7. Points of inflection: $\mu - \sigma$ and $\mu + \sigma$ **M1**
 $\mu - \sigma = 4.9$ (1)
 $\mu + \sigma = 11.2$ (2) **M1**
 (1) + (2)
 $2\mu = 9.8$
 $\therefore \mu = 4.9$ **A1**
 Substitute this value into (2):
 $4.9 + \sigma = 11.2$
 $\therefore \sigma = 11.2 - 4.9 = 6.3$ **A1** [4 Marks]

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8. $X \sim N(86, 5^2)$

a) $P(X < 81) = P\left(Z < \frac{81-86}{5}\right)$ **M1**
 $= P(Z < -1)$
 $= \Phi(-1)$ **A1**

Technical
standards
 $N(0, 1)$
the for

b) $P(X \geq 85) = P\left(Z \geq \frac{85-86}{5}\right)$ **M1**
 $= P(Z \geq -0.2)$
 $= 1 - P(Z < -0.2)$
 $= 1 - \Phi(-0.2)$ **A1**

Alternative
is symmetrical
 $P(Z \geq -0.2)$

c) $P(87 < X < 87.5) = P(X < 87.5) - P(X < 87)$
 $= P\left(Z < \frac{87.5-86}{5}\right) - P\left(Z < \frac{87-86}{5}\right)$ **M1**
 $= \Phi(0.3) - \Phi(0.2)$ **A1**

9. $X \sim N(\mu, 4)$ and $P(X > 37) = 0.15$

So $P\left(Z > \frac{37-\mu}{4}\right) = 0.15$ **M1**

Technical
standards
can the
distribution
calculate
in the
normal
problem

$\therefore \frac{37-\mu}{4} = 1.03643...$ **M1**

Rearranging this gives $\mu = 37 - (4 \times 1.03643...) = 32.8542... = 32.9$ (3 s.f.) **A1**

10. $H_0 : \mu = 190, H_1 : \mu < 190$, so test is one-tailed **M1**

Sample size = 30

Level of significance = 0.1

Assume H_0 is true, so $X \sim N(190, 33^2)$ **M1**

Sample mean \bar{X} is normally distributed with $\bar{X} \sim N\left(190, \frac{33^2}{30}\right)$, i.e. $\bar{X} \sim N(190, 36.3)$

$P(\bar{X} < 183) = 0.122651...$ **M1**

$0.122651... > 0.1$ so there is insufficient evidence at the 10% level of significance to reject H_0 that the mean CO₂ emissions of cars registered in 2002 is less than 190 g/km **A1**

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Preview of Answers Ends Here

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