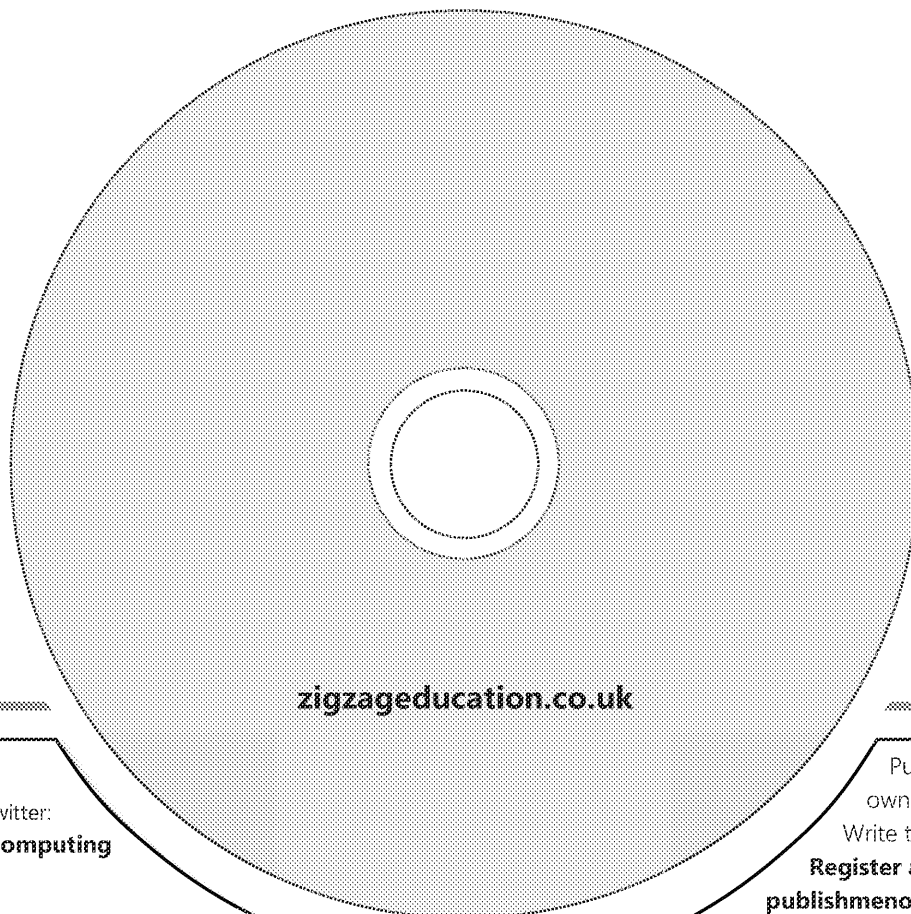


C# Exercises

for AS & A Level AQA Computer Science



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Teacher's Introduction

This resource has been designed to support the development of students' programming skills at KS5.

It contains 10 unique exercises, featuring a range of scenarios that develop the core programming principles, as well as bringing to life a number of important concepts across the A Level AQA specification – including programming constructs, recursion, global/local variables, modularity, debugging programs, object-oriented techniques, divide-and-conquer algorithms, data structures and standard algorithms.

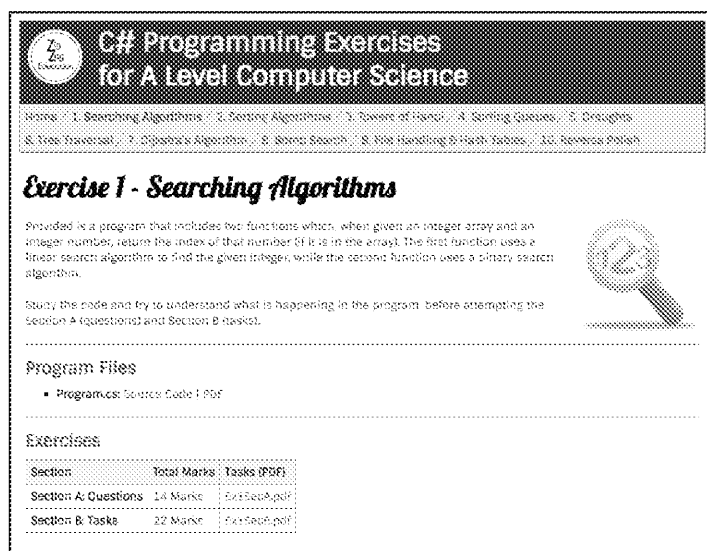
Each exercise contains a combination of questions and tasks, and consists of two sections – Section A and Section B.

Section A

Section A provides a series of questions that test theoretical understanding of the code. The code that these questions are based on is provided as .cs files and as PDFs for convenient printing. These questions require written responses only – **no programming is required.**

Section B

Section B provides a series of tasks that require the programs to be modified in order to make improvements and/or develop their functionality – **programming is required.**



C# Programming Exercises for A Level Computer Science

Exercise 1 - Searching Algorithms

Provided is a program that includes two functions which, when given an integer array and an integer number, return the index of that number (if it is in the array). The first function uses a linear search algorithm to find the given integer, while the second function uses a binary search algorithm.

Study the code and try to understand what is happening in the program before attempting the Section A (questions) and Section B (tasks).

Program Files

- Program.cs Source Code 1 PDF

Exercises

Section	Total Marks	Tasks (PDF)
Section A: Questions	14 Marks	Ex1SecA.pdf
Section B: Tasks	22 Marks	Ex1SecB.pdf

For every exercise, there is source code, which students will need to save to their computer (or other local directory) and open in a code editor before they can complete the tasks.

Section B should take longer than Section A to complete and will aid preparation for the non-exam assessment (NEA) and any other practical assessments.

The question/task sheets can be photocopied or, if using the PDF versions on the CD, can be printed or simply followed on-screen (for Section B especially).

Suggested solutions and mark schemes for all questions/tasks are provided (in print and as electronic copies on the CD). Note that credit should be given for any valid responses that are not explicitly included in this resource. Exemplar C# files demonstrating all of the Section B changes made for every exercise are also included on the CD.

Note that the mark schemes and solution files are not directly accessible to the students via the HTML interface ([index.html](#)), but can be accessed directly from the resource folder.

A Level AQA Computer Science Specification Map

	1	2	3	4	5	6	7	8	9	10
	Searching Algorithms	Sorting Algorithms	Towers of Hanoi	Sorting Queues	Draughts	Tree Traversal	Dijkstra's Algorithm	Bomb Search	File Handling & Hash Tables	Reverse Polish
1.1.1 – Data types	✓	✓	✓	✓	✓		✓	✓	✓	✓
1.1.2 – Programming concepts	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓
1.1.3 – Arithmetic operations	✓	✓		✓	✓	✓	✓	✓	✓	✓
1.1.4 – Relational operations	✓	✓	✓	✓	✓		✓	✓	✓	✓
1.1.5 – Boolean operations	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓
1.1.6 – Constants and variables	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓
1.1.7 – String handling	✓	✓	✓		✓		✓	✓	✓	✓
1.1.8 – Random numbers	✓							✓		
1.1.9 – Exception handling	✓	✓			✓			✓		✓
1.1.10 – Subroutines		✓	✓	✓	✓	✓	✓	✓	✓	✓
1.1.11 – Parameters	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓
1.1.12 – Returning values	✓	✓	✓		✓	✓	✓	✓	✓	✓
1.2.1 – Programming paradigms	✓	✓	✓	✓	✓		✓	✓	✓	✓
1.2.2 – Procedural paradigms	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓
1.2.3 – Object-oriented paradigms	✓	✓		✓	✓	✓	✓	✓	✓	✓

(Continues on next page)

(Continued from previous page)

	1	2	3	4	5	6	7	8	9	10
	Searching Algorithms	Sorting Algorithms	Towers of Hanoi	Sorting Queues	Draughts	Tree Traversal	Dijkstra's Algorithm	Bomb Search	File Handling & Hash Tables	Reverse Polish
2.1.2 – Arrays	✓	✓	✓	✓	✓		✓	✓	✓	✓
2.1.4 – Data structures			✓	✓		✓	✓			✓
2.2.1 – Queues				✓						
2.3.1 – Stacks			✓							✓
2.4.1 – Graphs							✓			
2.5.1 – Trees						✓				✓
2.6.1 – Hash tables									✓	
3.1.1 – Graph-traversal						✓				
3.2.1 – Tree-traversal						✓				✓
3.3.1 – Reverse Polish Notation							✓			✓
3.4.1 – Linear search	✓								✓	
3.4.2 – Binary search	✓									
3.5.1 – Bubble sort		✓								
3.5.2 – Merge sort		✓								
3.6.1 – Dijkstra's shortest path							✓			

EXERCISE 1 — SEARCHING ALGORITHMS

SECTION A

A 1

Give a line number from the program that contains a function call.

A 2

Give the line number from the program that contains a DIV operation.

A 3

Explain why, given a choice of both, a binary search is often preferable.

A 4

Explain why some arrays are not searchable with a binary search algorithm.

A 5

The program uses a constant.

Explain why a constant was a suitable choice in this case.

A 6

Both functions return -1 if no value is found.

Explain why -1 is a suitable choice of value in this case.

A 7

The `linearSearch` function does not use an ELSE statement as part of its logic.

Explain why it is not essential to use an ELSE statement in this case.

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A 8

Explain what is meant by the time complexity of an algorithm.

.....

.....

.....

A 9

State the time complexity of the linear search and binary search algorithm.



.....

.....

A 10

The binary search algorithm can be implemented using recursion.
Explain why a recursive version of the binary search algorithm may not be suitable.

.....

.....

.....



EXERCISE 1 — SEARCHING ALGORITHMS

SECTION B

B 1

Identify and correct the syntax error in this version of the linear search

```
private static int linearSearch(int[] searchList, int searchVal) {
    for(int i=0; i < searchList.Length; i++) {
        if (searchList[i] = searchVal) {
            return i;
        }
    }
    Console.WriteLine("Value not found!");
    return VALUE_NOT_FOUND;
}
```

Program in question has been successfully corrected ☐

B 2

Modify the program so that when the functions do not find the value part of the message shown on the console.

Program updated ☐

B 3

Modify the program so that the identifier x is replaced with a better value

Program updated ☐

B 4

Modify the program to add a recursiveBinarySearch function to and indices to call at the start and end of the portion of the array which is being searched. The recursiveBinarySearch function should return the index of the search value if it is in the array, and "Value not found" if the value is found not to be in the array. The main program procedure should be updated to call this procedure

Program updated ☐

B 5

Modify the program to add a getVal function that asks the user for an integer. This function should take no arguments and be able to handle user input. The main program procedure should be updated to call this function. The getVal function will end up being passed to each of the search methods.

Program updated ☐

B 6

Modify the program to add a generateList function that is given a value and returns an ordered array of all positive integers from 1 to the given value. The main program procedure should be updated to call this procedure to create the search list given by the user.

Program updated ☐

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B

7

Create duplicate copies of the methods `linearSearch` and `binarySearch` to be on comparing their time efficiency. The duplicate methods should be called `timedLinearSearch` and `timedBinarySearch`. The new functions should have a count variable that increments by 1 every time a new element is visited. The count should be returned when the search ends (either if the value is found or when the search value is not in the array).

A `testLinearTimings` function should now be added that accepts

- `n` for the length of the array to be used for testing purposes
- `tests` for the number of tests that should be carried out on the array

The function should generate an array of length `n` and then repeatedly search the array `tests` times. It should then return the average (i.e. the mean) of the times taken by the `linearSearch` method. It is advisable to search for values 1, 2, ..., `n` so that all elements in the array are searched for.

Next, a similar method called `testBinaryTimings` needs to be created. This should be done on arrays using binary searches and then find the average amount of time taken by the `testLinearTimings` function and modify the copy to fulfil the same purpose.

The main program procedure should now have test code added to it. Arrays of length 1,000 and 10,000 are created and the same numbers of searches are performed (i.e. 10 for each array is searched for once). The main program should output the results of the searching alongside the average time taken for binary searching, such as:

```
Test LINEAR timings (10 elements, 10 tests): 9.5
Test BINARY timings (10 elements, 10 tests): 2.9
Test LINEAR timings (100 elements, 100 tests): 54.5
Test BINARY timings (100 elements, 100 tests): 8.8
Test LINEAR timings (1,000 elements, 1,000 tests): 500.5
Test BINARY timings (1,000 elements, 1,000 tests): 8.907
Test LINEAR timings (10,000 elements, 10,000 tests): 5000.5
Test BINARY timings (10,000 elements, 10,000 tests): 12.3631
```

Programmer's Note:



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EXERCISE 2 – SORTING ALGORITHMS

SECTION A

A 1

Explain how the integer values for the array are passed in on line 9.



A 2

State the line number from the `mergeSort()` method where recursion

A 3

Define 'recursion'.

A 4

The character `'\t'` is used in the `Main()` method.
Explain what it is and how it has been used in this case.



A 5

When the `bubbleSort` function is called, the program uses a Boolean variable.
Explain the role played by this variable.

A 6

A FOR loop is used in the `bubbleSort()` method. The value of the loop counter is as far as the value before `SIZE-1` instead of going all the way up to the value of `SIZE-1`.
Explain why this is the correct approach to use in this case.



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A 7

The purpose of the `split()` method is to separate one array into two. If the number of elements in the original array is even, the two arrays will be of equal length. If the original array contains an odd number of elements, the middle element of the original array will be the first element of the second array. Determine what will happen to the middle element of the original array if the original array contains an odd number of elements. Explain the role of the `DivideAndConquer` class.



A 8

The merge sort algorithm is an example of a divide-and-conquer algorithm. Explain what a divide-and-conquer algorithm is.

A 9

Compare the time complexity of the bubble sort and merge sort algorithms.

A 10

Another method of sorting an array of numbers is known as an insertion sort. Describe how the insertion sort algorithm works.



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EXERCISE 2 — SORTING ALGORITHMS

SECTION B

B 1

Modify the program to allow the user to enter a list of 12 integers.

Program updated ☐

B 2

Modify the program so that the bubbleSort function outputs the full array after each pass. It has stepped through the elements from left to right and before it restarts the next pass, it has copied a copy of the current array to a newly written method. Once this has been achieved, modify the Main() method to make use of the many FOR loops which do the same task.

```
Bubble sort returns:
2 7 8 3 0 -5 -3 1
2 7 3 0 -5 -3 1 -6
2 3 0 -5 -3 1 -6 4
2 0 -5 -3 1 -6 3 -8
0 -5 -3 1 -6 2 -8 3
-5 -3 0 -6 1 -8 2 3
-5 -3 -6 0 -8 1 2 3
-5 -6 -3 -8 0 1 2 3
-6 -5 -8 -3 0 1 2 3
-6 -8 -5 -3 0 1 2 3
-8 -6 -5 -3 0 1 2 3
-8 -6 -5 -3 0 1 2 3
-8 -6 -5 -3 0 1 2 3
```

Program updated ☐

B 3

Modify the FOR loop of the bubbleSort function so that it doesn't sort elements that are known to already be sorted, i.e. those that have been sorted after each pass. To achieve this, stop the nested loop from going all the way to the end of the array.

Program updated ☐

B 4

Modify the program so that the program does not crash if the user enters a non-integer. Prompted to add a number to the array. Your solution should display the error message when they have entered a non-integer number and keep asking for a valid integer.

```
Add an integer number to the list: 5
Add an integer number to the list: 7
That was not an integer; please try again.
Add an integer number to the list: 3
Add an integer number to the list: -9
Add an integer number to the list: 1
Add an integer number to the list: 2
Add an integer number to the list: -6
Add an integer number to the list: 0
That was not an integer; please try again.
Add an integer number to the list: 4
That was not an integer; please try again.
Add an integer number to the list: 6
Add an integer number to the list: 4
Add an integer number to the list: 4
Add an integer number to the list: 8
Add an integer number to the list: -2
That was not an integer; please try again.
Add an integer number to the list: +
That was not an integer; please try again.
Add an integer number to the list: -8
Original list of values given:
5 7 3 -9 1 2 -6 6
```

Program updated ☐

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B 5

Currently, the code (which has just been improved in Task B4) that asks the user to enter values into the array is hard-coded into the main program procedure, and so it is not reusable. Modify the program so that this code is moved into a new `GetList()` function. The function should take an array as a parameter and returns the array fully populated with values. The main program procedure to overwrite the empty array `numList` should be modified to call `GetList()` as described in Task B4.

Program updated ☐

B 6

Modify the `GetList` function so that the user can also choose to enter values into the array separated by commas (e.g. 4, 4, 2, 17, 14, 12) to give their entire array at once. The `Split()` method of the `String` class may be used to achieve this. The user should still have the option to enter numbers individually if they prefer. Use the comment in this task to make the list option robust enough to deal with both cases.

```
Would you like to provide the list of values one at a time? Key Y or N
N
Please key in your list of 12 integers in the following format, where N=N,N,N,N,N,N,N,N,N,N,N,N
4,7,6,8,9,0,0,3,4,5,6,7
Original list of values given:
4 7 6 8 9 0 0 3
Bubble sort returns:
4 6 7 8 9 0 3 4
4 6 7 8 9 3 4 5
4 6 8 8 3 4 5 6
4 8 8 3 4 5 6 6
9 8 3 4 4 5 6 6
9 8 3 4 4 5 6 6
9 8 3 4 4 5 6 6
Merge sort returns:
9 8 3 4 4 5 6 6
```

Program updated ☐

B 7

Modify the `bubbleSort` function so that it passes the array and the number of elements to a new `Swap()` function which uses the parameters passed to it to return the values correctly swapped around. The `bubbleSort()` function should be modified to use this function.

Program updated ☐

B 8

Thoroughly comment the entire `merge()` function to aid future programmers.

Program updated ☐

B 9

Modify the program's output to observe the behaviour of the `bubbleSort()` function. The `bubbleSort()` function should now include a `swaps` variable that counts the number of swaps made on each pass. The program should display the value of `swaps` after each pass, and the total number of swaps performed after the next pass.

Test it with a sorted list and it should produce the following output along the following lines:

```
Original list of values given:
0 1 2 3 4 5 6 7
Bubble sort returns:
0 1 2 3 4 5 6 7
Number of swaps this pass: 0
0 1 2 3 4 5 6 7
```

Program updated ☐

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EXERCISE 3 – TOWERS OF HANOI

SECTION A

A 1

Give a line number from the `Game` class where an instance variable is

A 2

What percentage of the methods in the `Tower` class are constructors?

A 3

Discs can only be removed from or added to the end of a tower's array.
State the data structure which represents this behaviour and describe
of that data structure.

A 4

The program requires less information when the `Game` class tries to instantiate
`towerThree`.

How can all three towers get successfully instantiated despite the
requirements.

A 5

The program does not accept "ONE", "TWO" or "THREE" as valid input.
Explain what would happen if such inputs were given and how C# would

A 6

A less robust program could crash if the player tried to move a disc from
a tower to itself.
Explain how the `Move()` method handles this eventuality.

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A 7

The OR operator is used to perform a check before a valid move occurs. Explain the role of the OR operator in this case.

A 8

Explain the operation of the RemoveFirst() method of the Tower class.



A 9

The program uses multiple classes for encapsulation. State the meaning of encapsulation and why it is useful.

A 10

Outline the differences between an array and a list.



EXERCISE 3 — TOWERS OF HANOI

SECTION B

B 1

Modify the program to output an introductory line at the start of a new game, showing the name of the game.

Program updated ☐

B 2

Modify the program so that it accepts "ONE", "TWO" and "THREE" as input for the number of discs. Make this so that it is robust enough to accept the letters in any case, e.g. it accepts "One", "ONE", "oNe" and "one".

Program updated ☐

B 3

The instance variable `Number` in the `Tower` class currently has public mutator methods for this variable and set its visibility to private, modify the program so that they call the relevant accessor/getter method instead.

Program updated ☐

B 4

Modify the program so that it displays a simple visual representation of the towers after each move is played.

```
START TOWER CHOSEN = 2
END TOWER CHOSEN = 3
VALUE BEING MOVED = 0
Disc moved successfully to tower #3
TOWER #1 >> 5 4
TOWER #2 >> 1
TOWER #3 >> 2 0
```

Program updated ☐

B 5

Modify the program to add a `CheckWon` function in the `Game` class that returns `True` if the game has been successfully completed, or otherwise returns `False`. (Hint: The `CheckWon` function should be a line of code inside a method body!). The `Main` procedure should be modified to call the `CheckWon` function to end the game once it has been won, and then displays the message. Modify the program to print a message to tell the player that they have completed the game. Change the `while True:` loop to use a more appropriate condition, as `while True` loops should be reserved for testing purposes or infinite loops.

Program updated ☐

B 6

The minimum number of moves needed to complete the game is $2^n - 1$, where n is the number of discs. So a game with three discs can be completed in 7 moves, a game with four discs in 15 moves, etc.

Modify the program to allow the user to choose the number of discs. The program should then output the minimum number of moves needed to complete the game. The program should also check for invalid inputs of the number of discs, such as non-integer data type and integers that are out of range. If the user enters an invalid input, the program will keep track of how many successful moves the user has made. If the user enters a valid input, output a message congratulating them on achieving their goal, or else encouraging them to try again to see if they can make it.

Program updated ☐

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EXERCISE 4 – SORTING QUEUES

SECTION A

A 1

How many private members (i.e. attributes and methods) are there in

A 2

Give a line of code from the Node class that demonstrates parameter



A 3

A queue is one type of data structure; a stack is another type.

Explain the difference between a queue and a stack.

A 4

The method `IdentifyQueueTail()` is used to find the tail node in

State why this method must therefore be a part of the `Enqueue`

A 5

`PrintQueue()` procedure uses a FOR loop.

Explain the purpose of the FOR loop.



A 6

The `Node` constructor sets a new node's pointer to be null. Explain why

A 7

The queue is implemented as a linked list.

Explain one advantage of using a linked list instead of an array to imple



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A

8

Having read and understood the code, describe in words how to enqueue that is implemented as a linked list.



A

9

Queues can be implemented in different ways; for example, as a circular queue. Explain what a circular queue is.

A

10

Explain why a queue is used in the program and how you can check if it is full.



EXERCISE 4 – SORTING QUEUES

SECTION B

B 1

Modify the program so that it outputs a meaningful message to the console when an item is dequeued (added to the tail of the queue) using the lines of the example below.

```
-----Cactus-----
-----Spices-----
queue is empty.

-----Plants-----
The value Elderflower has been enqueued to the Plants queue
The value Bonsai has been enqueued to the Plants queue
1      Cactus
2      Elderflower
3      Bonsai

-----Spices-----
The value Cinnamon has been enqueued to the Spices queue
The value Cardamom has been enqueued to the Spices queue
The value Fenugreek has been enqueued to the Spices queue
The value Paprika has been enqueued to the Spices queue
1      Cinnamon
2      Cardamom
3      Fenugreek
4      Paprika

-----Plants-----
The value Elderflower has been dequeued from the Plants queue
The value Bonsai has been dequeued from the Plants queue
Program updated ☐
```

B 2

Modify the program so that it outputs a meaningful message to the console when an item is dequeued (removed from the head of the queue). Be careful where you place the code.

Program updated ☐

B 3

Add a method called `GetSize()` to the `Queue` class which returns the number of items in the queue. The method should work with empty queues (size = 0). Choose meaningful names and any variables used within it. Write code in `Program.cs` to test the method. Add comments on all newly added code.

Program updated ☐

B 4

A 'doubly linked' list (also known as a 'two-way' linked list) uses pointers and pointers that point to the previous value in the list. Modify the `Node` class to include a `Previous` attribute that indicates the node that comes before it. Add a `SetPrevious()` function and the `SetPrevious()` procedure to the `Node` class.

The methods `Enqueue()` and `Dequeue()` should be amended accordingly to include the new attribute. Finally, the constructor for a queue which takes a node should be amended so that it calls the `Enqueue()` method from now on. Suitable test code should be added into `Queue.PrintQueue()` to ensure that it has succeeded.

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Exemplar output is shown below.

```
-----Spices-----
#  VALUE  (...PREVIOUS VALUE)
1  Cinnamon (...)
2  Cardamom (...Cinnamon)
3  Fenugreek (...Cardamom)
4  Paprika (...Fenugreek)
5  Nutmeg (...Paprika)
-----
```

Program updated

B 5

GetNodeAt (n) function to the Queue class which gets the nth node. Node indexing should NOT be used. Assume that the first node in the queue is the head.

Add a Bump () procedure to the Queue class.

When the function is called, as long as there are two or more items in the queue, show an on-screen printout of the queue and they should then be asked to indicate a particular position in the queue (#1 represents the head of the queue, the head of the queue will be regarded as #1, the only valid inputs are integers greater than 1 and have no previous node with which to swap) and ranging all the way up to the last node in the queue. Suitable validation should be included to make this procedure robust.

```
There are currently 4 items in the queue:
-----Spices-----
#  VALUE  (...PREVIOUS VALUE)
1  Cinnamon (...)
2  Cardamom (...Cinnamon)
3  Fenugreek (...Cardamom)
4  Paprika (...Fenugreek)
-----
Which queue item (2-4) should be swapped with the item 1?
Please choose a queue item number in the range 2 to 4.
> 1
This is not an integer value; please try again.
> 1.5
This is not an integer value; please try again.
> 4
The user has chosen Paprika to be bumped up the queue...here
The queue bump is complete!
-----Spices-----
#  VALUE  (...PREVIOUS VALUE)
1  Cinnamon (...)
2  Cardamom (...Cinnamon)
3  Paprika (...Cardamom)
4  Fenugreek (...Paprika)
-----
```

The program should then swap that node with the previous node in the queue. This is the 'bumping' the user's chosen node closer to the front of the queue. Update Program.cs to ensure that the Bump () procedure is working effectively.

Here is some structured analysis to guide the latter half of this task once you have been received:

1. Traverse through the queue until the desired node is reached and swap it with the previous node. Work through each of the three Pointer variables and modify the queue).

- Work through each of the three previous pointers and modify the tail towards the head of the queue).
- Output the newly sequenced queue.

Program updated ☐

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B	6
---	---

Bubble sort is a sorting algorithm where values held in a linear data structure are compared and potentially swapped with adjacent values. On each pass, the maximum value 'bubbles' to the head and takes its place as the maximum value. On successive passes to ignore that node.

Having developed a swapping procedure, make a copy of it and name it `Swap()`. Modify `Swap()` to swap the position of an item in the queue (as a `QueueItem`) and the `Swap()` procedure to swap the value that is currently ahead of it in the queue.

Next, build a procedure called `BubbleSort()` that uses the `Swap()` procedure to bubble sort a queue held as a linked list into alphabetical order. This procedure should start from the tail of the queue and keep 'bubbling' the earlier values to the head.

The `BubbleSort()` procedure should return straight away if there are no items in the queue.

Program updated ☐

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EXERCISE 5 — DRAUGHTS

SECTION A

A 1

Give the class name and the line number from the program where a `Piece` object is created.

.....

A 2

Give a class name and the line number from the program where a private field is



declared

gets initialised.....

has its value read in full

A 3

Explain why the `PlacePieces` method is private instead of public.

.....

.....

.....

A 4

Explain why the constructor of the `Piece` class requires one and only one argument to it.



.....

.....

.....

A 5

Which of the following is true?

1. 'Each piece stores its position on the board.'
2. 'The board stores the piece positioned on each square.'

Explain your answer.

.....

.....



.....

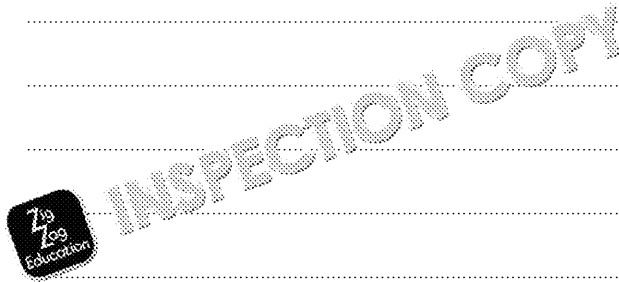
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A 6

Explain how the program generates the output shown below when it runs. List the methods involved and describe what they do, but you do not need to carry out their roles.



#	0	1	2	3	4	5	6
0		R				R	
1	R		R		R		R
2		R		R		R	
3							
4							
5	B		B		B		B
6		B		B		B	
7	B		B		B		B

A 7

The value 8 is hard-coded into the `Board` class to represent the size of the board. Explain why this is considered bad practice and what should be used instead.



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A 8

Explain the use of the MOD operator in placing the pieces on the board.

.....

.....

.....

A 9

A new King class could be created that inherits the Piece class.

Explain the difference and why it is useful.



.....

.....

.....

.....

A 10

Explain the difference between functions, procedures and methods.



.....

.....

.....

.....

A 11

A Board object is created to represent one game's board.

Explain the difference between an object and a class in this case.



.....

.....

.....

EXERCISE 5 — DRAUGHTS

SECTION B

B 1

Modify the program so that the white squares are indicated by an underscore is displayed.



#	0	1	2	3	4
0		R	—	R	—
1	R	—	R	—	R
2	—	R	—	R	—
3		—		—	
4	—	—	—	—	—

Program updated ☐

B 2

Modify the program to add a `BoardSize` attribute to the `Board` class. It should be set to 8 in the constructor, and the `BoardSize` attribute should be hard-coded values throughout the `Board` class.

Program updated ☐

B 3

Add an accessor method for the `BoardSize` attribute.

Program updated ☐

B 4

Modify the program to add a public `PieceAt` function into the `Board` class. It takes two integers (a row and a column from the board) as input and returns the piece found there. Zero-based indexing should be used. Validate the user's input is within range, and return a `Null` value if either is out of range.

Add a procedure called `DisplayPieceAt` into the `Board` class. It takes two integers (a row and a column from the board) as input and return the character representation of the piece found there, treating black and white pieces differently from all white squares. Add code to the `Program` class to test the `PieceAt` and `DisplayPieceAt` functions.

```
No piece is found at [4,5].
[0,0] is a white square so no pieces
R is found at [0,1].
B is found at [7,0].
```

Program updated ☐

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Add a private integer attribute called `TurnNumber` to the `Board` class moves made by the players. When whoever is playing as black (B) moves of turns should be incremented from 1 to 2. Amend the constructor accordingly and a mutator method that simply increments it.

Modify the program to add a `ValidMove` function in the `Board` class (representing a start position and an end position on the board) as indicating if the given colour can move a piece from the given start position to the end position. The ability to do repetitive moves in a game of draughts can be determined by whether the correct colour piece has been chosen by the player will



The rules of draughts movement which must now be programmed are:
 • Pieces can move in a straight diagonal line either one space (king) or two spaces (if the tile one space diagonally on from the start position is empty).
 • Non-king pieces can move only towards the opponent's side.

- King pieces can move in any diagonal direction.
- Pieces cannot move to a position that is not on the board.

Here is a pseudocode structure you can follow:

Store the PieceToBeMoved as a Piece variable
Return False if PieceToBeMoved isn't an actual Piece
Return False if the destination is off the board

IF PieceToBeMoved is not a king:

- *IF it's Black's move:*
 - *IF Black is moving only 1 row 'forwards' AND 1 column:*
 - *IF the destination is empty:*
 - *ALLOW*
 - *ELSE*
 - *DISALLOW*
 - *ELSE IF Black is moving 2 rows away:*
 - *IF Black is moving 2 columns left or right:*
 - *IF the destination is empty:*
 - *IF there is a Red in between:*
 - *ALLOW*
 - *ELSE*
 - *DISALLOW*
 - *ELSE*
 - *DISALLOW*
 - *ELSE*
 - *DISALLOW*
 - *ELSE*
 - *DISALLOW*
- *ELSE*
 - *... as above but reinterprets the idea of 'forwards' and the*

ELSE:

- *... as Above but with more freedom of movement between*



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Modify the program to include a `ValidColour` method which takes as parameters and returns `True` if the user has their correct colour of piece, and `False` if the user has an incorrect colour. To achieve this, firstly check if the playing piece chosen is correct, and then proceed to check the colour against the turn number.



B 7

Modify the program to add a `GetMove` procedure that asks the user (at a time) and then checks if the playing piece lifted by the user is of (using the turn number that the game is currently at). If the colour is proceed to read in an end position (one integer at a time) and check given by calling the `ValidMove` method.

Assuming all checks pass, the move should be updated accordingly and amended accordingly. If `ValidMove` fails, the user should be told "If the colour test fails, the user should be told "The board has not been changed. Try again; it is still the same."

All four integers from the user should be fully validated using `ValidMove` should be added to the `Program` class so that six moves can be made some invalid.

Program updated ☐

B 8

Modify the program to add a `CheckWon` function that returns the player as a string (if the game has been won) or returns an empty string if not. To support the development of this method, add two instance variables: `pieces of each colour that have been removed from the board`.

Add lines of code to the `GetMove` method so that when a piece is just on the board.

The main method of the program should be modified to run in a loop from each player until one of the players has won, displaying the status. At the end of the game, a message should be displayed to say which player won.

Program updated ☐

B 9

Modify the `GetMove` method so that when a piece reaches the opposite end of the board, the code for awarding King status for Red and Black is still valid. If the board size was increased or decreased.

Modify the `Piece.cs` class so that when a piece is kinged, its letter is updated. Use this approach so that if the kinged piece re-enters the far row, it will not be kinged any way:

```
("" + Colour).ToLower()[0]
```

#	0	1	2	3	4	5
0		R		b		R
1	R		R			
2				R		
					R	

Program updated ☐

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EXERCISE 6 — TREE TRAVERSAL

SECTION A

A 1

Give a class name and line number from the program that contains a call to a constructor

private attribute definition



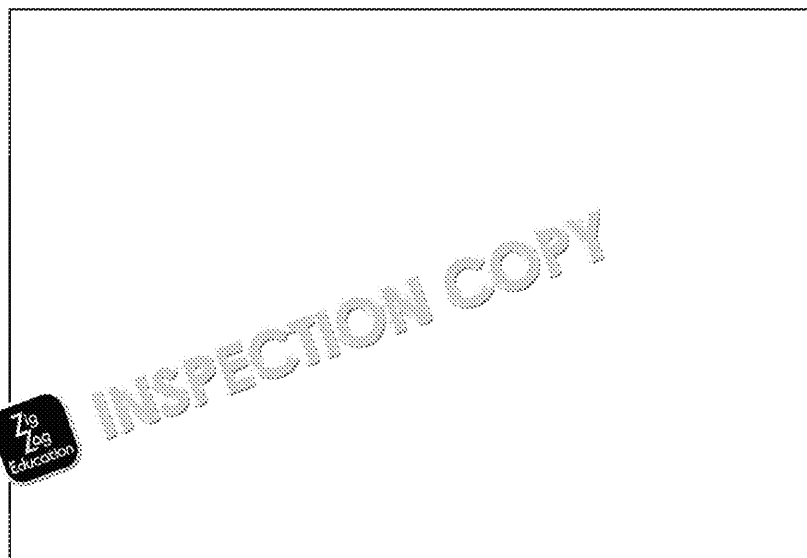
a null pointer

A 2

Give the class name and line number from the program that shows the

A 3

Draw the tree that is created by the program. You only have to show



A 4

The tree created by the program is a binary tree.

Explain the difference between a binary tree and a multi-branch tree.

A 5

The program uses recursion. Explain with reference to the Node



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A 6

The program uses just four data types. Name all four of them.

- 1.....
- 2.....
- 3.....
- 4.....

A 7

Write a line of code that would attempt to display the value found at `tree[0][0]`. This line of code would not work.



A 8

Explain how C# would handle the error that would occur in Task A7 as written.

.....

.....

.....

.....

A 9

Write the tree values as they would be returned in a depth-first, post-order traversal.

.....

A 10

Write the tree values as they would be returned in a depth-first, pre-order traversal.



.....

A 11

Write the tree values as they would be returned in a depth-first, in-order traversal.

.....

A 12

Write the tree values as they would be returned in a breadth-first tree traversal.

.....

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EXERCISE 6 — TREE TRAVERSAL

SECTION B

B 1

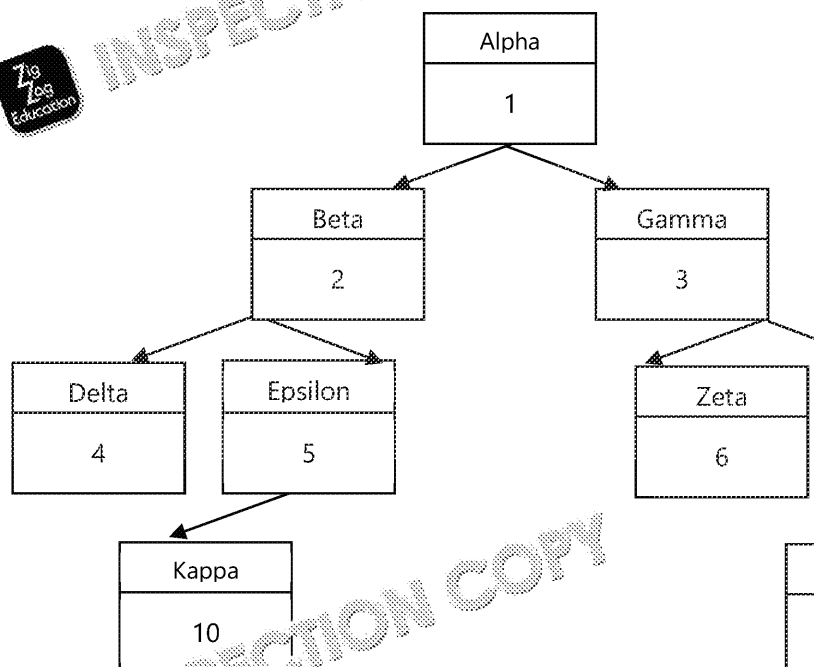
Modify `Node.cs` so that it contains a procedure that can print a full set of information about a node, as per the example output below. Insert the code into `Program.cs` so that it prints out all four existing nodes of `GreekTree`.

```
-----ALPHA-----
The value held in this node is 1
To its left is the value 2
To its right is the value 3
-----BETA-----
The value held in this node is 2
To its left is the value 4
There is no node to its right.
-----GAMMA-----
The value held in this node is 3
There is no node to its left.
There is no node to its right.
-----DELTA-----
The value held in this node is 4
There is no node to its left.
There is no node to its right.
```

Program updated ☐

B 2

Modify `Program.cs` so that `GreekTree` represents this binary tree at the end of any existing code in task B1.



Program updated ☐

B 3

Modify the program so that it creates a new tree called `AssortedTree` and have the value 24, and there should be only a right node whose value is 8. Add a line of code to display the full set of information.

Program updated ☐

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B 4

Modify `Program.cs` to add a recursive `PostOrderTraversal` procedure that takes a `TreeNode` as input and performs a depth-first, post-order tree traversal from that root node. The values should be separated by > symbols as it progresses.

To achieve this, here is a suitable algorithm for the body of the procedure:

If NOT Null:

- Traverse the Left subtree via a recursive call that passes in the left child of the node
- Traverse the Right subtree via a recursive call that passes in the right child of the node
- Display the Value followed by a > symbol without taking a newline



The `Main` procedure should be modified to test the procedure twice using the `PostOrderTraversal` procedure using the `Root` value from both of the programs. Each value should be displayed in the order in which it is displayed and this should be manually checked for correctness.

```
>>>> POST-ORDER TRAVERSAL: GreekTree >>>>
4 > 10 > 5 > 2 > 6 > 14 > 15 > 7 > 3 > 1 >
>>>> POST-ORDER TRAVERSAL: AssortedTree >>>>
8 > 24 >
```

Program updated ☐

B 5

Modify the program to add a recursive `PreOrderTraversal` procedure that takes a `TreeNode` as input and performs a depth-first pre-order tree traversal from that root node. The values should be separated by > symbols as it progresses.

The `Main` procedure should be modified to test the procedure twice using the `PreOrderTraversal` procedure using the `Root` value from both of the programs. Each value should be displayed in the order in which it is displayed and this should be manually checked for correctness.



```
>>>> PRE-ORDER TRAVERSAL: GreekTree >>>>
1 > 2 > 4 > 5 > 10 > 3 > 6 > 7 > 14 > 15 >
>>>> PRE-ORDER TRAVERSAL: AssortedTree >>>>
24 > 8 >
```

Program updated ☐

B 6

Modify the program to add a recursive `InOrderTraversal` procedure that takes a `TreeNode` as input and performs a depth-first, in-order tree traversal from that root node. The values should be separated by > symbols as it progresses.

The `Main` procedure should be modified to test the procedure twice using the `InOrderTraversal` procedure using the `Root` value from both of the programs. Each value should be displayed in the order in which it is displayed and this should be manually checked for correctness.



```
>>>> IN-ORDER TRAVERSAL: GreekTree >>>>
2 > 10 > 5 > 1 > 6 > 3 > 14 > 7 > 15 >
>>>> IN-ORDER TRAVERSAL: AssortedTree >>>>
24 > 8 >
```

Program updated ☐

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B

7

Modify the program to add a `BreadthFirstTraversal` procedure and performs a breadth-first tree traversal from that root node, output symbols as it progresses.

Here is an algorithm for guidance:

- Create two lists of `Node` objects: one for the current level and one for the next level
- Handle empty trees to improve this method's robustness
 - Output a message
 - Return/Exit
- Initialise the list of nodes at this level with the root of the tree passed in
- While the list of nodes has not yet been encountered...
 - Form a new empty list for the next level's nodes
 - Visit all the nodes in the list
 - Output the value found at each node
 - If the node has a left/right node further down the tree, add it to the next level's list
 - Having visited all this level's nodes, set the next level's list to the current level's list

The `Main` procedure should be modified to test the procedure twice. First, test the `BreadthFirstTraversal` procedure using the `Root` value from before. Then, test it using a sorted array of integers. Each value should be displayed in the order in which it is encountered, and this should be manually checked for correctness.

```
>>>> BREADTH FIRST TRAVERSAL: GreekTree >>>>
1 > 2 > 3 > 4 > 5 > 6 > 7 > 10 > 14 > 15 >
>>>> BREADTH FIRST TRAVERSAL: AssortedTree >>>>
24 > 8 >
```

Program updated ☐

B

8

A special case of a binary tree is called a **BINARY SEARCH TREE**. It has the following properties:

- It is a binary tree.
- When any node is chosen, its left subtree contains only values less than the node's value.
- When any node is chosen, its right subtree contains only values greater than the node's value.

Modify the `Program` class by adding a recursive `CreateBinarySearchTree` method that takes in a sorted array of integers and create a binary search tree from it which returns the root node object (its root node). For robustness, any null or zero-length arrays should be handled. Here is an algorithm to guide the development process:

- Set up a method that returns a `Node` and takes in 3 parameters: the array of integers, the lower boundary and a pointer to the upper boundary of the array. This is to handle the recursive calls, hence the need for 3 parameters.
- If any of the following 3 cases arises, return `Null` immediately:
 - The array supplied is `Null` or `empty`
 - The array supplied has 0 values in it
 - The lower boundary is greater than the upper boundary
- Calculate and store the index of the midpoint of the array
- Determine the value held at the midpoint of the array
- Declare and initialise a new node using the value just found at the midpoint
- Set the left pointer of this new node by recursively calling the method on the left portion of the sorted array (by setting the parameters to describe the left of the mid-value)

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- Set the right pointer of this new node by recursively calling the portion of the sorted array (by setting the parameters to describe right of the mid-value)
- Return the newly created node

To make it easier to use this recursive method, overload the method to require the programmer to supply the low and upper boundaries with the Main method. This new method will then generate the relevant pointer defined method that was in (1) of either of the following two cases:

- The array supplied is a null pointer
- The array supplied has 0 values in it

The Main procedure should be modified to create the array Number {1, 2, 3, 4, 5, 6, 7, 8}. Construct a Tree object using this array and traversals on this tree.

Program updated ☐

B	9
---	---

Modify the program to add a SearchBST function in the Program class that takes a search tree's root node and an integer value as parameters. The method should traverse the relevant subtrees emanating from the root node until it can decide if the value is found or not found in the tree. It should return a single Boolean result.

Note: This method cannot be used with unsorted trees such as B-Trees.

Here is an algorithm to aid the development of this method:

- If the node is a null pointer, return False
- If the sought value is found at the node, return True
- If the sought value is less than the value found at that node, search by performing a recursive call
- If the sought value is greater than the value found at that node, search by performing a recursive call

The Main procedure should be modified to call the SearchBST function created from the list {1, 2, 3, 5, 6, 7, 8} to search for the values 6, 7, 8 and display the results. An example is shown below as a guideline only.

```
>>>> BST SEARCH: Does BST contain 6? It actually does
True

>>>> BST SEARCH: Does BST contain 7? It actually does
True

>>>> BST SEARCH: Does BST contain 8? It actually does
True

>>>> BST SEARCH: Does BST contain 9? It actually does
False

>>>> BST SEARCH: Does BST contain 0? It actually does
False
```

Program updated ☐

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B 10

Here are the lines of code required to traverse an unordered tree using an unsorted list of values found. Put the lines of code into the correct order in `Program.cs` as a new method.

A	<code>InOrderListBuilder(SubtreeRoot.GetLeft(), CurrentList)</code>
B	<code>}</code>
C	<code>return CurrentList;</code>
D	<code>public static List<int> InOrderListBuilder(Node SubtreeRoot, CurrentList)</code>
E	<code>InOrderListBuilder(SubtreeRoot.GetRight(), CurrentList)</code>
F	<code>}</code>
G	<code>{</code>
H	<code>if (SubtreeRoot != null)</code>
I	<code>{</code>
J	<code>CurrentList.Add(SubtreeRoot.GetValue());</code>

Now that a function exists that can convert an unordered tree into a list, create a `Sort()` method for sorting lists in C#.

The following method takes a list, sorts it and constructs a binary search tree. As before, convert an unordered binary tree into a binary search tree. As before, put the lines into the correct order, adding the method to `Program.cs` so that it

A	<code>// [2] Sort the list</code>
B	<code>return NewBST;</code>
C	<code>// [1] Turn the tree into a list using in-order traversal</code>
D	<code>ListFormat.Sort();</code>
E	<code>Node NewTreeRoot = ConstructBinarySearchTree(ListFormat)</code>
F	<code>{</code>
G	<code>ListFormat = InOrderListBuilder(RootOfUnsortedTree, ListFormat);</code>
H	<code>}</code>
I	<code>public static Tree ConvertToBST(Node RootOfUnsortedTree)</code>
J	<code>Tree NewBST = new Tree(NewTreeRoot);</code>
K	<code>List<int> ListFormat = new List<int>();</code>
L	<code>// [3] Convert it into a BST</code>

Program updated ☐

B 11

Modify the program by making a copy of the `BreadthFirstTraverse` method and add a new method `AddNode` in the `Program` class. This version of the method should take a `Node` as a parameter and add that node to that tree in the first available slot using a breadth-first approach. It should return a `Tree`.

The main program should be modified to add some randomly chosen nodes to the `AssortedTree` using this new method, and then create a copy of the `AssortedTree` using the `ConvertToBST` method. The new tree is called `AssortedBST`.

Finally, the program should perform all four traversals on the `AssortedBST`. It is apparent that performing in-order traversal on a BST produces a sorted list. Program updated ☐

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EXERCISE 7 — DIJKSTRA'S SHORTEST PATH

SECTION A

A 1

On how many lines of `Program.cs` are other classes' constructors called?

.....

A 2

Give a line number in `Graph.cs` that uses all three of the Boolean operators.

.....

A 3

The attributes in the `Graph` class are private.

Define what a public attribute is and explain why an attribute may be not.

.....

.....

.....

A 4

The code contains very few comments, and the purpose of some of the code may not be immediately clear to anyone who sees it.

Explain what is happening on `Program.cs` line 30.

.....

.....

.....

.....

.....

.....

.....

A 5

Explain what is happening on `Graph.cs` lines 16–19.

.....

.....

.....

.....

.....

.....

.....

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A 6

The 'closest node' is the node that you can advance to directly in one at. If a node is at a 'dead end' and no nodes emanate from it, there will be no next node. Using the comments given and by looking in detail at the lines of code for `GetClosestNode` in `Graph.cs` works.



A 7

Sketch a UML class diagram for `Edge.cs`.



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A 8

The program defines a graph data structure. A tree is a specific type of graph. Explain what a graph data structure is and what the features of a tree are.

.....

.....

.....

.....

A 9



Let's assume the `getNextNode` function can be used as part of an implementation of Dijkstra's shortest path algorithm.

State the purpose of Dijkstra's shortest path algorithm.

.....

.....

A 10

Describe how Dijkstra's shortest path algorithm works.

.....

.....

.....

.....



.....

.....

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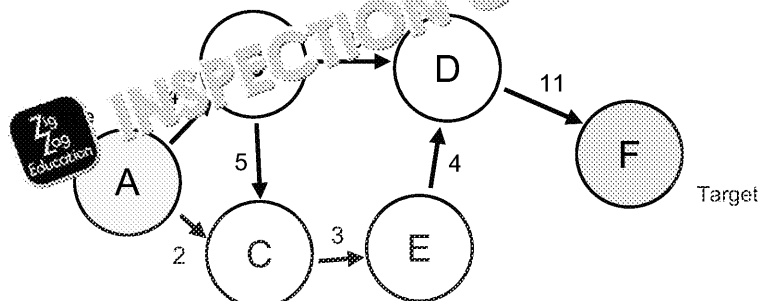


EXERCISE 7 — DIJKSTRA'S SHORTEST PATH

SECTION B

3 **1**

Modify the program by commenting out the existing graph creation replacing it with code which will model the graph shown here:



Program updated ☐

22

Modify the program so that when it is run, the graph above is visualised.

```

---- GRAPH ----
Source Node = A
Target Node = F
A ||| ----4----> B
A ||| ----2----> B
B ||| ----5----> D
C ||| ----3----> E
C ||| ----4----> D
D ||| ----11----> F

```

Program updated ☐

3

Modify the program to output the closest node that comes after each was used in the given code from Section A. This should expose a bug end' nodes, which have no nodes emanating from them. Diagnose the

To debug the problem, add a new private method to `Program.cs` called `InvestigateNode` which receives two parameters (the graph and the node being investigated) and prints out all the cases such as node F.

Finally, replace the code you have just added so that it uses the `Output` instead to output the closing tag for each node.

Program update

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B

4

When manually performing Dijkstra's shortest path algorithm, a table

- the name of each node
- whether that node has been visited (i.e. all edges emanating from that node)
- the length of the shortest known path from that node back to the start node
- the node that sits prior to that node along the shortest path

Before advancing to making further modifications to the program, try Dijkstra's algorithm on paper for both directed graphs shown previously.

Section A		
Node	Visited?	Shortest Distance to Start Node
A		0
B		∞
C		∞
D		∞
E		∞
F		∞
G		∞
H		∞
I		∞
Section B		
Node	Visited?	Shortest Distance to Start Node
A		0
B		∞
C		∞
D		∞
E		∞
F		∞

Section A: Shortest path from A to I = _____

Section B: Shortest path from A to F = _____

Modify the program to model the table structure as a list of objects in a class to perform Dijkstra's algorithm:

- 1) Build a new class called `TableRow` which contains four attributes corresponding to the four columns.
- 2) Add accessor and mutator methods for all four attributes in the `TableRow` class.
- 3) In the `Graph` class, add a new private instance method called `GetTable` which returns the current graph described by a blank table (the return type is a list of `TableRow` objects). It should be implemented by following the algorithm below:

- Create an empty list of nodes called `TableNodes`.
- Create a node variable called `NodeMaybeAdded` to temporarily hold nodes being considered for addition to the table.
- For all edges in the graph:
 - If the node at the start of that edge is not already in the table.
 - If the node at the end of that edge is not already in the table.
- Make a new empty list of `TableRow` objects.

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- For all nodes in `TableNodes`:
 - Create a new `TableRow` object by passing the node
 - Add it to the list of `TableRow` objects
 - If the node is also the `SourceNode` for this graph, so this, use the fact that it will currently be the last element added, and bear in mind that `SourceNode` is an object)
- Return the list of `TableRow` objects.

4) Add a new instance variable to `Graph.cs` called `DijkstraTable` of type `Table<Node, TableRow>`. Amend the existing constructors and the `PrintTable` method of each method, after something has changed it. Add a `PrintTable` method to update the instance variable `DijkstraTable`. Add an `AddEdge()` too so that the table version of the digraph is also updated. Finally, add a public accessor method to provide the `DijkstraTable` variable.

5) Add a public procedure called `PrintTable` to the `Graph` class. It should work robustly whether Dijkstra's algorithm is underway or is fully complete. This will involve watching out for `int.MaxValue` and unusual values (e.g. `int.MaxValue`) when outputting `PrintTable` using the following pseudocode, then add one test that it works:

- Output suitable table column headings and an overarching title
- For each row of the table:
 - If the row node is null, output an underscore; otherwise
 - Output "True"/"False" for whether the node has been visited
 - If the shortest distance is `int.MaxValue`, output "Infinite"
 - If the previous node is null, output the Null symbol
- Take a new line
- Output a footer of continuous equal signs to end the table

```
-----CURRENT TABLE-----
```

NODE	VISITED?	SHORTEST DISTANCE TO SOURCE
A	False	0
B	False	Infin.
C	False	Infin.
D	False	Infin.
E	False	Infin.
F	False	Infin.

```
=====
```

Program updated ☐

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B 5

When iteratively processing the table rows during Dijkstra's algorithm, the stopping condition is that when you look at all of the rows for unvisited target/destination node is the one with the minimum distance from the source node.

Modify the `Graph` class to add a public function called `TargetNode`. This function returns a Boolean value to indicate whether the target node is found.

Here is a pseudocode outline of how this should be implemented:

- Declare and initialise an integer variable called `MinimumDistanceInTable` (to hold the shortest distance to all unvisited nodes) in the table and set its value to the distance of the source node.
- Declare an integer variable called `CurrentDistance` for temporary value.
- Declare an integer variable called `NotedPositionNumber` to record where the `TargetNode` is found. Initialise this to -1 to help identify it.
- FOR all table rows in `DijkstraTable` (tip: use a FOR loop):
 - If it is an unvisited node:
 - Overwrite `CurrentDistance` with that node's current distance to the source node
 - If the `CurrentDistance < MinimumDistanceInTable`, then set `MinimumDistanceInTable` to hold the value of `CurrentDistance`.
 - If it is the target node:
 - Record the position in the list that you are currently processing.
- IF `NotedPositionNumber` is still -1, output an error message and return "False".
- ELSE IF the target node's shortest distance to the source/start node is equal to the `MinimumDistanceInTable` value, return "True".
- ELSE return "False".

Test the new method by adding the new code to `Program.cs` and modify the `Program.cs` so that the source and target nodes are the same.



B 6

Each time a new row of the table is to be inspected, it has to be chosen from the unvisited nodes. The row with the shortest distance value in column 3 is the next node to inspect. Modify the `Graph` class so that it has a new method called `GetNextUnvisitedNode()` which returns the node held at the table (the index will be zero-based) containing the unvisited node with the shortest distance value. If no unvisited node is found, return -1.

Here is some test code and the expected outcomes that can be used to verify the code.

`Program.cs` should have the following added to it:

```
// 86
Console.WriteLine("Next node to visit is " + Map.GetNextUnvisitedNode());
Map.GetDijkstraTable()[1].SetShortestDistanceToStart(2);
Map.GetDijkstraTable()[1].SetVisited();
Console.WriteLine("Next node to visit is " + Map.GetNextUnvisitedNode());
Map.GetDijkstraTable()[4].SetShortestDistanceToStart(5);
Map.GetDijkstraTable()[1].SetVisited();
Console.WriteLine("Next node to visit is " + Map.GetNextUnvisitedNode());
Map.PrintTable();
```

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Expected outcome:

```
Next node to visit is A
Next node to visit is B
Next node to visit is E

-----CURRENT TABLE-----
NODE      VISITED?      SHORTEST DISTANCE TO START
A          True          0
B          True          2
C          False         Infin.
D          False         Infin.
E          False          5
F          False         Infin.
```

Program updated ☐

B **7**

Modify the program by adding a method called `GetAllEmanatingNodes` in a node and consults the table and the diagram to identify any unvisited (i.e. come after) that node in the diagram.

It should return a list of suitable nodes.

This task can be achieved by looking for existing similar code in the

Immediately before the return statement, insert a block of code to obtain the nodes that are in the list that is about to be returned:

```
// B7 quick check:
Console.WriteLine("++++++ Checking the Get All Emanating Nodes");
foreach(Node N in TestList.Nodes)
{
    Console.WriteLine("NODE " + N.GetLetter());
}
```

Here is some test code that can thus be added to `Program.cs`, as well:

```
// B7
Map.GetDijkstraTable()[1].SetVisited(false);
List<Node> Tester = Map.GetAllEmanatingNodes(NodeB);
```

```
++++++ Checking the Get All Emanating Nodes
NODE C
NODE D
```

Notice that the 'visited' property of `NodeB` is set to `false` before testing for `true` for testing purposes.

Program updated ☐

B **8**

Modify the program by adding a `ConvertNodeToRowIndex` function that returns the row index where it exists in the `DijkstraTable` list.

Program updated ☐

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89

Modify the program by adding a `GetShortestPath` function that uses Dijkstra's algorithm to construct and output a table describing the shortest path from a given node of that digraph. (NB. The table will thus also describe the shortest path to the same starting node, but the algorithm will terminate based on the first shortest path found.) Here is the algorithm that should be implemented:

- **Declare the following 5 variables:**
 - A list of Node objects called *SourceNotVisited*
 - Integers called *NextStr*, *FromSource* and *TableRow*
 - Set *Table* $Table[11][11]$
 - A Node called *Current* which should be initialised by *getNextUnvisitedNode()* method
 - A Boolean called *TargetNodeNotVisited*, initialised to *True*

WHILE the target node doesn't hold the shortest distance AND

- `TableRowIndex =` the row index of `Current` (using an existing `Current` node)
 - IF `TableRowIndex == -1`, output an error string and return
 - Populate `StillNotVisited` by passing `Current` to an existing `PopulateStillNotVisited` function
 - Initialise a list of Edge objects called `RelevantEdges` by passing `Current` to an existing `GetRelevantEdges` function
 - FOREACH Edge in `Diagram`:
 - If `Current ==` the `StartNode` of that Edge: Add it to `RelevantEdges`
 - END OF FOREACH LOOP
 - Declare `int FirstLegShortDistance` and retrieve the distance from `Current` to the `StartNode` that `TableRowIndex` points to in the table, storing it here
 - Declare `int LastLegDistance` (to be initialised later)
 - Declare `int RowInTableGettingUpdated`
 - FOREACH Edge in `RelevantEdges`:
 - Obtain the `LastLegDistance` from the Edge
 - Update the value of `NewDistanceFromSource` to be `FirstLegShortDistance + LastLegDistance`
 - Use the `EndNode` of that Edge to work out the `RowInTableGettingUpdated` (call an existing `GetRowInTableGettingUpdated` function)
 - IF the distance in the table is larger than the new distance:
 - Update the distance in the table
 - Update the "previous node" column in the table
 - END OF FOREACH LOOP
 - Set the `Visited?` property of that row of the table to `True`
 - IF the `Current` node is actually the `TargetNode`, set `TargetFound` to `True`
 - Update `Current` to the closest node to `Current` (use an existing `GetClosestNode` function)
 - Print the table for testing purposes with some blank lines
- END OF WHILE LOOP
- RETURN "This table represents the shortest path ^^^^^^^^^"

Finally, update the `Program.cs` code to call the method as follows:

```
Console.WriteLine(Map.GetShortestPath());
```

```

=====
NODE      VISITED?      DISTANCE TO START NODE  PREVIOUS NODE
=====
A         True           0                       0
B         False          4                       A
C         False          2                       A
D         True           9                       E
E         True           5                       C
F         True          20                       D
=====
THIS TABLE REPRESENTS THE SHORTEST PATH

```

Program updated ☐

EXERCISE 8 — BOMB SEARCH

SECTION A

A 1

Which one of the three existing method stubs in `Board.cs` is suited

A 2

Give a class name and the number from the program where a constr



A 3

Explain the purpose of the code `Bombs = R*C / 3;` in the constr

A 4

Explain why the constructor in `Tile.cs` only takes one parameter wh
variables that have been initialised.



A 5

There is an extra, redundant method in `Tile.cs` called `Reveal()`.
Explain why it is convenient to include this method.

A 6

program could be crashed by passing negative numbers to the co
Name the type of exception that would be thrown in this case.



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A 7

The constructor of `Board.cs` could be made more robust by using a try-catch statement to handle the unusual event that negative numbers are passed in as parameters. Explain how try-catch statements work and how one can be useful in this context.



A 8

The `Arena` variable is an instance variable of the `Board` class. It is a `List<int>`. State the key difference between a list and an array.

A 9



Discuss whether or not it would be suitable to use a list instead of an array for the `Arena` variable.

A 10

The `Board` class stores the number of rows and columns integers for the board. Write a line of code that could be used to find the number of columns in the board.



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EXERCISE 8 — BOMB SEARCH

SECTION B

B 1

Modify the program to implement the `Explain` method of `Tile.cs` to output a description of a particular tile to the console.

Program updated ☐

B 2

Modify the `Tile.cs` class to include accessor and mutator methods for instance variables.

Program updated ☐

B 3

Modify the `SetUpBoard()` procedure to add tiles to the board. The tiles are added to random positions on the board. Here is an algorithm to guide the implementation.

- Build a list of Bomb tiles
- Build a list of Safe tiles
- Build an empty list of tiles to hold the newly shuffled list
- WHILE both lists contain elements:
 - Choose at random which list to remove a tile from: Bomb or Safe
 - Add the first tile from the chosen list to the shuffled list
 - Remove the first tile from the chosen list
- ENDWHILE
- Determine which list has still got elements in it and add the remaining tiles to the shuffled list
- Place the tiles from the shuffled list onto the board
- Amend each tile's adjacent 'bomb' value now that it is in place ← many!

Here is an algorithm to guide the implementation of the method for checking for bombs.

- Make the row and column position indices in as parameters
- Declare a counter variable to keep a running total of bombs found
- IF the row is not the top row, proceed to check the 3 squares above
- IF the row is not the bottom row, proceed to check the 3 squares below
- IF the tile isn't in the first column, proceed to check the square immediately to the left
- IF the tile isn't in the final column, proceed to check the square immediately to the right
- Return the total number of bombs found

Solving this part of the problem is faster if you understand 'short circuit' logical expressions, i.e. when you use a logical AND, the expression on the right is only evaluated if the expression on the left evaluates to False. Deploying this knowledge can save you a lot of time by ensuring that you aren't about to attempt to access an array index that is out of bounds.

Program updated ☐


B 4

Modify the `DisplayBoard` procedure so that the board is visualised as a grid of cells. The visualisation should show the row and column indices of each cell and there should be lines partitioning the rows and columns. Having just developed a method for setting up a board, it would be useful to be able to visually see the positions of the bombs and the numeric values of the cells. Modify the first set up. Any bombs should be displayed as B. Any revealed numeric values should be displayed as a single-digit numeric value.

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
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#	0	1	2	3	4	5	6
0	1	2	8	1	0	0	0
1	2	8	3	1	0	1	1
2	2	8	2	0	1	2	8
3	1	1	1	8	2	8	4
4	0			0	2	8	8

Running the program several times will always produce randomised results




#	0	1	2	3	4	5	6
0	0	0	0	1	8	8	8
1	1	1	1	2	3	5	8
2	1	8	1	1	8	3	2
3	1	1	1	1	1	2	8
4	0	0	0	0	0	1	1

You can also try with different dimensions of the game board in Program 1



#	0	1	2	3	4	5	6	7	8
0	0	1	1	2	8	1	1	1	1
1	0	2	8	3	1	1	2	8	2
2	1	3	8	2	0	0	3	8	3
3	8	4	4	3	1	0	3	8	3
4	2	8	8	8	2	2	5	8	3
5	1	3	8	3	2	8	8	8	2
6	0	1	1	1	1	3	8	3	1
7	0	0	0	0			1	1	0
8	0	0			0	0	0	0	0



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#	0	1	2	3	4	5	6
0	1	8	2	1	0	1	8
1	2	4	8	2	0	1	1
2	1	8	8	3	1	1	0
3	2	3	3	0	1	0	0
4	2	0	2	2	2	2	0
5	1	1	3	2	8	2	1
6	1	1	2	8	2	2	8
7	0	0	1	1	1	1	1

If you are not happy with how well-distributed the bombs are, the issue is randomisation was used. Try to vary the random number selection process.

Once this is proven to work, create a second copy of the method called `RevealBomb()` that it displays as a '?' character any tile that has not yet been revealed. A zero value should be blank, not zero-valued.

Add test code for both methods to `Program.cs`. Remember that you need to call `SetUpBoard()` first or there will be no tiles in each of the positions. Program updated ☐

B 5

Modify the `Program` to add code to the `GetMove()` method of the `Program` class to deal with incorrect data types being entered. It should return `False` if the input is not a valid integer. Program updated ☐

B 6

Modify the `Board` class to add a `Reveal()` function that gets a move (from the `GetMove` function) and reveals the chosen tile. The user's selection should be checked to ensure that the tile has not yet been revealed, and if it has, the function should return `False`. The function should output a "Game Over" message if a bomb has been revealed. Otherwise, it should simply return a `False` value. The main program procedure should be modified to continually call `RevealBomb()` until the result in a variable, and then display the game board. The result of `RevealBomb()` can be used to decide whether to continue iterating.

Program updated ☐

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B **7**

Modify the `Main` program to display a celebratory message followed by a message that the player has revealed every tile except those containing bombs. Add a `Board.cs` to store the number of safe (non-bomb) tiles that have already been revealed. Add a constructor and add suitable getter and setter methods.

Modify `Program.cs` so that it checks the number of safe tiles found and displays a message when the game is won.

For example, the result of winning would be:

```

=====
#      0      1      2      3
0      ?      2      1
1      2      ?      1
2      1      1      1      ?
=====

Enter the row number (0-2) of the tile you wish to reveal:
Enter the column number (0-3) of the tile you wish to reveal:

=====
#      0      1      2      3
0      ?      2      1
1      2      ?      1
2      1      1      1
=====

CONGRATULATIONS YOU HAVE WON!!!!
Number of bombs avoided: 2

=====
#      0      1      2      3
0      0      2      1      0
1      2      0      1      0
2      1      1      1      0
=====

The End.
  
```

Program updated ☐

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EXERCISE 9 — FILE HANDLING AND HASH TABLE

SECTION A

A 1

Give a line number from the program that contains a literal long value.

A 2

Give a line number from the program where an array of longs is declared.

A 3

Explain how the program ensures that the newly generated product of a single digit provided by the user.

A 4

The array could instead be implemented as a tuple. Describe what a tuple is.

A 5

Explain why you might choose to avoid tuples for representing products.

A 6

The program does not currently access the text file that stores multiple products. Name the class that is used to represent the text file as an object in a program.

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A 7

A list variable called `Table` is to be set up so that it can be used to store data. The data is to be populated with data held in the current text file.

Explain how data is stored in a hash table.



A 8

The unique product codes can be used as keys (inputs) for the hash function.

a) Explain what a hash function is.



b) Even when keys for data are unique it is often the case that hash values that have been generated before. Name this phenomenon and explain why the number of possible hash values is limited, even though this may lead to collisions.

A 9

Compare and contrast the use of a serial text file with the use of a sequential file.



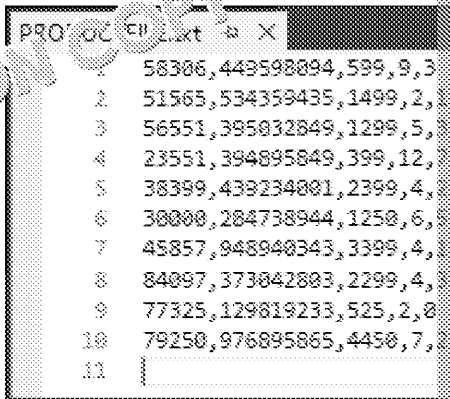
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A 10

The records of each product will be organised as a hash table using the formula $(\text{ProductCode} * (\text{ProductCode} + \text{ProductCode} / 29)) \% 29$... and then the resulting table will be stored as a new text file called PRODUCTFILE.txt.

Compute the contents of this hash table manually using the data from PRODUCTFILE.txt.



Line	Product Code
1	56386,443598894,599,9,3
2	51565,534359435,1499,2,
3	56551,395032849,1299,5,
4	23551,394895849,399,12,
5	36399,433234001,2399,4,
6	30000,284738944,1250,6,
7	45857,948940343,3399,4,
8	84097,373042803,2299,4,
9	77325,129819233,525,2,0
10	79250,976895865,4450,7,
11	

Hash Table Location	First Entry	Other
Table[0]		
Table[1]		
Table[2]		
Table[3]		
Table[4]		
Table[5]		
Table[6]		
Table[7]		
Table[8]		
Table[9]		
Table[10]		
Table[11]		
Table[12]		
Table[13]		
Table[14]		
Table[15]		
Table[16]		
Table[17]		
Table[18]		

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EXERCISE 9 — FILE HANDLING & HASH TABLES

SECTION B

B 1

Add a new text file to the project called HASHFILE.txt and leave it blank. Comment out all contents of Main() except Console.ReadKey() and open on the screen.

Program updated ☐

B 2



Add a private class method called GenerateHashValue which is a function that takes a string as a parameter and returns its hash value.

Program updated ☐

B 3

Add a line of code to the ShowFactFile() method so that the hash value is displayed at the end of the fact file when it is output.

Program updated ☐

B 4

Add a private class function called ReadInOldTextFile() which reads the contents of PRODUCTFILE.txt. Each line of the file should be transformed into an array of integers. The whole should be represented as a list of these arrays when it is returned. The hash value handling should be used as part of opening the file.

Program updated ☐

B 5

Add a private class procedure called ConvertArrayOfWholeTable to convert the arrays generated from the previous task's function ReadInOldTextFile() into a single string. Add code to the ShowFactFile() method to display it in full. Add code to the Main() method to test everything is working.



Program updated ☐

B 6

Add a function called InitiallyPopulateHashFile() which takes the contents of the old products file called PRODUCTSFILE.txt and returns a hash table. The hash table is a list of 19 lists of arrays, and the decision as to which array gets added to is determined by its hash value. Use the identifier returned by the function. Add code to the Main() method to call the function and store the result in a variable.

Program updated ☐

B 7

Add a procedure called WriteMigratedData() to write the current contents of HASHFILE.txt, separating the arrays from each other with the '>' character on the same line. The file will have 19 lines for storing data (one per list of arrays). Lines with no data should stay blank. The first few lines can be removed. The method (which currently opens the file in read mode and builds a hash table) can be replaced with a single call to InitiallyPopulateHashFile. A single call to InitiallyPopulateHashFile can be made from within the Main() method. Replace the existing method code with a call to this new method to test it. Finally, replace the existing method code with a call to this new method to test it. Finally, replace the existing method code with a call to this new method to test it. Finally, replace the existing method code with a call to this new method to test it.



Tip: While it is not essential, it is advisable to write a separate function called ConvertArrayToString() to reformat an array of long integers into a separated list.

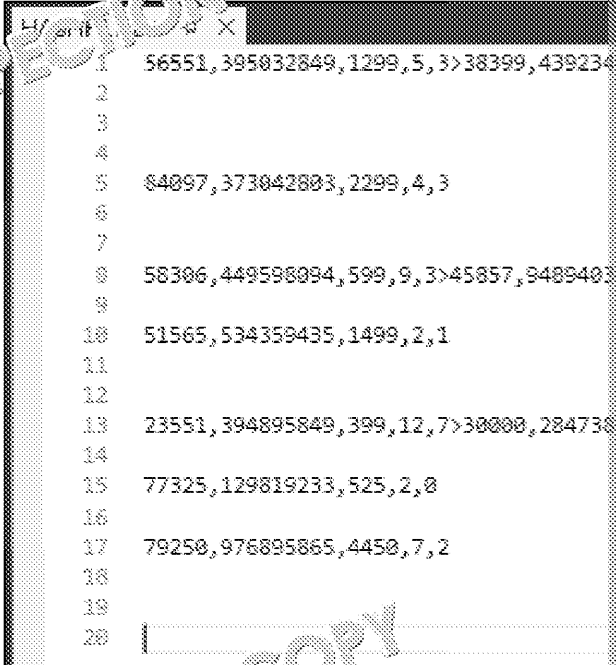
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It is intended that this method will be used only once as part of data copy and the new system, so once the file is successfully populated you can delete which accesses the old text file. Moving forward, the features that this program is solely around the ability to work with the new HASHFILE.txt file.

Note: In the diagram below, the line numbers are 1 higher than the hash table line numbering in Visual Studio and the hash value is not stored with the range from 0 to 19.



```

1 56551,395032849,1299,5,3>38399,439234
2
3
4
5 84097,373042803,2299,4,3
6
7
8 58306,449598094,599,9,3>45857,9485403
9
10 51565,534359435,1499,2,1
11
12
13 23551,394895849,399,12,7>30000,284730
14
15 77325,129819233,525,2,0
16
17 79250,976895865,4450,7,2
18
19
20

```

Program updated ☐

8



Create a second copy of the `WriteMigratedData()` called `UpdateHashFile()` as a parameter and overwrites the current text file with it. This should be the first few lines from this copy of the method and inserting a parameter.

Program updated ☐

9

Create a `ReadHashFile()` function which reads the entire contents of the hash table into the hash table format used previously: a list of lists of long integers. You can construct this function if you also construct a function called `ConvertHash` which can convert one product's details from a string representation to an array.

Program updated ☐

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EXERCISE 10 — REVERSE POLISH

SECTION A

A 1

Line 9 references the bitwise ^ operator, which is some other language. Explain what it achieves in C#.

A 2

Give a line number from the program that contains a class variable.

A 3

Explain how the IsInt function determines whether or not the given

A 4

Write the RPN form of the following infix expression: $(3 + 2) * (4 - 1)$

A 5

Write the infix form of the following RPN expression: $4\ 5\ +\ 3\ 2\ 1\ /\ -\ *$

A 6

A stack is a data structure that behaves like a list but with restrictions. Describe the main features of a stack.

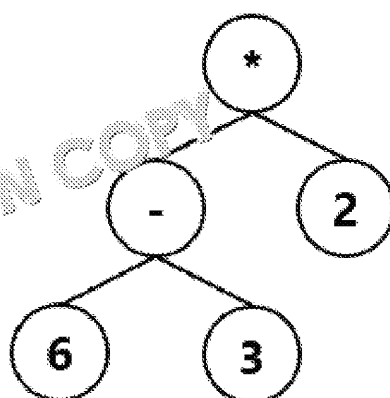
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A 7

Mathematical expressions can be represented as a binary tree, where a pre-order traversal will produce the RPN expression, and an in-order tree traversal will produce the infix expression. Write the RPN expression produced by the following binary tree:



A 8

Write the infix expression produced by the binary tree in A7.

A 9

Draw the binary tree that is created by the following infix expression:

A 10

Draw the binary tree that is created by the following RPN expression:

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EXERCISE 10 — REVERSE POLISH

SECTION B

B 1

Modify the `ConvertToPostfix` function so that it accepts a list of parameter and returns a list of strings

Program updated ☐

B 2

Modify the `ConvertToPostfix` function so that, at the very beginning, the variables are initialised: `Stack` and `OpStack`.

Program updated ☐

B 3

Modify the `ConvertToPostfix` function so that the major iterative part is controlled by a `FOREACH` loop that iterates through all items in the list parameter. Use the identifier `Item` when setting up the loop.

Program updated ☐

B 4

Modify the `ConvertToPostfix` function so that the first task carried out is a check to see whether the value of `Item` is an integer, and if it is, it is pushed to `Stack`. While `Stack` is technically a list and not formally defined as a stack to behave like a stack and so items pushed to it should be appended to the end position.

Program updated ☐

B 5

Modify the `ConvertToPostfix` function so that the `ELSE` block which begins with an inner `while` statement which checks that the `OpStack` is not empty, as long as it isn't empty, the variable `LastOp` should be set to store a copy of the value of the item at the top of the stack of operators (but it should not be removed from the stack!).

Program updated ☐

B 6

Modify the `ConvertToPostfix` function so that after the `IF` statement which checks for opening parentheses, there is a new and separate `IF-ELSEIF-ELSE` structure that implements the logic. The nested `IF` structure must also sit inside the same `ELSE` structure as the

If any of these 3 criteria is true, enter the IF block:

- 1. OpStack is empty*
- 2. Item is an opening parenthesis*
- 3. LastOp is either + or -, and at the same time, Item is either * or /*

ELSE IF Item is a closing parenthesis:

Set the value of Operator to null

WHILE Operator is not an opening parenthesis AND OpStack contains Operator

Pop the value of the top of OpStack and store it in the variable LastOp

IF Operator is not an opening parenthesis, push it to Stack

ELSE

Zig Zag Education

LastOp is not an opening parenthesis:

Push LastOp to Stack

Overwrite the top value of OpStack with Item

ELSE

Push Item on to OpStack

Program updated ☐

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B	7
---	---

Modify the `ConvertToPostfix` function so that after the `FOREACH` iterates from right to left through the `OpStack` list and successively:

- pushes each item to `Stack`
- pops each item from `OpStack` (without storing or inspecting)

Program updated ☐

B	8
---	---

Modify the `Main()` procedure so that it tests the working of the `ConvertToPostfix` function with valid strings.

Program updated ☐



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SUGGESTED SOLUTIONS & MARK SCHEME

Exercise 1 – Searching Algorithms

Section A

Section B

Exercise 2 – Sorting Algorithms

Section A

Section B

Exercise 3 – Towers of Hanoi

Section A

Section B

Exercise 4 – Sorting Queues

Section A

Section B

Exercise 5 – Draughts

Section A

Section B

Exercise 6 – Tree Traversal

Section A

Section B

Exercise 7 – Dijkstra's Shortest Path

Section A

Section B

Exercise 8 – Bomb Search

Section A

Section B

Exercise 9 – File Handling and Hash Tables

Section A

Section B

Exercise 10 – Reverse Polish

Section A

Section B

NB. When studying the suggested answers for Section B tasks, it is important to remember that there are often many different ways of achieving the same outcome, and credit should be given for alternative solutions.

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EXERCISE 1 – SEARCHING ALGORITHMS

SECTION A

■ A1

1 mark for giving a suitable example:

Line 7/8/9

■ A2

1 mark for giving a suitable example:

Line 20

■ A3

1 mark for explaining that binary search is more efficient / faster than linear search.

Binary search is usually more time-efficient (takes less time to run) than linear search.

■ A4

1 mark for explaining that binary search can be performed only on sorted lists:

The list might be unsorted – a binary search requires the list to be sorted.

■ A5

1 mark for explaining why it was used, not defining what it is:

It aided readability as it was obvious when it was used.

The same rogue value (-1) was used throughout the program.

There was no risk of accidentally overwriting it (i.e. no logic error was possible).

■ A6

1 mark for explaining the suitability:

Array indexing starts at 0, so -1 is an obviously invalid number.

■ A7

Up to 2 marks for explaining the reason why ELSE is optional; award 2 marks for clarity.

The linear search function will be exited when it hits the return statement within the IF block. If the Boolean expression evaluates to *False*, then the program advances immediately after the IF block anyway. Using ELSE is thus optional.

■ A8

2 marks (1 mark for explaining that time complexity describes number of operations; 1 mark for explaining how time complexity relates to varying input sizes):

The time complexity of an algorithm is a description of the number of operations it will complete in relation to the size of the input given to the algorithm.

■ A9

2 marks (1 mark for stating the time complexity of linear search; 1 mark for binary search):

Linear search has a time complexity of **O(n)**. Binary search has a time complexity of **O(log n)**.

■ A10

Up to 2 marks for explaining why recursion may not be suitable. For example:

Recursion may not be suitable for searching large arrays because each recursive call creates a new frame which includes a copy of the list (or part of the list), return addresses, and the variables to be used. This could lead to the computer running out of memory. In many languages, combinations have imposed recursion limits for this reason. As a result, recursive solutions are less time-efficient than iterative solutions.

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SECTION B

■ B1

1 mark available for providing this correction:

= should be replaced with == on Line 3

■ B2

1 mark available for modifying the code as shown (or equivalent code):

In linear search:

```

58         Console.WriteLine("The value " + searchVal + " was not found!");
59         return VALUE_NOT_FOUND;
60     }

```

In binary search:

```

72         Console.WriteLine("The value " + searchVal + " was not found!");
73         return VALUE_NOT_FOUND;
74     }

```

■ B3

1 mark available for modifying the code as shown (or equivalent code):

```

9         public static void Main(string[] args)
10        {
11            int soughtValue = getVal(); // B3 answer

```

■ B4

5 marks available for modifying the code as shown (or equivalent code):

Marks could be awarded for:

- creating a recursive `BinarySearch` function that takes an array, search value and start and end index (mid) when the element is found
- returning "VALUE_NOT_FOUND" if the element is not in the array
- recursively calling `recursiveBinarySearch` if another stage of searching is required
- modifying the main program procedure to display the result of recursive search

```

77     private static int recursiveBinarySearch(int[] searchList, int start, int end)
78     {
79         int mid;
80
81         while (start <= end)
82         {
83             mid = (start + end) / 2;
84
85             if (searchList[mid] == searchVal)
86             {
87                 return mid;
88             }
89             else if (searchList[mid] < searchVal)
90             {
91                 return recursiveBinarySearch(searchList, searchVal, mid + 1, end);
92             }
93             else if (searchList[mid] > searchVal)
94             {
95                 return recursiveBinarySearch(searchList, start, mid - 1);
96             }
97         }
98         Console.WriteLine("The value was not found!");
99         return VALUE_NOT_FOUND;
100     }

```

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In the main program:

```
16 // B4 answer part 2 of 2:
17 Console.WriteLine("RECURSIVE BINARY TEST (-5): " + B4);
18 Console.WriteLine("RECURSIVE BINARY TEST ( 1): " + B4);
19 Console.WriteLine("RECURSIVE BINARY TEST ( 0): " + B4);
20 Console.WriteLine("RECURSIVE BINARY TEST (10): " + B4);
21 Console.WriteLine("RECURSIVE BINARY TEST (11): " + B4);
```

■ B5

4 marks available for modifying the code as shown (or equivalent code):

Marks could be awarded for:

- creating a `getVal` function that repeats until a valid input is given
- handling (but not accepting) invalid input
- using appropriate messages
- returning the resulting value as an integer
- modifying the main program procedure to use `getVal` to set the value of `soughtValue`

```
// B5 answer part 1 of 2:
private static int getVal()
{
    Console.Write("Enter an integer value to search for: ");
    string userInput = Console.ReadLine();
    int userValue = 0;
    bool successful = false;

    do
    {
        try
        {
            userValue = int.Parse(userInput);
            successful = true;
        }
        catch (Exception e)
        {
            Console.WriteLine("NOT AN INTEGER! TRY AGAIN...\nEnter an integer value: ");
            userInput = Console.ReadLine();
        }
    } while (!successful);

    return userValue;
}
```

In the main program:

```
10 {
11     int soughtValue = getVal(); // B3 answer
12     // B3 answer: Console.WriteLine("The value of soughtValue is: " + soughtValue);
```

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■ B6

2 marks available for modifying the code as shown (or equivalent code):

Marks could be awarded for:

- creating a `generateList` function that correctly generates and returns length
- modifying the main program procedure to use `generateList` to create

```

127 // B6 answer part 1
128 private static int[] generateList(int size)
129 {
130     int[] orderedList = new int[size];
131
132     for(int count=0; count<size; count++)
133     {
134         orderedList[count] = count+1;
135     }
136     return orderedList;
137 }

```

In the main program:

```

12 int[] searchList = generateList(25); //

```

■ B7

5 marks available for modifying the code as shown (or equivalent code):

Marks could be awarded for:

- correctly counting and returning the number of steps made by the linear search
- correctly counting and returning the number of steps made by the binary search
- creating a test function that returns the average number of operations for a given length
- modifying the main program to use `test` to perform 1,000 tests on lists of length 10 and 100
- modifying the main program to display how many more operations linear search takes than binary search for each of the list lengths tests

```

140 private static int timedBinarySearch(int[] searchList)
141 {
142     int start = 0;
143     int end = searchList.Length - 1;
144     int mid;
145     int count = 0; // B7 answer part 5
146
147     while (start <= end)
148     {
149         mid = (start + end) / 2;
150
151         count++; // B7 answer part 6
152
153         if (searchList[mid] == searchVal)
154         {
155             return count; // B7 answer part 7
156         }
157         else if (searchList[mid] < searchVal)
158         {
159             start = mid + 1;
160         }
161     }

```

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```

161         else
162         {
163             end = mid - 1;
164         }
165     }
166     Console.WriteLine("The value " + searchVal + "
167     return count; // B7 answer part 3
168 }

```

```

170 // B7:
171 private static int timedLinearSearch(int[] searchList,
172 int searchVal)
173 {
174     int count = 0; // B7 answer part 1
175     for (int i = 0; i < searchList.Length; i++)
176     {
177         count++; // B7 answer part 2
178         if (searchList[i] == searchVal)
179         {
180             return count; // B7 answer part 3
181         }
182     }
183     Console.WriteLine("The value " + searchVal + "
184     return count; // B7 answer part 4
185 }

```

```

186 // B7:
187 private static double testLinearTimings(int n, int tests)
188 {
189     int totalTimeTaken = 0;
190     int[] arrayToTest = generateList(n);
191
192     for (int testNumber = 1; testNumber <= tests; testNumber++)
193     {
194         totalTimeTaken += timedLinearSearch(arrayToTest, searchVal);
195     }
196
197     return (double) totalTimeTaken / tests; // AVERAGE
198 }

```

```

200 // B7:
201 private static double testBinaryTimings(int n, int tests)
202 {
203     int totalTimeTaken = 0;
204     int[] arrayToTest = generateList(n);
205
206     for (int testNumber = 1; testNumber <= tests; testNumber++)
207     {
208         totalTimeTaken += timedBinarySearch(arrayToTest, searchVal);
209     }
210
211     return (double) totalTimeTaken / tests; // AVERAGE
212 }

```

In the main program:

```

23 // Main program
24 Console.WriteLine("Test LINEAR timings (10 elements, 10 tests): " + testLinearTimings(10, 10));
25 Console.WriteLine("Test BINARY timings (10 elements, 10 tests): " + testBinaryTimings(10, 10));
26 Console.WriteLine("Test LINEAR timings (100 elements, 100 tests): " + testLinearTimings(100, 100));
27 Console.WriteLine("Test BINARY timings (100 elements, 100 tests): " + testBinaryTimings(100, 100));
28 Console.WriteLine("Test LINEAR timings (1,000 elements, 1,000 tests): " + testLinearTimings(1000, 1000));
29 Console.WriteLine("Test BINARY timings (1,000 elements, 1,000 tests): " + testBinaryTimings(1000, 1000));
30 Console.WriteLine("Test LINEAR timings (10,000 elements, 10,000 tests): " + testLinearTimings(10000, 10000));
31 Console.WriteLine("Test BINARY timings (10,000 elements, 10,000 tests): " + testBinaryTimings(10000, 10000));

```

EXERCISE 2 – SORTING ALGORITHMS

SECTION A

■ A1

1 mark for giving a suitable example:

They are accepted in string format... [1]

... then the string is parsed to read its value in as an integer... [1]

■ A2

1 mark:

Line 66

■ A3

1 mark for a suitable definition:

Recursion is when a subroutine is defined in terms of itself or calls itself.

■ A4

2 marks for any two of these points:

\t is an escape sequence.

In this case it represents the Tab character.

It is used here so that lists get output with their values all starting at a new tab stop in a human-friendly format, horizontally across the screen without overlapping.

■ A5

Any 2 marks drawn from any of the following points:

When its value eventually gets set to *True*...

... this represents the event where an entire pass has been made through the array

... and when this occurs, the sorting can be repeated immediately...

... as the array is sorted.

This improves the overall efficiency of the algorithm in cases where it would be the array check values that are in order.

■ A6

2 marks for any two of these ideas:

During bubble sort, the index of the value on the left is indicated by the pointer.

The value to the right of the pointer is thus compared with the value at the pointer.

A pointer value of `SIZE-1` would point at the last element in the array due to the use of arrays.

If the pointer were permitted to point at the last element, it would attempt to compare immediately to its right.

This would be an 'array out of bounds' exception / a logic error / a run-time error.

■ A7

3 marks (1 mark for explaining `DIV`; 1 mark for explaining the impact on BOTH arrays)

The `DIV` operation takes the odd length and divides it by two, discarding the remainder. This means that the new left array would contain only six elements.

The right array will have the remaining elements, calculated from the original array length, so the middle element always ends up occurring as the first element of the right array. This means that the middle element always ends up occurring as the first element of the right array.

■ A8

2 marks (1 mark for explaining that divide-and-conquer algorithms break a problem into smaller problems (divide); 1 mark for explaining that these problems can then be further divided until they are solved (conquer)):

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A divide-and-conquer algorithm is an algorithm that breaks down a problem into a smaller problem that can be individually solved and then recombined to solve the original problem.

■ A9

2 marks (1 mark for giving the time complexity of a bubble sort; 1 mark for giving the time complexity of a merge sort). Bubble sort has a time complexity of $O(n^2)$. Merge sort has a time complexity of $O(n \log n)$.

■ A10

2 marks (1 mark for describing how an insertion sort uses a sorted list and an unsorted list; 1 mark for describing how each element in the unsorted list is placed into the correct position in the sorted list).

An insertion sort creates an empty sorted list and an unsorted list. Each element of the unsorted list is placed into the sorted list until the unsorted list is empty and all the numbers are in the correct order. The sorted list is then the new sorted list.

SECTION B

■ B1

1 mark available for modifying the code as shown:

```
7 private const int SIZE = 12; // B1: Convert from 9 to 12
```

■ B2

1 mark available for modifying the code as shown (or equivalent code):

Main method (1 mark):

```
15 Console.WriteLine("\nOnly 10 values given. Please use the new method.");
16 printArray(numList); // B2: Using the new method
```

printArray method (2 marks):

```
195 // B2: Procedure for printing the whole array
196 private static void printArray(int[] list)
197 {
198     for (int i = 0; i < list.Length; i++)
199     {
200         Console.Write("\t" + list[i]);
201     }
202     Console.WriteLine();
203 }
204
```

Bubble sort method (1 mark):

```
55 // B2: Output the array
56 printArray(sortlist);
57 Console.WriteLine("SWAPS MADE ON THIS PASS: " + swaps);
58 swaps = 0;
59 }
60 return sortlist;
61 }
62
```

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■ B3

1 mark deducted per earmarked part missing or improperly used:

```

33 public static int[] bubbleSort(int[] sortList)
34 {
35     bool sorted = false;
36     // int temp = 0; // Removed in B7
37     int endPoint = SIZE - 1; // B3
38     int swaps = 0;
39
40     while (!sorted)
41     {
42         sorted = true;
43         for (int i = 0; i < endPoint; i++) // B3
44         {
45             if (sortList[i] > sortList[i + 1])
46             {
47                 sortList = Swap(sortList, i); //
48                 swaps++;
49                 sorted = false;
50             }
51         }
52         endPoint--; // B3
53     }

```

■ B4

4 marks available for modifying the code as shown (or equivalent code):

Marks could be awarded for:

- setting up a loop that ends only once enough inputs are given
- successfully adding valid values to the array at the right location
- displaying a clear error message if invalid input is given
- correctly allowing re-try of an attempt

```

218 // B4: Adding robustness
219 do
220 {
221     Console.Write("Add an integer number to the list: ");
222     try
223     {
224         listToPopulate[numbersObtained] = int.Parse(Console.ReadLine());
225         numbersObtained++;
226     }
227     catch (FormatException ex)
228     {
229         Console.WriteLine("That was not an integer");
230     }
231 } while (numbersObtained < SIZE);

```

■ B5

4 marks available for modifying the code as shown (or equivalent code):

Marks could be awarded for:

- creating a `getList` function that returns a list
- using a `while` loop followed by a selection structure (or equivalent) to continue until a valid rank is given
- using try-except structure to detect invalid input and having an appropriate message and another value to be added under these circumstances
- modifying the main program procedure to use the `getList` function appropriately

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```

207 // B5: Improving reusability
208 private static int[] GetList(int[] listToPopulate)
209 {
210     // B6 - Mode 1 - One at a time
211     int numbersObtained = 0;
212
213     // B4: Adding robustness
214     do
215     {
216         Console.Write("Add an integer number to the list: ");
217         try
218         {
219             listToPopulate[numbersObtained] = int.Parse(Console.ReadLine());
220             numbersObtained++;
221         }
222         catch (FormatException fex)
223         {
224             Console.WriteLine("That was not an integer; please try again.");
225         }
226     } while (numbersObtained < SIZE);
227
228     return listToPopulate; // B5
229 }

```

■ B6

7 marks available for modifying the code as shown (or equivalent code):

Marks could be awarded for:

- [1] reading in the user's preferred mode of entry
- [1] identifying if they have chosen option #1
- [1] embedding previously written code successfully into the new selection
- [1] making it clear to the user how to format their comma-separated list
- [1] separating the list into values
- [1] adding the values correctly to the list
- [1] returning the comma-separated list as an array

```

207 // B5: Improving reusability
208 private static int[] GetList(int[] listToPopulate)
209 {
210     // B6: Two modes of operation
211     Console.WriteLine("Would you like to provide the list of values one at a time? Key in Y or N");
212     string userChoice = Console.ReadLine();
213
214     if (userChoice.ToUpper()[0] == 'Y')
215     { // B6 - Mode 1 - One at a time
216         int numbersObtained = 0;
217
218         // B4: Adding robustness
219         do
220         {
221             Console.Write("Add an integer number to the list: ");
222             try
223             {
224                 listToPopulate[numbersObtained] = int.Parse(Console.ReadLine());
225                 numbersObtained++;
226             }
227             catch (FormatException fex)
228             {
229                 Console.WriteLine("That was not an integer; please try again.");
230             }
231         } while (numbersObtained < SIZE);
232
233         return listToPopulate; // B5
234     }
235     else

```

```

236     { // B6 - Mode 2 - Comma separated list
237         Console.WriteLine("Please key in your list of +SIZE+ integers in the following format, where N = +SIZE+");
238         string commaSeparatedList = Console.ReadLine();
239         string[] commaSeparatedStrings = commaSeparatedList.Split(',');
240         for (p=0; p<SIZE; p++)
241         {
242             listToPopulate[p] = int.Parse(commaSeparatedStrings[p]);
243         }
244         return listToPopulate;
245     }
246 }

```

■ B7

2 marks (as shown below, or equivalent code):

```

249 // B7 - Swapping
250 private static int[] Swap(int[] fulllist, int pointer)
251 {
252     int temp = fulllist[pointer];
253     fulllist[pointer] = fulllist[pointer + 1];
254     fulllist[pointer + 1] = temp;
255
256     return fulllist;
257

```

1 mark (calling Swap correctly from within the bubble sort method):

```

42 sorted = true;
43 for (int i = 0; i < endPoint; i++) // B3
44 {
45     if (sortlist[i] > sortlist[i + 1])
46     {
47         sortlist = Swap(sortlist, i); // B7
48         swaps++;
49         sorted = false;

```

■ B8

6 marks for overall quality:

Award marks as follows:

- [0] for minimal commenting
- [2] for clear comments but not many of them
- [4] for medium-level volumes of comments or inaccurate/wasteful comments
- [6] for excellent comments that clearly aid maintainability and readability

```

109 // B8 - Merging
110
111 * This function takes 2 arrays of integers that are both pre-sorted
112 * It merges them into a single sorted array.
113 * int[] leftArray = 1st sorted array, due to be merged
114 * int[] rightArray = 2nd sorted array, due to be merged
115 */
116
117 public static int[] merge(int[] leftArray, int[] rightArray)
118 {
119     // Store the lengths of both arrays to aid iteration later
120     int leftLength = leftArray.Length;
121     int rightLength = rightArray.Length;
122     // Calculate the length of the new, merged array and initialise it
123     int[] entireList = new int[leftLength + rightLength];
124
125     // Merging can be accelerated when it is known that 1 array
126     // All that remains is to copy values of the other array
127     // These variables signal when the end of an array has been reached
128     bool endOfLeftArrayReached = false;
129     bool endOfRightArrayReached = false;
130
131     int leftPointer = 0; // belongs to left/1st array
132     int rightPointer = 0; // belongs to right/2nd array
133     int entireListPointer = 0; // Keep track of position in the
134

```

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```

136 // Whilst both the left and right arrays have more elements to
137 while (!endOfAnArrayReached)
138 {
139     // Decide which array contains the next element to be added
140     if (leftArray[leftPointer] < rightArray[rightPointer])
141     {
142         entireList[entireListPointer] = leftArray[leftPointer];
143         entireListPointer++; // Advance the larger array's pointer
144         leftPointer++; // Advance the smaller array's pointer
145
146         // Determine if that was the last element in the smaller array
147         if (leftPointer >= leftlength)
148         {
149             endOfLeftArrayReached = true;
150         }
151     }
152     else
153     {
154         entireList[entireListPointer] = rightArray[rightPointer];
155         entireListPointer++; // Advance the larger array's pointer
156         rightPointer++; // Advance the smaller array's pointer
157
158         // Determine if that was the last element in the smaller array
159         if (rightPointer >= rightlength)
160         {
161             endOfRightArrayReached = true;
162         }
163     }

```

```

165 // Update the flag which indicates that one array has been exhausted
166 // This controls this loop
167 endOfAnArrayReached = endOfLeftArrayReached || endOfRightArrayReached;
168 }
169
170 // One of the 2 smaller arrays has been fully exhausted,
171 // so this block will copy across all values of the other array
172 // without further checks on the relative size of its elements
173 if (endOfLeftArrayReached)
174 {
175     while (leftPointer < leftlength) // Whilst more values remain
176     {
177         entireList[entireListPointer] = leftArray[leftPointer];
178         entireListPointer++; // for tracking where to write data
179         leftPointer++; // for continuously advancing through array
180     }
181 }
182 else
183 {
184     while (rightPointer < rightlength) // Whilst more values remain
185     {
186         entireList[entireListPointer] = rightArray[rightPointer];
187         entireListPointer++; // for tracking where to write data
188         rightPointer++; // for continuously advancing through array
189     }
190 }
191
192 return entireList; // Return the newly merged, single array of elements
193 }

```

■ B9

4 marks available for modifying the code as described:

Marks could be awarded for the swaps variable being:

- correctly created as a local variable
- correctly
- correctly changed during iterations
- output within a meaningful statement

```

32 // B3 - Modified to display swaps per pass
33 public static int[] B1q1Sort(int[] sortlist)
34 {
35     bool sorted = false;
36     // int temp = 0; // Removed in B7
37     int endPoint = SIZE - 1; // B3
38     int swaps = 0; // B9
39
40     while (!sorted)
41     {
42         sorted = true;
43         for (int i = 0; i < endPoint; i++) // B3
44         {
45             if (sortlist[i] > sortlist[i + 1])
46             {
47                 sortlist = Swap(sortlist, i); // B7
48                 swaps++; // B9
49                 sorted = false;
50             }
51         }
52
53         endPoint--; // B3
54
55         // B2: Output array
56         printArray(sortlist);
57         Console.WriteLine("SWAPS MADE ON THIS PASS: " + swaps);
58         swaps = 0;
59     }
60     return sortlist;
61 }

```

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EXERCISE 3 – TOWERS OF HANOI

SECTION A

■ A1

1 mark:

Line 9

■ A2

1 mark:

40%

■ A3

3 marks (1 mark for identifying data structure as a stack; 1 mark for describing a stack; 1 mark for describing what it means for a data structure to be FILO):

This behaviour is represented by a stack data structure.

A stack is a First-In, Last-Out (FILO) data structure (can also say LIFO), meaning that only the most recently stored data can be accessed.

■ A4

1 mark per relevant point in the explanation (up to 3):

This is achieved through the use of multiple constructors.

All three require a constructor to build a new object, but by default any newly built integers, as well as a tower number.

It is only Tower #1 that needs further information, so it is built using a different constructor. This is possible in OOP thanks to method overloading.

■ A5

1 mark for each part of the explanation (up to 3):

This would lead to a string being parsed which cannot be turned into digits...

... resulting in an exception being thrown,

... specifically a `FormatException`,

... which would crash the program as no exception handling has been built in.

■ A6

2 marks for quoting code and giving an explanation in prose; limit to 1 if no reference to code

Line 45 solves this:

```
if (StartTower.CheckTower().Count != 0)
```

...and the corresponding ELSE block on Line 64 absorbs the cases where there are no discs

```
else
```

```
{
```

```
    Console.WriteLine("Invalid move: There are no discs on the tower");
```

```
}
```

■ A7

3 marks for communicating the need for an OR is needed to avoid an exception being thrown

If the tower is EMPTY

... or if the value being added to it is smaller than the current top of the tower...

... then proceed with the move.

This is required to implement the key rule of the Towers of Hanoi.

The first part of the OR is required because no index notation can be used to read the tower is EMPTY, the OR expression 'short circuits' and the part on the right is never TRUE.

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■ A8

4 marks (1 mark for explaining that the value of the top disc is returned; 1 mark for removed from the tower; 1 mark for explaining that -1 refers to the right of the list, 1 mark for perfect accuracy of explanation, with no ambiguity):

```

33     public int RemoveDisc()
34     {
35         int TopOfThisTowerWas = Discs[Discs.Count-1];
36         Discs.Remove(Discs.Count-1);
37         return TopOfThisTowerWas;
28     }

```

The code on line 37 on the above screenshot of the program is used to return the value of the top disc. The code on line 36 removes that disc from the tower... using the top of the stack as a pointer, generated from the size of the stack but... The index value of -1 is used to remove the rightmost element of the list, which is the right-hand side being the top of the stack (or tower).

■ A9

Up to 2 marks:

Encapsulation means grouping together related data and subroutines and controlling access to them by which parts of the program by hiding the details of implementation. Encapsulation allows code to be modified without affecting the entire program, as the implementation of methods can change without changing how the methods are used.

■ A10

Up to 3 marks for full explanation; limit to 2 if the word 'mutability' is not used:

- [0] Arrays & lists use numeric indexes.
- [0] Arrays & lists hold values with compatible/matching/same data types.
- [1] Arrays have an immutable size BUT...
- [1] ... lists can grow and shrink.

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SECTION B

■ B1

1 mark available for modifying the code as shown (or equivalent code):

```
9 // B1
10 Console.WriteLine("////////////////////////////////// Welcome to //////////////////////////////////");
11 Console.WriteLine("////////////////////////////////// TOWERS OF HANOI //////////////////////////////////");
12
```

■ B2

1 mark available for:

- meaningful prompt to the user
- try-catch but using try-catch OR alternative approach, e.g. looking for
- copy inputs given in upper case / lower case
- successful conversion from words to numbers
- robust defence against invalid inputs
- replicating the work for both inputs

```
72 public void GetMove()
73 {
74     // B2
75     Console.Write("Which tower would you like to remove a disc from? ");
76     String chosenFromT = Console.ReadLine();
77     int startTower = -1;
78     try
79     {
80         startTower = int.Parse(chosenFromT);
81     }
82     catch (FormatException fex)
83     {
84         chosenFromT = chosenFromT.ToUpper();
85         switch (chosenFromT)
86         {
87             case "ONE":
88                 startTower = 1; break;
89             case "TWO":
90                 startTower = 2; break;
91             case "THREE":
92                 startTower = 3; break;
93             default:
94                 Console.WriteLine("Invalid from tower chosen.");
95                 break;
96         }
97     }
98     Console.WriteLine();
99
```

```
101 Console.Write("Which tower would you like to move this disc to? ");
102 String chosenToT = Console.ReadLine();
103 int endTower = -1;
104 try
105 {
106     endTower = int.Parse(chosenToT);
107 }
108 catch (FormatException fex)
109 {
110     chosenToT = chosenToT.ToUpper();
111     switch (chosenToT)
112     {
113         case "ONE":
114             endTower = 1; break;
115         case "TWO":
116             endTower = 2; break;
117         case "THREE":
118             endTower = 3; break;
119         default:
120             Console.WriteLine("Invalid end tower chosen.");
121             break;
122     }
123 }
```

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■ B3

1 mark available from each method (getter/accessor and setter/mutator):

Private visibility [0 marks in itself]:

```
8 // Attributes
9 private int Number;
10 private List<int> DiscArrangement;
```

Methods required [1 mark each]:

```
46 // B3
47 public int GetTowerNumber()
48 {
49     return Number;
50 }
51
52
53 public void SetTowerNumber(int NewNumber)
54 {
55     Number = NewNumber;
56 }
```

For example, in Game .cs it has been used [1 mark]:

```
54 EndTower.AddDisc(valueBeingMoved);
55 Console.WriteLine("Disc moved successfully to Tower");
56 movesCount++;
```

■ B4

4 marks available for developing the method, +1 mark for calling it:

```
131 // B4
132 public void ShowBoard()
133 {
134     List<int> discArrangement;
135
136     int pole=0; pole<GameBoard.Count; pole++)
137     {
138         discArrangement = GameBoard[pole].CheckTower();
139
140         Console.Write("TOWER #" + (pole+1) + " >>\n");
141         for(int d=0; d< discArrangement.Count; d++)
142         {
143             Console.Write("\t" + discArrangement[d]);
144         }
145         Console.WriteLine();
146     }
147 }
```

Method call in Program.cs:

```
37 while (!PlayGame.CheckWin())
38 {
39     PlayGame.GetMove();
40     PlayGame.ShowBoard();
41 }
```

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■ B5

4 marks available for:

- checking if the game has been won (all discs on Peg #3 OR both other pegs)
- returning a suitable value (MUST be Boolean)
- calling the method iteratively using NOT
- suitable messages in Program.cs

```

151         // B5
152         public bool CheckWon()
153         {
154             return gameBoard[0].CheckTower().Count == 0
155                 && gameBoard[1].CheckTower().Count == 0;
156         }

```

In the Main method:

```

37         while (!PlayGame.CheckWon())
38         {
39             PlayGame.GetMove();
40             PlayGame.ShowBoard();
41         }
42
43         Console.WriteLine("##### You have won!! Well done!");

```

■ B6

6 marks available for reading in the number of discs and validating it, then proceeding

Marks could be awarded EARLY in Program.cs for validation [2] and outputs [2]

Marks can be awarded LATER in Program.cs for reporting to how many moves

In Program.cs:

```

13
14         int DiscsToUse = -1;
15
16         // B6
17         do
18         {
19             Console.Write("How many discs would you like to use to play? Check
20             try
21             {
22                 DiscsToUse = int.Parse(Console.ReadLine());
23             }
24             catch (FormatException ForExg)
25             {
26                 Console.WriteLine("INVALID - Please only enter positive number
27             }
28         } while (DiscsToUse < 1 || DiscsToUse > 12);
29
30         // B6
31         int minimumMoves = (int) (Math.Pow(2, DiscsToUse) - 1);
32         Console.WriteLine("THIS GAME CAN BE SUCCESSFULLY COMPLETED IN " + minimumMoves);
33
34
35         Game PlayGame = new Game("Hi - you are playing the game of the Tower of Hanoi");
36
37         while (!PlayGame.GameOver())
38         {
39
40             // B6
41             if (PlayGame.getMovesCount() <= minimumMoves)
42             {
43                 Console.WriteLine("Congratulations on completing the game in the minimum number of moves!");
44             }
45             else
46             {
47                 Console.WriteLine("It is still possible to complete the game in fewer moves than you have taken!");
48             }
49         }

```

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EXERCISE 4 – SORTING QUEUES

SECTION A

■ A1

1 mark for saying three members:

3 members = 2 attributes + 1 method

■ A2

1 mark for anywhere that uses parameter passing:

Line 15/42/47/53

■ A3

2 marks (1 mark for explaining that a queue is FIFO (First-In, First-Out); 1 mark for explaining that a stack is LIFO (First-In, Last-Out)):

The first element placed into a queue is the first element to be removed from the queue. The last element placed into a stack is the last element to be removed from the stack.

■ A4

1 mark for explaining the cause of the error:

Data values can join a queue only at the tail of the queue. This method must be able to add a new item to the queue and enqueue subsequent data values there.

■ A5

1 mark for explaining that it outputs a useful/meaningful number of hyphens:

Earlier in the program a series of hyphens was used to denote a heading. The FOR loop is used to produce a sequence of hyphens such that the sequence has the same length as the heading text (which contained hyphens as well as the heading itself).

■ A6

1 mark for explaining why:

A newly created node has no successor (node that comes after it) in the queue, so its pointer to the next object and its pointer to the next node takes the value Null.

■ A7

3 marks (1 mark for explaining that an array cannot change its size at run-time; 1 mark for explaining that a list can change its size while running to match the number of elements needed; 1 mark for explaining the advantage over fixed-length arrays):

A fixed-length array has to declare the number of memory locations it will use, and this is fixed. A list has a dynamic size, so it doesn't take up more memory than it needs. This makes it more efficient than if they used arrays instead. Array immutability is thus a barrier here.

■ A8

1 mark for explaining how pointers need to be updated:

The current node at the tail of the queue needs to be updated by traversing all pointers. The new node must have been instantiated. The tail node's pointer needs to point to the newly added node.

■ A9

3 marks (1 mark for explaining that a circular queue has a fixed size; 1 mark for explaining how start and end pointers work; 1 mark for explaining that elements are placed at the front of the queue and removed at the rear of the queue):

A circular queue is a queue of a fixed length that uses start and end pointers to point to the first and last elements. If there is no space at the back of a circular queue, but there is still space at the front, new elements are added to the front of the queue, and the end pointer is moved to the front.

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■ A10

2 marks (1 mark for identifying that the queue is a dynamic queue (no fixed length) detect whether it is circular or dynamic):

The queue in the program is dynamic (not circular) because it has no end pointer

SECTION B

■ B1

1 mark available for modifying the code as shown (or equivalent code):

```

96 public void Enqueue(int value)
97 {
98     QueueTail = IdentifyQueueTail();
99     QueueTail.SetPrevious(CurrentTail); // 88
100     (CurrentTail == null)
101     {
102         QueueHead = AddedNode;
103     }
104     else
105     {
106         CurrentTail.SetPointer(AddedNode);
107     }
108 }
109 // 81
110 Console.WriteLine("The value " + IdentifyQueueTail().GetValue() + " has been enqueued");
111 }
112

```

■ B2

1 mark available for modifying the code as shown (or equivalent code):

```

123 public void Dequeue()
124 {
125     if (QueueHead == null)
126     {
127         Console.WriteLine("The " + QueueDescriptor + " queue was empty and no node was removed");
128     }
129     else
130     {
131         // 82
132         Console.WriteLine("The value " + QueueHead.GetValue() + " has been dequeued");
133         QueueHead.SetPointer(QueueHead.GetPointer());
134     }
135     if (QueueHead == null)
136     {
137         Console.WriteLine("The only element in the " + QueueDescriptor + " queue was removed");
138     }
139     // 84
140     else
141     {
142         QueueHead.SetPrevious(null); // 84
143     }
144 }
145

```

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■ B3

5 marks available for modifying the code as shown (or equivalent code):

```

137 // B3
138 public int GetSize()
139 {
140     // Empty queues have a size of 0 nodes
141     if (QueueHead == null)
142     {
143         return 0;
144     }
145     // Point to the current head of the queue and create a new node
146     Node TailNode = QueueHead;
147     int QuantityOfNodes = 1;
148
149     // Whilst there are other nodes to be found...
150     while (TailNode.GetPointer() != null)
151     {
152         // ... advance the pointer to them and add
153         TailNode = TailNode.GetPointer();
154         QuantityOfNodes++;
155     }
156
157     return QuantityOfNodes;
158 }
159

```

Marks can be awarded for:

- handling null pointers
- setting the head of the queue to be the tail pointer (which deals with lists of length 0)
- advancing the tail pointer while there are more nodes in the list (which would be a list of length of 1)
- keeping a running total of how many nodes were found
- returning the correct value accurately

■ B4

6 marks available for modifying the code as shown (or equivalent code):

Marks could be awarded for:

- adding a previousNode attribute to the Node class
- setting the previousNode attribute according to a parameter passed into the addValue procedure
- modifying the addValue procedure to correctly set the previousNode attribute

In Node.cs: [0 marks] for this:

```

7 // Instance attributes
8
9 private String Value;
10 private Node Pointer;
11 private Node PreviousNode;
12

```

[1 mark] for this:

```

34
35 public Node GetPrevious()
36 {
37     return PreviousNode;
38 }
39

```

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[1 mark] for this:

```

52          // B4
53      public void SetPrevious(Node UpdatedPrevious)
54      {
55          PreviousNode = UpdatedPrevious;
56      }

```

In Queue.cs: [1 mark] for this:

```

98      Node CurrentTail = IdentifyQueueTail();
99      AddNodeToPrevious(CurrentTail); // B4
100     CurrentTail = null;

```

[1 mark] for

```

129          // B4
130      else
131      {
132          QueueHead.SetPrevious(null); // B4
133      }
134  }
135  }

```

[1 mark] for this:

```

17
18      public Queue(String Details, Node FirstNodeAdded)
19      {
20          Enqueue(FirstNodeAdded);
21          QueueDescriptor = Details;
22      }

```

Suitable output from Queue.PrintQueue [1 mark] for this:

```

66      Console.WriteLine(NodeIndex + "\t" + CurrentNode.GetValue() + "
67
68      CurrentNode = CurrentNode.GetPointer();

```

■ B5

6 marks available for modifying the code as shown (or equivalent code):

[2 marks] for successfully producing the GetNodeAt (n) function:

```

162     private Node GetNodeAt(int pos)
163     {
164         // Empty queues have a size of 0 nodes
165         if (QueueHead == null)
166         {
167             return null;
168         }
169
170         // Point to the current head of the queue and create a
171         Node LocatedNode = QueueHead;
172         int QuantityOfNodes = 1;
173
174         // If there are other nodes to be found...
175         while (QuantityOfNodes < pos)
176         {
177             // ... advance the pointer to them and add
178             LocatedNode = LocatedNode.GetPointer();
179             QuantityOfNodes++;
180         }
181
182         return LocatedNode;
183     }

```

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[3 marks] for the Bump () procedure handling short queues effectively AND robustly

```

185 // 05
186 public void Bump()
187 {
188     int SizeOfQueue = GetSize(); // storing the size prevents multiple method calls and
189
190     // Exit this procedure if there are not enough items to permit swapping
191     if (SizeOfQueue < 2)
192     {
193         Console.WriteLine("As there are fewer than 2 items in the queue, swapping will
194             return;
195     }
196
197     // Allow the user to decide if they want to bump up the queue
198     Console.WriteLine("The queue has " + SizeOfQueue + " items in the queue.");
199     PrintQueue();
200     Console.WriteLine("Queue item (#2 to #) + SizeOfQueue + ") should be swapped with
201     int positionChosen = -1;
202

```

```

204 {
205     try
206     {
207         positionChosen = int.Parse(Console.ReadLine());
208         if(positionChosen < 2 || positionChosen > SizeOfQueue)
209         {
210             Console.WriteLine("Please choose a queue item number in the range 2 to
211         }
212     }
213     catch (FormatException FormatEx)
214     {
215         Console.WriteLine("This is not an integer value; please try again.");
216     }
217 } while (positionChosen < 2 || positionChosen > SizeOfQueue);
218
219 // Identify the node to be brought forward:
220 Node BringForward = GetNodeAt(positionChosen);
221
222 // Now that the node is in hand...
223 Console.WriteLine("The user has chosen " + BringForward.GetValue() + " to be bumped
224
225 // [1ST FORWARD POINTER (working from the HEAD of the queue)]
226 if(BringForward.GetPrevious().GetPrevious() != null) // in case dealing with 2 at
227 {
228     BringForward.GetPrevious().GetPrevious().SetPrevious(BringForward);
229 }
230 else
231 {
232     Queue.First.SetPrevious(BringForward);
233 }
234

```

[4 marks] for the complex job of handling pointers:

```

236 // [2ND FORWARD POINTER]
237 BringForward.GetPrevious().SetPointer(BringForward.GetPointer());
238
239 // [3RD FORWARD POINTER]
240 BringForward.SetPointer(BringForward.GetPrevious());
241
242 // [1ST PREVIOUS POINTER (working from the TAIL of the queue)]
243 if(BringForward.GetPointer().GetPointer() != null) // in case
244 {
245     BringForward.GetPointer().GetPointer().SetPrevious(BringForward);
246 }
247
248 // [2ND PREVIOUS POINTER]
249 BringForward.SetPrevious(BringForward.GetPointer().GetPrevious());
250
251 // [3RD PREVIOUS POINTER]
252 BringForward.GetPointer().SetPrevious(BringForward);
253
254 Console.WriteLine("Queue bump is complete!");
255 PrintQueue();
256

```

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9 marks available for modifying the code as shown (or equivalent code):

[3 marks] for setting up Swap () to take in a parameter and proceed as Bump () do

```

259 public void Swap(int positionChosen)
260 {
261     int SizeOfQueue = GetSize(); // storing the size prevents multiple method
262
263     // Identify the node to be brought forward
264     Node BringForward = GetNodeAt(positionChosen);
265
266     // [1ST FORWARD POINTER] (bring the HEAD of the queue)
267     if (BringForward.GetPrevious() != null) // in case dealing with
268     {
269         BringForward.GetPrevious().GetPrevious().SetPointer(BringForward);
270     }
271     // [2ND FORWARD POINTER]
272     QueueHead = BringForward;
273
274     // [3RD FORWARD POINTER]
275     BringForward.GetPrevious().SetPointer(BringForward.GetPointer());
276
277     // [4TH FORWARD POINTER]
278     BringForward.SetPointer(BringForward.GetPrevious());
279
280 }

```

```

282 // [1ST PREVIOUS POINTER (working from the TAIL of the queue)]
283 if (BringForward.GetPointer().GetPointer() != null) // in case dealing with
284 {
285     BringForward.GetPointer().GetPointer().SetPrevious(BringForward.GetPointer());
286 }
287
288 // [2ND PREVIOUS POINTER]
289 BringForward.SetPrevious(BringForward.GetPointer().GetPrevious());
290
291 // [3RD PREVIOUS POINTER]
292 BringForward.GetPointer().SetPrevious(BringForward.GetPrevious());
293 }

```

[6 marks] for the logic of the BubbleSort () method:

- [1] for handling lists with less than three items
- [1] for identifying the left and right values
- [1] for successfully determining their alphabetical order
- [1] for iterating correctly (OUTER loop)
- [1] for iterating correctly (INNER loop)
- [1] for swapping effectively

```

296 public void BubbleSort()
297 {
298     // Exit this procedure if there are not enough items to permit bubble sort
299     if (GetSize() < 2)
300     {
301         Console.WriteLine("The queue is already in order. No swaps were required.");
302         return;
303     }
304
305     // Store (temporarily) the 2 node values at the tail of the queue
306     string LeftValue;
307     string RightValue;
308
309     // Exclude 1 more node on the HEAD side of the queue after each full pass
310     int EndOfSortedValuesPointer = 0;
311     while (EndOfSortedValuesPointer < GetSize()) // note that zero-based index
312     {
313         // Note that EndOfSortedValuesPointer is NOT in use here
314         for (int i = 1; i < (GetSize() - EndOfSortedValuesPointer); i++)
315         {
316             LeftValue = GetNodeAt(i-1).GetValue();
317             RightValue = GetNodeAt(i).GetValue();
318
319             if (string.CompareOrdinal(LeftValue, RightValue) > 0) // compare
320             {
321                 Swap(i-1, i);
322             }
323         }
324         EndOfSortedValuesPointer++;
325     }
326 }

```

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EXERCISE 5 – DRAUGHTS

SECTION A

■ A1

1 mark for:

Line 13 of Board.cs

■ A2

1 mark for 1 example in each line below:

Declared: Board.cs Line 7, Piece.cs Line 7/8

Initialised: Piece.cs Line 13, Piece.cs Line 14/15

Read: Board.cs Line 21, Piece.cs Line 22/27

■ A3

1 mark for giving a valid reason to use private methods; for example:

A method may be made public so that it can be accessed from other parts of the program (which the attribute is declared).

Setting PlacePieces to private is done as it is needed only from within this class ... so to protect programmers from accidentally misusing the method in the wrong way.

■ A4

1 mark for each point:

It needs one so that its colour can be determined at the point of need [1], ... but it can't be because all pieces will be initialised without being kinged [1] and the king=false setting.

■ A5

1 mark per point; must include first point:

Option 2 is correct [1 – essential]

The board is a 2D array of Piece objects, many of them null pointers [1]

If we used the Piece objects to store their position, we would have to be able to iterate through the image of the board, and this would require them to be in a data structure anyway.

■ A6

1 mark per point:

- The main method constructs a new Board object; only one for one game.
- The Display() method of this one board is called from within the main method.
- Heading rows get output. [NB As an extension task, this feature could make use of a BoardSize variable in Section B to make it always output the correct heading rows there are...]
- The various rows of the board are iterated through using the GetLength() method to find out how many rows there are...
- ... and within each row the columns are iteratively visited by using the GetLength() method to work out the number of columns.
- Each square gets output as a visualisation including the character code R or W for white squares. Black squares have no visible characters. All rows end with a newline character determined by calling the accessor method named GetColour() of the Piece object.
- The board ends with a marker character.

■ A7

2 marks (1 mark for explaining why it is bad practice; 1 mark for suggesting what should be done)

It is bad practice to hard-code in a value that is used throughout the program, as if at a later point, every instance of the value in the program needs to be changed. Instead, a constant (or a static variable) that contains this value should be used so that if the value needs to be changed, it can be done in only one place in the program. The name of the constant being visible throughout the program improves readability/maintainability.

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■ A8

2 marks (1 mark for stating what it does; 1 mark for explaining how it works); for example:

- MOD checks that a square is black.
- It does this before setting a piece on the board. If a square is white, it drops the piece.
- It works by adding the row and column numbers. All white squares have an odd sum, and all black squares have an even sum using the result of Sum MOD 2. If it yields a 0, the square is white.

■ A9

2 marks (1 mark for explaining what inheritance is; 1 mark for explaining why inheritance is used in relating it to draughts); for example:

Inheritance is when a class takes on the functionality of a different class. It is used when multiple classes share the same data or methods. Here, it can be used to create a specialised version of a playing piece with some unique attributes and methods without creating a new Piece class.

■ A10

3 marks (1 mark for explaining what a function is, 1 mark for explaining what a procedure is, 1 mark for explaining what a method is):

A function is a subroutine that returns a value, whereas a procedure is a subroutine that does not return a value. A method is a subroutine that is part of a certain class (a method can be either a function or a procedure).

■ A11

2 marks (1 mark for explaining that a class is a template used to define objects; 1 mark for explaining that an object is an existing instance of a class):

A class is a template of what attribute and methods are needed for objects of that class. An object is an instance of that class that has its own concrete attributes. Here, a DraughtsBoard created could have its own attributes but their key characteristics are defined in their class from which they are created.

SECTION B

■ B1

1 mark available for modifying the code as shown (or equivalent code):

```

55         if (((row + col) % 2) == 0) // B1
56         {
57             Console.WriteLine(" _ |"); // square is white
58         }
59         else if (DraughtsBoard[row, col] != null)

```

■ B2

1 mark available for modifying the code as shown (or equivalent code):

```

6         {
7             private Piece[,] DraughtsBoard;
8             private int BoardSize; // B2

```

1 mark for the constructor:

```

17         BoardSize = 8; // B2
18         DraughtsBoard = new Piece[BoardSize, BoardSize];

```

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■ B3

2 marks available for modifying the code as shown (or equivalent code):

1 mark per meaningful line:

```

32          // B3
33      public int GetBoardSize()
34      {
35          return BoardSize;
36      }

```

■ B4

4 marks available for completing the methods (as shown below, or equivalent code).

Marks could be awarded for:

- [1] creating a PieceAt function in the Board class that takes a row and col
- [1] returning the piece at the position given by the input list, applying suit
- [1] checking for nulls and white squares in the DisplayPieceAt method
- [1] displaying the contents of all squares with pieces on them appropriately

In Board.cs:

```

121          // B4
122      public Piece PieceAt(int row, int col)
123      {
124          if(row < 0 || row >= BoardSize || col < 0 || col >= BoardSize)
125          {
126              return null;
127          }
128          return DraughtsBoard[row, col];
129      }
130
131          // B4
132      public void DisplayPieceAt(int row, int col)
133      {
134          Piece PieceObtained = PieceAt(row, col);
135          if((row + col) % 2 == 0)
136          {
137              Console.WriteLine("[ " + row + ", " + col + " ] is a white square");
138          }
139          else if(PieceObtained == null)
140          {
141              Console.WriteLine("No piece is found at [ " + row + ", " + col + " ]");
142          }
143          else
144          {
145              Console.WriteLine(PieceAt(row, col).GetColour() + " is found at [ " + row + ", " + col + " ]");
146          }
147      }
148
149

```

In Program.cs:

```

12          // B4
13      GameBoard.DisplayPieceAt(4, 0);
14      GameBoard.DisplayPieceAt(6, 0);
15      GameBoard.DisplayPieceAt(0, 1);
16      GameBoard.DisplayPieceAt(7, 0);
17

```

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■ B5

2 marks for the TurnNumber work:

```

9      private int TurnNumber; // B5

38     // B5
39     public int GetTurnNumber()
40     {
41         return TurnNumber;
42     }
43
44     // Mutation of the
45     // TurnNumber
46     public void UpdateTurnNumber()
47     {
48         TurnNumber++;
49     }
50

```

10 marks for validating the move attempted:

Marks could be awarded for:

- creating a `validMove` function that returns *True* if a given move by a given
- returning *False* if there is no piece at the start position to move
- returning *False* if the end position is not on the board
- returning *False* if the player tries to move a token non-diagonally or more than
- returning *False* if the end position is not empty
- returning *False* if the player tries to move a token two spaces without taking
- returning *False* if a player tries to move a non-king piece backwards
- handling non-integer input
- checking for the existence of a piece in a square BEFORE proceeding to ask
- **overall** readability/commenting on code to make this complex algorithm rea

```

150
151  public bool ValidMove(int StartRow, int StartCol, int EndRow, int EndCol)
152  {
153      Piece PieceToBeMoved = PieceAt(StartRow, StartCol);
154
155      if(PieceToBeMoved == null)
156      {
157          Console.WriteLine("ERROR - INVALID PIECE SELECTION {Error occurred}");
158          return false;
159      }
160
161      // Check if the destination is off the board
162      if(EndRow >= BoardSize || EndCol >= BoardSize || EndRow < 0 || EndCol < 0)
163      {
164          Console.WriteLine("ERROR - INVALID DESTINATION SQUARE SELECTION");
165          return false;
166      }
167
168      if(!PieceToBeMoved.GetKing()) // assuming the piece is not a King
169      {
170          if (TurnNumber % 2 == 1)
171          {
172              // It is Black's turn to move a non-knight
173

```

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```

174 // Black is attempting to move 1 step without capturing
175 if (StartRow - 1 == EndRow && (EndCol == StartCol - 1 || EndCol == StartCol + 1))
176 {
177     // Black is attempting to land 1 square forwards
178     if (PieceAt(EndRow, EndCol) == null)
179     {
180         return true;
181     }
182     else
183     {
184         Console.WriteLine("ERROR - The destination square is not empty");
185         return false;
186     }
187 }
188 // Black is attempting to move 2 squares forwards, capturing
189 else if (StartRow - 2 == EndRow)
190 {
191     // Check that the destination is 2 diagonal squares away
192     if (EndCol == StartCol - 2 || EndCol == StartCol + 2)
193     {
194         // Black is attempting to land 2 squares forwards
195         if (PieceAt(EndRow, EndCol) == null)
196         {
197             if (PieceAt((StartRow + EndRow) / 2, (StartCol + EndCol) / 2) != null)
198             {
199                 return true;
200             }
201             Console.WriteLine("ERROR - You must capture a piece");
202             return false;
203         }
204         else
205         {
206             Console.WriteLine("ERROR - The destination square is not empty");
207             return false;
208         }
209     }
210     else
211     {
212         Console.WriteLine("ERROR - This move is not a 1 or 2 square move");
213         return false;
214     }
215 }
216 }
217 else
218 {
219     // It is RED's move as a non-knight ///////////////////////////////////
220 }
221 // Red is attempting to move 1 step without capturing
222 if (StartRow + 1 == EndRow && (EndCol == StartCol - 1 || EndCol == StartCol + 1))
223 {
224     // Red is attempting to land 1 square forwards
225     if (PieceAt(EndRow, EndCol) == null)
226     {
227         return true;
228     }
229     else
230     {
231         Console.WriteLine("ERROR - The destination square is not empty");
232         return false;
233     }
234 }

```

```

234     }
235     // Red is attempting to move 2 squares forwards, capturing
236     else if (StartRow + 2 == EndRow)
237     {
238         // Check that the destination is 2 diagonal squares away
239         if (EndCol == StartCol - 2 || EndCol == StartCol + 2)
240         {
241             // Red is attempting to land 2 squares forwards and
242             if (PieceAt(EndRow, EndCol) == null)
243             {
244                 if (PieceAt((StartRow + EndRow) / 2, (StartCol
245                 {
246                     return true;
247                 }
248                 Console.WriteLine("ERROR - You must capture a
249                 return false;
250             }
251             else
252             {
253                 Console.WriteLine("ERROR - This move is not a
254                 return false;
255             }
256         }
257     }
258     else
259     {
260         Console.WriteLine("ERROR - This move is not a 1-step
261         return false;
262     }
263 }
264 }
265 else

```

```

266 // The piece is a King and has more freedom of movement
267 {
268     if (TurnNumber % 2 == 1)
269     {
270         // It is BLACK's move as a knight
271
272         // Black is attempting to move 1 square without capturing
273         if ((StartRow - 1 == EndRow || StartRow + 1 == EndRow) && (EndCol ==
274         {
275             // Black is attempting to land 1 square up/down and 1 step left/right
276             if (PieceAt(EndRow, EndCol) == null)
277             {
278                 return true;
279             }
280             else
281             {
282                 Console.WriteLine("ERROR - The destination square is not empty
283                 return false;
284             }
285         }
286         // Black is attempting to move 2 squares away diagonally, capturing
287         else if (StartRow - 2 == EndRow || StartRow + 2 == EndRow)
288         {
289             // Check that the destination is 2 diagonal squares away
290             if (EndCol == StartCol - 2 || EndCol == StartCol + 2)
291             {
292                 // Black is attempting to land 2 squares forwards and 2 step
293                 if (PieceAt(EndRow, EndCol) == null)
294                 {

```

```

295         if (PieceAt((StartRow + EndRow) / 2, (StartCol + EndCol))
296             {
297             return true;
298             }
299         Console.WriteLine("ERROR - You must capture a Red if jump
300         return false;
301     }
302     else
303     {
304         Console.WriteLine("ERROR - The destination square is not
305         return false;
306     }
307 }
308 }
309 else
310 {
311     Console.WriteLine("ERROR - This move is not a 1-step or 2-step di
312     return false;
313 }
314 else
315 {
316     // It is RED's move as a knight
317
318     // Red is attempting to move 1 step away without capturing
319     if ((StartRow - 1 == EndRow || StartRow + 1 == EndRow) && (EndCol ==
320     {
321         // Red is attempting to land 1 square up/down and 1 step left/right
322         if (PieceAt(EndRow, EndCol) == null)
323         {

```

```

325         return true;
326     }
327     else
328     {
329         Console.WriteLine("ERROR - The destination square
330         return false;
331     }
332 }
333 // Red is attempting to move 2 squares away diagonally, capture
334 else if (StartRow + 2 == EndRow || StartRow - 2 == EndRow)
335 {
336     // Check that the destination is 2 diagonal squares away
337     if (EndCol == StartCol - 2 || EndCol == StartCol + 2)
338     {
339         // Red is attempting to land 2 squares up/down and
340         if (PieceAt(EndRow, EndCol) == null)
341         {
342             if (PieceAt((StartRow + EndRow) / 2, (StartCol
343             {
344                 return true;
345             }
346             Console.WriteLine("ERROR - You must capture a
347             return false;
348         }
349         else
350         {
351             Console.WriteLine("ERROR - The destination square
352             return false;
353         }
354     }

```

```

355     }
356     else
357     {
358         Console.WriteLine("ERROR - This move is not a 1
359         return false;
360     }
361 }
362 }
363 }
364 return false;
365 }

```

```

19 PiecePieces();
20 TurnNumber = 1; // B5
21 BlackPiecesRemoved = 0;

```

■ B6

5 marks available for modifying the code as shown (or equivalent code):

Marks could be awarded for:

- handling null pointers at vacant squares
- returning *True* when Black is found on a black square on Black's turn
- returning *True* when Red is found on a black square on Red's turn
- returning *False* in other cases
- suitable console output

```

367 // B6
368 public bool ValidColour(int Row, int Col)
369 {
370     if(DraughtsBoard[Row, Col] == null)
371     {
372         Console.WriteLine("No playing piece found at [" +
373             Row + ", " + Col + "]");
374         return false;
375     }
376     if(DraughtsBoard[Row, Col].GetColour() == 'B')
377     {
378         if(TurnNumber % 2 == 1)
379         {
380             return true;
381         }
382         Console.WriteLine("The piece at [" + Row + ", " + Col + "] is Black");
383         return false;
384     }
385     else if(DraughtsBoard[Row, Col].GetColour() == 'R')
386     {
387         if (TurnNumber % 2 == 0)
388         {
389             return true;
390         }
391         Console.WriteLine("The piece at [" + Row + ", " + Col + "] is Red");
392         return false;
393     }
394     Console.WriteLine("ERROR in ValidColour().");
395     return false;
396 }
397

```

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8 marks available for modifying the code as shown (or equivalent code):

Marks could be awarded for:

- creating a GetMove function that returns start and end positions as a pair
- by player input is valid
- getting a start position and an end position from the user
- checking whether or not the move is valid
- asking the user for new input if the move is invalid
- displaying appropriate message depending on whether or not the move is valid
- amending TurnNumber
- sensible output
- leaving the board unaffected by an invalid move

```

400 public void GetMove()
401 {
402     // ROW of piece
403
404     Console.WriteLine("Enter the row number (0-" + (BoardSize - 1) + ")");
405     int StartRow = -1;
406     do
407     {
408         try
409         {
410             StartRow = int.Parse(Console.ReadLine());
411             if (StartRow < 0 || StartRow >= BoardSize)
412             {
413                 Console.WriteLine("Valid options are 0-7 only. Try again.");
414             }
415         }
416         catch (FormatException fex)
417         {
418             Console.WriteLine("Please only enter integers. Try again.");
419         }
420     } while (StartRow < 0 || StartRow >= BoardSize);
421
422     // COLUMN of piece
423
424     Console.WriteLine("Enter the column number (0-" + (BoardSize - 1) + ")");
425     int StartCol = -1;
426     do
427     {
428         try
429         {
430             StartCol = int.Parse(Console.ReadLine());
431             if (StartCol < 0 || StartCol >= BoardSize)
432             {
433                 Console.WriteLine("Valid options are 0-7 only. Try again.");
434             }
435         }
436         catch (FormatException fex)
437         {
438             Console.WriteLine("Please only enter integers. Try again.");
439         }
440     } while (StartCol < 0 || StartCol >= BoardSize);
441
442     // Check that the correct colour of piece has been lifted:
443     if (ValidColour(StartRow, StartCol))
444     {
445         // ROW of destination
446
447         Console.WriteLine("Enter the row number (0-" + (BoardSize - 1) + ")");
448         int EndRow = -1;
449         do
450         {
451             try
452             {
453                 EndRow = int.Parse(Console.ReadLine());
454                 if (EndRow < 0 || EndRow >= BoardSize)
455                 {
456                     Console.WriteLine("Valid options are 0-7 only. Try again.");
457                 }
458             }
459             catch (FormatException fex)

```

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```

458         {
459             Console.WriteLine("Please only enter integers. Try again");
460         }
461     } while (EndRow < 0 || EndRow >= BoardSize);
462
463     // COLUMN of destination
464
465     Console.Write("Enter the column number (0." + (BoardSize-1) + ")");
466     int EndCol = -1;
467     do
468     {
469         try
470         {
471             EndCol = int.Parse(Console.ReadLine());
472             if (EndCol < 0 || EndCol >= BoardSize)
473             {
474                 Console.WriteLine("Valid options are 0-7 only. Try again");
475             }
476         }
477         catch (FormatException fex)
478         {
479             Console.WriteLine("Please only enter integers. Try again");
480         }
481     } while (EndCol < 0 || EndCol >= BoardSize);
482
483     // Valid input received by now.
484
485     // MOVE THE PIECE
486     if (ValidMove(StartRow, StartCol, EndRow, EndCol))
487     {
488         DraughtsBoard[EndRow, EndCol] = DraughtsBoard[StartRow, StartCol];
489         DraughtsBoard[StartRow, StartCol] = null;
490
491         // If Black reaches Red's starting row, it gets kinged
492         if (TurnNumber % 2 == 1 && EndRow == 0)
493         {
494             DraughtsBoard[EndRow, EndCol].SetKing();
495         }
496
497         // If Red reaches Black's starting row, it gets kinged
498         if (TurnNumber % 2 == 0 && EndRow == (BoardSize-1))
499         {
500             DraughtsBoard[EndRow, EndCol].SetKing();
501         }
502
503         // Remove jumped pieces
504         if (Math.Abs(EndRow - StartRow) == 2) // If the squares are 2
505         {
506             // Remove the piece in the middle of the Start and End squares
507             DraughtsBoard[(EndRow + StartRow) / 2, (StartCol + EndCol) / 2] = null;
508
509             // Update the number of pieces removed
510             if (TurnNumber % 2 == 0)
511             {
512                 BlackPiecesRemoved++;
513                 Console.WriteLine("BLACK PIECE REMOVED");
514             }
515             else
516             {
517                 RedPiecesRemoved++;
518                 Console.WriteLine("RED PIECE REMOVED");
519             }
520         }
521
522         UpdateTurnNumber();
523     }
524     else
525     {
526         Console.WriteLine("Invalid move. Try again.");
527     }
528 }
529
530 // The board has not been changed. Try again; it's the same board.
531 Console.WriteLine("The board has not been changed. Try again; it's the same board.");
532
533 }
534
535 }
536
537

```

In Program.cs: Test code:

```

29          // B6
30
31          // Black (turn 1)
32          GameBoard.GetMove();
33          GameBoard.Display();
34          // Red (turn 2)
35          GameBoard.GetMove();
36          GameBoard.Display();
37          // Black (turn 3)
38          GameBoard.GetMove();
39          GameBoard.Display();
40          // Red (turn 4)
41          GameBoard.GetMove();
42          GameBoard.Display();
43          // Black (turn 5)
44          GameBoard.GetMove();
45          GameBoard.Display();
46          // Red (turn 6)
47          GameBoard.GetMove();
48          GameBoard.Display();

```

■ B8

6 marks available for modifying the code as shown (or equivalent code):

Marks could be awarded for:

- creating a CheckWon function that returns either the playing piece colour or empty string if no player has won
- calling CheckWon after each move
- creating a game loop that exits once a player has won
- alternating turns between a 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 67, 68, 69, 70, 71, 72, 73, 74, 75, 76, 77, 78, 79, 80, 81, 82, 83, 84, 85, 86, 87, 88, 89, 90, 91, 92, 93, 94, 95, 96, 97, 98, 99, 100, 101, 102, 103, 104, 105, 106, 107, 108, 109, 110, 111, 112, 113, 114, 115, 116, 117, 118, 119, 120, 121, 122, 123, 124, 125, 126, 127, 128, 129, 130, 131, 132, 133, 134, 135, 136, 137, 138, 139, 140, 141, 142, 143, 144, 145, 146, 147, 148, 149, 150, 151, 152, 153, 154, 155, 156, 157, 158, 159, 160, 161, 162, 163, 164, 165, 166, 167, 168, 169, 170, 171, 172, 173, 174, 175, 176, 177, 178, 179, 180, 181, 182, 183, 184, 185, 186, 187, 188, 189, 190, 191, 192, 193, 194, 195, 196, 197, 198, 199, 200, 201, 202, 203, 204, 205, 206, 207, 208, 209, 210, 211, 212, 213, 214, 215, 216, 217, 218, 219, 220, 221, 222, 223, 224, 225, 226, 227, 228, 229, 230, 231, 232, 233, 234, 235, 236, 237, 238, 239, 240, 241, 242, 243, 244, 245, 246, 247, 248, 249, 250, 251, 252, 253, 254, 255, 256, 257, 258, 259, 260, 261, 262, 263, 264, 265, 266, 267, 268, 269, 270, 271, 272, 273, 274, 275, 276, 277, 278, 279, 280, 281, 282, 283, 284, 285, 286, 287, 288, 289, 290, 291, 292, 293, 294, 295, 296, 297, 298, 299, 300, 301, 302, 303, 304, 305, 306, 307, 308, 309, 310, 311, 312, 313, 314, 315, 316, 317, 318, 319, 320, 321, 322, 323, 324, 325, 326, 327, 328, 329, 330, 331, 332, 333, 334, 335, 336, 337, 338, 339, 340, 341, 342, 343, 344, 345, 346, 347, 348, 349, 350, 351, 352, 353, 354, 355, 356, 357, 358, 359, 360, 361, 362, 363, 364, 365, 366, 367, 368, 369, 370, 371, 372, 373, 374, 375, 376, 377, 378, 379, 380, 381, 382, 383, 384, 385, 386, 387, 388, 389, 390, 391, 392, 393, 394, 395, 396, 397, 398, 399, 400, 401, 402, 403, 404, 405, 406, 407, 408, 409, 410, 411, 412, 413, 414, 415, 416, 417, 418, 419, 420, 421, 422, 423, 424, 425, 426, 427, 428, 429, 430, 431, 432, 433, 434, 435, 436, 437, 438, 439, 440, 441, 442, 443, 444, 445, 446, 447, 448, 449, 450, 451, 452, 453, 454, 455, 456, 457, 458, 459, 460, 461, 462, 463, 464, 465, 466, 467, 468, 469, 470, 471, 472, 473, 474, 475, 476, 477, 478, 479, 480, 481, 482, 483, 484, 485, 486, 487, 488, 489, 490, 491, 492, 493, 494, 495, 496, 497, 498, 499, 500, 501, 502, 503, 504, 505, 506, 507, 508, 509, 510, 511, 512, 513, 514, 515, 516, 517, 518, 519, 520, 521, 522, 523, 524, 525, 526, 527, 528, 529, 530, 531, 532, 533, 534, 535, 536, 537, 538, 539, 540, 541, 542, 543, 544, 545, 546, 547, 548, 549, 550, 551, 552, 553, 554, 555, 556, 557, 558, 559, 560, 561, 562, 563, 564, 565, 566, 567, 568, 569, 570, 571, 572, 573, 574, 575, 576, 577, 578, 579, 580, 581, 582, 583, 584, 585, 586, 587, 588, 589, 590, 591, 592, 593, 594, 595, 596, 597, 598, 599, 600, 601, 602, 603, 604, 605, 606, 607, 608, 609, 610, 611, 612, 613, 614, 615, 616, 617, 618, 619, 620, 621, 622, 623, 624, 625, 626, 627, 628, 629, 630, 631, 632, 633, 634, 635, 636, 637, 638, 639, 640, 641, 642, 643, 644, 645, 646, 647, 648, 649, 650, 651, 652, 653, 654, 655, 656, 657, 658, 659, 660, 661, 662, 663, 664, 665, 666, 667, 668, 669, 670, 671, 672, 673, 674, 675, 676, 677, 678, 679, 680, 681, 682, 683, 684, 685, 686, 687, 688, 689, 690, 691, 692, 693, 694, 695, 696, 697, 698, 699, 700, 701, 702, 703, 704, 705, 706, 707, 708, 709, 710, 711, 712, 713, 714, 715, 716, 717, 718, 719, 720, 721, 722, 723, 724, 725, 726, 727, 728, 729, 730, 731, 732, 733, 734, 735, 736, 737, 738, 739, 740, 741, 742, 743, 744, 745, 746, 747, 748, 749, 750, 751, 752, 753, 754, 755, 756, 757, 758, 759, 760, 761, 762, 763, 764, 765, 766, 767, 768, 769, 770, 771, 772, 773, 774, 775, 776, 777, 778, 779, 780, 781, 782, 783, 784, 785, 786, 787, 788, 789, 790, 791, 792, 793, 794, 795, 796, 797, 798, 799, 800, 801, 802, 803, 804, 805, 806, 807, 808, 809, 810, 811, 812, 813, 814, 815, 816, 817, 818, 819, 820, 821, 822, 823, 824, 825, 826, 827, 828, 829, 830, 831, 832, 833, 834, 835, 836, 837, 838, 839, 840, 841, 842, 843, 844, 845, 846, 847, 848, 849, 850, 851, 852, 853, 854, 855, 856, 857, 858, 859, 860, 861, 862, 863, 864, 865, 866, 867, 868, 869, 870, 871, 872, 873, 874, 875, 876, 877, 878, 879, 880, 881, 882, 883, 884, 885, 886, 887, 888, 889, 890, 891, 892, 893, 894, 895, 896, 897, 898, 899, 900, 901, 902, 903, 904, 905, 906, 907, 908, 909, 910, 911, 912, 913, 914, 915, 916, 917, 918, 919, 920, 921, 922, 923, 924, 925, 926, 927, 928, 929, 930, 931, 932, 933, 934, 935, 936, 937, 938, 939, 940, 941, 942, 943, 944, 945, 946, 947, 948, 949, 950, 951, 952, 953, 954, 955, 956, 957, 958, 959, 960, 961, 962, 963, 964, 965, 966, 967, 968, 969, 970, 971, 972, 973, 974, 975, 976, 977, 978, 979, 980, 981, 982, 983, 984, 985, 986, 987, 988, 989, 990, 991, 992, 993, 994, 995, 996, 997, 998, 999, 1000
- displaying a message at the end of the game to say which player has won
- successfully using GetMove to remove a piece

In Board.cs:

```

539     public String CheckWon()
540     {
541         if(BlackPiecesRemoved > 11)
542         {
543             return "RED";
544         }
545         if(RedPiecesRemoved > 11)
546         {
547             return "BLACK";
548         }
549         return "";
550     }

```

In Program.cs:

```

19     String Winner = GameBoard.CheckWon();
20     while(Winner.Equals(""))
21     {
22         GameBoard.GetMove();
23         GameBoard.Display();
24         Winner = GameBoard.CheckWon();
25     }
26
27     Console.WriteLine("The winner is " + Winner);

```

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Removing a piece (in Board.cs):

```

506         if (Math.Abs(EndRow - StartRow) == 2) // If the squares are 2
507         {
508             // Remove the piece in the middle of the Start and End squares
509             DraughtsBoard[(EndRow + StartRow) / 2, (StartCol + EndCol)] = null;
510
511             // Update the number of pieces removed
512             if (TurnNumber % 2 == 0)
513             {
514                 BlackPiecesRemoved++;
515                 Console.WriteLine("BLACK PIECE REMOVED");
516             }
517             else
518             {
519                 RedPiecesRemoved++;
520                 Console.WriteLine("RED PIECE REMOVED");
521             }
522         }
523
524         UpdateTurnNumber();
525     }
526     else

```

■ B9

4 marks available for modifying the code as shown (or equivalent code):

Marks could be awarded for:

- correctly placing this after the move has taken place
- checking the turn and the end row criteria simultaneously
- treating Red differently in case of a different-sized board
- calling the amended SetKing() method

```

487 // MOVE THE PIECE
488 if (ValidMove(StartRow, StartCol, nr, nc, EndCol))
489 {
490     DraughtsBoard[nr, nc] = DraughtsBoard[StartRow, StartCol];
491     DraughtsBoard[StartRow, StartCol] = null;
492
493     // B9 - If Black reaches Red's starting row, it gets king
494     if (TurnNumber % 2 == 1 && EndRow == 0)
495     {
496         DraughtsBoard[EndRow, EndCol].SetKing();
497     }
498
499     // B9 - If Red reaches Black's starting row, it gets king
500     if (TurnNumber % 2 == 0 && EndRow == (BoardSize - 1))
501     {
502         DraughtsBoard[(BoardSize - 1), EndCol].SetKing();
503     }
504
505     // B9 - Remove jumped pieces
506     if (Math.Abs(EndRow - StartRow) == 2) // If the squares are 2

```

In Piece.cs:

```

32 public void SetKing()
33 {
34     King = true;
35     // B9
36     Name = Name + Colour.ToLower()[0]; // set to lowercase permanent
37     // Using Unicode value + 32 would recur every time the king is set
38     Console.WriteLine("The piece has reached the far side and has become a king");
39 }

```

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EXERCISE 6 – TREE TRAVERSAL

SECTION A

■ A1

1 mark each:

Call to a constructor: Line

Private attribute declaration: Line

Use of a null pointer: Line

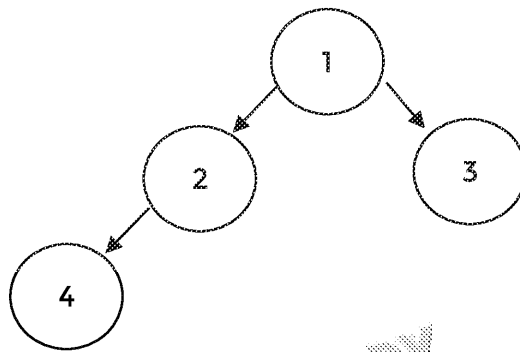
■ A2

1 mark for:

Line

■ A3

2 marks (1 mark for drawing a binary tree; 1 mark for arranging the values correctly)



■ A4

2 marks (1 mark for explaining that binary tree nodes can have a maximum of two children and that nodes in a multi-branch tree can have any number of child nodes):

The nodes in a binary tree can have a maximum of two child nodes, whereas any node in a multi-branch tree can have any number of child nodes.

■ A5

1 mark for explaining encapsulation and 1 mark for relating it to Node:

The Node class contains private attributes with public accessor/mutator methods. This means that they cannot be directly referenced for read/write access, instead forcing the use of the methods.

■ A6

1 mark for each:

Tree, Node, int/integer, String/string.

■ A7

1 mark for:

`GreekTree.GetRoot().GetRight().GetLeft().GetValue();`

■ A8

2 marks (1 mark for explaining it would throw an exception, 1 mark for saying null reference exception). An exception would be thrown. There is no node, so it would be a null reference exception.

```
Console.WriteLine("Further down on the left is " + GreekTree.GetRoot().GetLeft().GetLeft().GetValue());  
  
// A7  
GreekTree.GetRoot().GetRight().GetLeft().GetValue();  
  
// NullReferenceException was thrown  
An unhandled exception of type 'System.NullReferenceException' occurred in 'Ex5SecA.exe'
```

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■ A9

1 mark for giving the correct depth-first (post-order) tree traversal:

4, 2, 3, 1

■ A10

1 mark for giving the correct depth-first (pre-order) tree traversal:

1, 2, 4, 3

■ A11

1 mark for giving the correct depth-first (in-order) tree traversal:

4, 2, 1, 3

■ A12

1 mark for giving the correct depth-first (post-order) tree traversal:

1, 2, 3, 4

SECTION B

■ B1

3 marks for the method; 1 mark for the test code:

In Node.cs:

```

58      // B1
59      public void PrintNode()
60      {
61          Console.WriteLine("The value held in this node is:");
62
63          if (Left != null)
64          {
65              Console.WriteLine("There is no node to its left");
66          }
67          else
68          {
69              Console.WriteLine("To its left is the value:");
70          }
71
72          if (Right == null)
73          {
74              Console.WriteLine("There is no node to its right");
75          }
76          else
77          {
78              Console.WriteLine("To its right is the value:");
79          }
80      }

```

In Program.cs:

```

33      Console.WriteLine("-----ALPHA-----");
34      Alpha.PrintNode();
35      Console.WriteLine("-----BETA-----");
36      Beta.PrintNode();
37      Console.WriteLine("-----GAMMA-----");
38      Gamma.PrintNode();
39      Console.WriteLine("-----DELTA-----");
40      Delta.PrintNode();

```

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■ B2

1 mark for instantiating the new nodes; 3 marks for assembling the tree:

In Program.cs:

```

42      // B2
43      Node Epsilon = new Node(5);
44      Node Zeta = new Node(6);
45      Node Eta = new Node(7);
46      Node Kappa = new Node(8);
47      Node Xi = new Node(9);
48      Node Omicron = new Node(15);
49      Omicron.SetRight(Epsilon);
50      Omicron.SetLeft(Zeta);
51      Omicron.SetRight(Eta);
52      Epsilon.SetLeft(Kappa);
53      Eta.SetLeft(Xi);
54      Eta.SetRight(Omicron);

```

■ B3

1 mark for instantiating a new Tree, 1 mark for instantiating both Gold and Shoe, 1 mark for adding Gold and Shoe into the new Tree correctly, 1 mark for correct output:

```

56      // B3
57      Node Gold = new Node(24);
58      Node Shoe = new Node(8);
59      Tree AssortedTree = new Tree(Gold);
60      Gold.SetRight(Shoe);
61      Console.WriteLine("----- Gold -----");
62      Gold.PrintNode();

```

■ B4

5 marks awarded for modifying the code as shown (or equivalent code):

Marks are awarded for:

- creating a PostOrderTraversal procedure that takes a Node object as parameter
- implementing the IF structure correctly to handle null values (leaf nodes)
- performing a recursive call by passing the left/right node
- displaying all values in the tree in the correct order for depth-first, post-order
- appropriately modifying the main program procedure

```

142      // B4
143      public static void PostOrderTraversal(Node SubtreeRoot)
144      {
145          if (SubtreeRoot != null)
146          {
147              PostOrderTraversal(SubtreeRoot.GetLeft());
148              PostOrderTraversal(SubtreeRoot.GetRight());
149              Console.Write(SubtreeRoot.GetValue() + " > ");
150          }
151      }

```

```

63
64      // B4
65      Console.WriteLine("\n>>>> POST-ORDER TRAVERSAL: Greek Tree");
66      PostOrderTraversal(GreekTree.GetRoot());
67      Console.WriteLine("\n>>>> POST-ORDER TRAVERSAL: Assorted Tree");
68      PostOrderTraversal(AssortedTree.GetRoot());
69

```

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■ B5

5 marks available for modifying the code as shown (or equivalent code):

Marks are awarded for:

- creating a `PreOrderTraversal` procedure that takes a `Node` object as input
- implementing the IF structure correctly to handle null values (leaf nodes)
- performing a recursive call by passing the left/right node
- displaying all values in the tree in the correct order for depth-first, pre-order
- appropriately modifying the main program procedure

```

153 // B5
154 public static void PreOrderTraversal(Node SubtreeRoot)
155 {
156     if (SubtreeRoot != null)
157     {
158         Console.Write(SubtreeRoot.GetValue() + " > ");
159         PreOrderTraversal(SubtreeRoot.GetLeft());
160         PreOrderTraversal(SubtreeRoot.GetRight());
161     }
162 }

```

```

70 // B5
71 Console.WriteLine("\n>>>> PRE-ORDER TRAVERSAL: Greek");
72 PreOrderTraversal(GreekTree.GetRoot());
73 Console.WriteLine("\n>>>> PRE-ORDER TRAVERSAL: Assorted");
74 PreOrderTraversal(AssortedTree.GetRoot());
75

```

■ B6

5 marks available for modifying the code as shown (or equivalent code):

Marks are awarded for:

- creating an `InOrderTraversal` procedure that takes a `Node` object as input
- implementing the IF structure correctly to handle null values (leaf nodes)
- performing a recursive call by passing the left/right node
- displaying all values in the tree in the correct order for depth-first, post-order
- appropriately modifying the main program procedure

```

164 // B6
165 public static void InOrderTraversal(Node SubtreeRoot)
166 {
167     if (SubtreeRoot != null)
168     {
169         InOrderTraversal(SubtreeRoot.GetLeft());
170         Console.Write(SubtreeRoot.GetValue() + " > ");
171         InOrderTraversal(SubtreeRoot.GetRight());
172     }
173 }

```

```

76
77 Console.WriteLine("\n>>>> IN-ORDER TRAVERSAL: Greek");
78 InOrderTraversal(GreekTree.GetRoot());
79 Console.WriteLine("\n>>>> IN-ORDER TRAVERSAL: Assorted");
80 InOrderTraversal(AssortedTree.GetRoot());

```

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7 marks available for modifying the code as shown (or equivalent code):

Marks could be awarded for the bullets shown:

- [1] Create 2 lists of Node objects: one for the current level and one for the next level
- [1] Handle empty trees to improve this method's robustness
 - Output a message
 - Return/Exit
- [1] Initialise the list of nodes at this level with the root of the tree passed in
- [1] While a level with nodes has not yet been encountered...
 - [1] Form a new empty list for the next level's nodes
 - Visit all the nodes in the list
 - Output the value found at each node
 - If the node has a left/right node further down the tree, add it to the next level's list
 - [1] Having visited all this level's nodes, set the next level's list to be the current level's list

```

176 public static void BreadthFirstTraversal(Node SubtreeRoot)
177 {
178     // Create 2 lists of Node objects: one for the current level and one
179     List<Node> NodesAtThisLevel = new List<Node>();
180     List<Node> NodesAtNextLevel;
181
182     // Handle empty trees to improve this method's robustness
183     if (SubtreeRoot == null)
184     {
185         Console.WriteLine("This tree is empty.");
186         return;
187     }
188
189     // Initialise the list of nodes at this level with the root of the tree
190     NodesAtThisLevel.Add(SubtreeRoot);
191
192     // While a level with nodes has not yet been encountered...
193     while (NodesAtThisLevel.Count > 0)
194     {
195         // Form a new empty list for the next level's nodes
196         NodesAtNextLevel = new List<Node>();
197
198         // Visit all the nodes in the list
199         for (int pointer = 0; pointer < NodesAtThisLevel.Count; pointer++)
200         {
201             // Output the value found at each node
202             Console.Write(NodesAtThisLevel[pointer].GetValue() + " > ");
203
204             // If the node has a left/right node further down the tree, add it
205             if (NodesAtThisLevel[pointer].GetLeft() != null)
206             {
207                 NodesAtNextLevel.Add(NodesAtThisLevel[pointer].GetLeft());
208             }
209             if (NodesAtThisLevel[pointer].GetRight() != null)
210             {
211                 NodesAtNextLevel.Add(NodesAtThisLevel[pointer].GetRight());
212             }
213         }
214
215         // Having visited all this level's nodes, set the next level's list
216         NodesAtThisLevel = NodesAtNextLevel;
217     }
218 }
    
```

```

82 // B7
83 Console.WriteLine("\n>>>> BREADTH FIRST TRAVERSAL:");
84 BreadthFirstTraversal(GreekTree.GetRoot());
85 Console.WriteLine("\n>>>> BREADTH FIRST TRAVERSAL:");
86 BreadthFirstTraversal(AssortedTree.GetRoot());
    
```

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14 marks available for modifying the code as shown (or equivalent code):

- [1] taking in three parameters: int[], int, int
- [1] handling null, length=0 and Lo>Hi
- [1] calculating middle index
- [1] deriving mid-value
- [1] initialising a new node with the mid-value
- [1] setting the left subtree's node
- [1] setting the right subtree's node
- [1] return statement
- [1] overloading correctly
- [2] creating a one-parameter version of the method with one OR only
- [1] setting Lo and Hi automatically
- [1] Main calls the method
- [1] Main performs all four traversals

```

220 // B8
221 public static Node ConstructBinarySearchTree(int[] SortedArray, int Lo
222 {
223     // Handle empty arrays and null pointers as well as cases where
224     if (SortedArray == null || SortedArray.Length == 0 || Lo > Hi)
225     {
226         return null;
227     }
228
229     int MidIndex = (Lo + Hi) / 2;
230     int MidValue = SortedArray[MidIndex];
231
232     Node NewNode = new Node(MidValue);
233
234     NewNode.SetLeft(ConstructBinarySearchTree(SortedArray, Lo, MidIndex));
235     NewNode.SetRight(ConstructBinarySearchTree(SortedArray, MidIndex + 1, Hi));
236
237     return NewNode;
238 }

```

```

240
241 public static Node ConstructBinarySearchTree(int[] SortedArray)
242 {
243     if (SortedArray == null || SortedArray.Length == 0)
244     {
245         return null;
246     }
247
248     Node NewNode = ConstructBinarySearchTree(SortedArray, 0, SortedArray.Length - 1);
249     return NewNode;
250 }

```

```

88 // B8
89 int[] NumberList = { 1, 2, 3, 4, 5, 6, 7, 8 };
90 Tree BST = new Tree(ConstructBinarySearchTree(NumberList));
91 Console.WriteLine("\n>>> POST-ORDER TRAVERSAL: BST");
92 PostOrderTraversal(BST.GetRoot());
93 Console.WriteLine("\n>>> PRE-ORDER TRAVERSAL: BST");
94 PreOrderTraversal(BST.GetRoot());
95 Console.WriteLine("\n>>> IN-ORDER TRAVERSAL: BST");
96 InOrderTraversal(BST.GetRoot());
97 Console.WriteLine("\n>>> BREADTH-FIRST TRAVERSAL: BST");
98 BreadthFirstTraversal(BST.GetRoot());

```

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6 marks available for modifying the code as shown (or equivalent code):

Marks are awarded for:

- creating a `SearchBST` function that takes a search value and node as input
- handling nulls
- returning `True` if the value is found
- recursively checking the left subtree
- recursively checking the right subtree
- providing intelligible output from the main program

```

252 // B9
253 public static bool SearchBST(Node BSTRoot, int SoughtValue)
254 {
255     if (BSTRoot == null)
256     {
257         return false;
258     }
259
260     if (BSTRoot.GetValue() == SoughtValue)
261     {
262         return true;
263     }
264
265     if (BSTRoot.GetValue() > SoughtValue)
266     {
267         return SearchBST(BSTRoot.GetLeft(), SoughtValue);
268     }
269
270     return SearchBST(BSTRoot.GetRight(), SoughtValue);
271 }

```

```

100
101 Console.WriteLine("\n>>> BST SEARCH: Does BST contain 6?");
102 Console.WriteLine(SearchBST(BST.GetRoot(), 6));
103 Console.WriteLine("\n>>> BST SEARCH: Does BST contain 7?");
104 Console.WriteLine(SearchBST(BST.GetRoot(), 7));
105 Console.WriteLine("\n>>> BST SEARCH: Does BST contain 8?");
106 Console.WriteLine(SearchBST(BST.GetRoot(), 8));
107 Console.WriteLine("\n>>> BST SEARCH: Does BST contain 9?");
108 Console.WriteLine(SearchBST(BST.GetRoot(), 9));
109 Console.WriteLine("\n>>> BST SEARCH: Does BST contain 0?");
110 Console.WriteLine(SearchBST(BST.GetRoot(), 0));

```

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■ B10

3 marks per correctly sorted program:

```

273 // B10
274 public static List<int> InOrderListBuilder(Node SubtreeRoot)
275 {
276     if (SubtreeRoot != null)
277     {
278         InOrderListBuilder(SubtreeRoot.GetLeft(), CurrentList);
279         CurrentList.Add(SubtreeRoot.GetValue());
280         InOrderListBuilder(SubtreeRoot.GetRight(), CurrentList);
281     }
282     return CurrentList;
283 }
284
285 // B10
286 public static Tree ConvertToBST(Node RootOfUnsortedTree)
287 {
288     // [1] Turn the tree into a list (use in-order traversal)
289     List<int> ListFormat = new List<int>();
290     ListFormat = InOrderListBuilder(RootOfUnsortedTree, ListFormat);
291
292     // [2] Sort the list
293     ListFormat.Sort();
294
295     // [3] Convert it into a BST
296     Node NewTreeRoot = ConstructBinarySearchTree(ListFormat);
297     Tree NewBST = new Tree(NewTreeRoot);
298     return NewBST;
299 }

```

```

112 // B10
113 List<int> ListFormat = new List<int>();
114 ListFormat = InOrderListBuilder(GreekTree.GetRoot(), x);
115 foreach (int i in x)
116 {
117     Console.Write(i + " > ");
118 }

```

■ B11

6 marks for the AddNode method developed from the breadth-first traversal method

Marks are awarded for:

- [1] adding to the root when the Tree is a null pointer
- [1] using return and the Tree data type
- [1] retaining the WHILE loop
- [1] retaining the FOR loop
- [2] adding the two ELSE blocks which include return statements

5 marks for the correct code in the Print method:

Marks are awarded for:

- [1] using new or more new nodes to AssortedTree
- [1] creating and initialising a new BST
- [1] deriving the BST values from AssortedTree
- [1] outputting all four traversals
- [1] correctness – the in-order traversal should be SORTED

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```

301 // 811
302 public static Tree AddNode(Tree TreeToBeAddedTo, Node NewNode)
303 {
304     // Create 2 lists of Node objects: one for the current level and one
305     List<Node> NodesAtThisLevel = new List<Node>();
306     List<Node> NodesAtNextLevel;
307
308     // Handle empty trees
309     if (TreeToBeAddedTo == null)
310     {
311         TreeToBeAddedTo.SetRoot(NewNode);
312         return TreeToBeAddedTo;
313     }
314
315     // Initialize the list of nodes at this level with the root of the tree
316     NodesAtThisLevel.Add(TreeToBeAddedTo.GetRoot());
317
318     // While a level with no nodes has not yet been encountered...
319     while (NodesAtThisLevel.Count > 0)
320     {
321         // Form a new empty list for the next level's nodes
322         NodesAtNextLevel = new List<Node>();
323
324         // Visit all the nodes in the list
325         for (int pointer = 0; pointer < NodesAtThisLevel.Count; pointer++)
326         {
327             // If the node has a left/right node further down the tree,
328             if (NodesAtThisLevel[pointer].GetLeft() != null)
329             {
330                 NodesAtNextLevel.Add(NodesAtThisLevel[pointer].GetLeft());
331             }
332             else
333             {
334                 NodesAtThisLevel[pointer].SetLeft(NewNode);
335                 return TreeToBeAddedTo;
336             }
337             if (NodesAtThisLevel[pointer].GetRight() != null)
338             {
339                 NodesAtNextLevel.Add(NodesAtThisLevel[pointer].GetRight());
340             }
341             NodesAtThisLevel[pointer].SetRight(NewNode);
342             return TreeToBeAddedTo;
343         }
344     }
345
346     // Having visited all this level's nodes, set the next level's list
347     NodesAtThisLevel = NodesAtNextLevel;
348 }
349
350 return TreeToBeAddedTo; // never used but has to be here for completeness
351 }

```

```

120 // 811
121 AssortedTree = AddNode(AssortedTree, new Node(8420));
122 AssortedTree = AddNode(AssortedTree, new Node(-19));
123 AssortedTree = AddNode(AssortedTree, new Node(71));
124 AssortedTree = AddNode(AssortedTree, new Node(333));
125
126 Tree AssortedBST = ConvertToBST(AssortedTree.GetRoot()); // call
127
128 Console.WriteLine("POST-ORDER TRAVERSAL: AssortedBST >>>");
129 PostOrderTraversal(AssortedBST.GetRoot());
130 Console.WriteLine("\n>>> PRE-ORDER TRAVERSAL: AssortedBST >>>");
131 PreOrderTraversal(AssortedBST.GetRoot());
132 Console.WriteLine("\n>>> IN-ORDER TRAVERSAL: AssortedBST >>>");
133 InOrderTraversal(AssortedBST.GetRoot());
134 Console.WriteLine("\n>>> BREADTH-FIRST TRAVERSAL: AssortedBST >>>");
135 BreadthFirstTraversal(AssortedBST.GetRoot());
136
137 Console.ReadKey(); // holder
138 }

```

EXERCISE 7 – DIJKSTRA'S SHORTEST PATH

SECTION A

■ A1

1 mark for correctly counting uses of the 'new' keyword:

25

■ A2

1 mark for:

Line 100

■ A3

2 marks (1 mark for a suitable definition; 1 mark for giving a valid reason to use private)

A public attribute is a (class or instance) variable that can be accessed from outside the class. It is made private to prevent it from being accidentally changed by other parts of the program.

Alternative reason: it enables encapsulation of the entire class, meaning that you don't have to worry about the details of how the class has been implemented (as an external user).

■ A4

1 mark for each appropriate comment given:

Program.cs Line 30:

A new edge [1] is built

... to connect node G to node H [1]

... one-way only [1]

... and it is assigned a weight of 10 [1].

■ A5

1 mark for each appropriate comment given:

Graph.cs Lines 16–19:

A new graph is made [1] (this is a constructor)

... but no parameters are passed in [1]

... so only an empty list of edges is created [1].

■ A6

10 marks (1 mark per useful point):

1. The method takes in one node and returns its closest node. [1]
2. If the node passed in as a parameter is null, return *Null* immediately. [1]
3. If the node sits on its own and there are no edges in the digraph, then return the node. [1]
4. Next, the program iterates through all of the edges in the digraph and builds a temporary list of edges that are connected directly to the node being investigated (*NodeToCheck*). It is called *EmanatingEdges* and checks two possibilities:
 - a. that the start node along that edge is the one being investigated
 - b. that the end node along that edge is the one being investigated, but only if it is a one-way edge, in which case it would be relevant to include it [1]
5. In the event that none of the edges in the temporary list (*EmanatingEdges*) are connected to the node being investigated, a *Null* is returned as no node exists as a meaningful answer. [1]
6. Otherwise, the program will firstly output the temporary list of all of the edges. [1]
7. It will then iterate through the list of edges and continuously overwrite the *temporaryEdge* variable with the edge it finds to be shorter than previous ones. [1] In order to do this, the *temporaryEdge* variable is given a high integer value so that any further comparison will be less than this. [1]
8. To determine the node to be returned from this function, it checks if the node being investigated (*NodeToCheck*) is at the beginning of the edge, in which case it returns the end node. Otherwise, it returns whichever node is at the beginning of the edge. [1]

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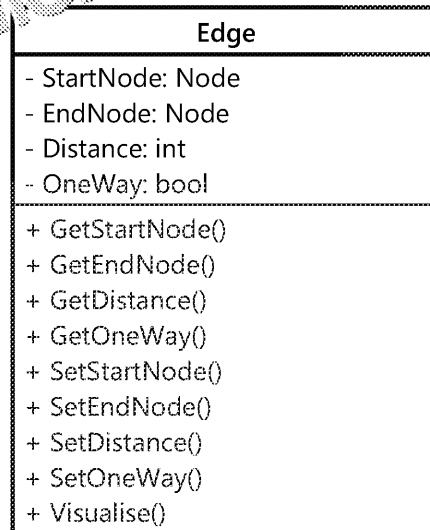


■ A7

1 mark for each of the following:

1. Rectangular shape with three parts for: class name, attributes, methods [1]
2. Class name = Edge [1]
3. Attributes = StartNode, EndNode, Distance, OneWay [1]. Data types shown
4. Methods = 4× Get, 4× Set, Visualise [1]

Constructors can be omitted. Visibility settings can be provided but all attributes are public, indicated by – and + respectively below. Parameters can be omitted.



■ A8

2 marks (1 mark for explaining what a graph is; 1 mark for explaining the features of a graph)
 A graph is a data type that consists of a set of nodes and a set of edges that connect the nodes. A tree graph contains no loops and no two nodes are connected by more than one edge.

■ A9

1 mark for explaining the purpose of Dijkstra's shortest path algorithm:

Dijkstra's shortest path algorithm is used to find the shortest path between two nodes in a graph.

■ A10

4 marks (1 mark for describing how all edges from the start node are checked; 1 mark for how the closest node to the start node is selected; 1 mark for describing how nodes are not revisited; 1 mark for describing how the end node is reached once the end node is visited):

Dijkstra's algorithm starts at the given start node. All edges connected to this node are checked and the closest node to the start node is selected. The edges connected to the new node are checked and the closest node to the start node is selected. The process repeats until the given end node is reached. The algorithm keeps a note of the path that was taken to reach this node and visits whichever node is closest to the start node and hasn't already been visited. This process repeats until the given end node is reached.

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SECTION B

■ B1

1 mark available for each part of the modification (or equivalent code):

- creating six node objects [1]
- creating seven edge objects [1]
- creating and populating a graph object with all edges [1]
- setting the start and end nodes as A and F respectively [1]

```
9 // B1
10 Node NodeA = new Node('A');
11 Node NodeB = new Node('B');
12 Node NodeC = new Node('C');
13 Node NodeD = new Node('D');
14 Node NodeE = new Node('E');
15 Node NodeF = new Node('F');
16
17 Edge EdgeAB = new Edge(NodeA, NodeB, 4, true);
18 Edge EdgeAC = new Edge(NodeA, NodeC, 2, true);
19 Edge EdgeBC = new Edge(NodeB, NodeC, 5, true);
20 Edge EdgeBD = new Edge(NodeB, NodeD, 10, true);
21 Edge EdgeCE = new Edge(NodeC, NodeE, 3, true);
22 Edge EdgeED = new Edge(NodeE, NodeD, 4, true);
23 Edge EdgeDF = new Edge(NodeD, NodeF, 11, true);
24
25 Graph Map = new Graph();
26 Map.AddEdge(EdgeAB);
27 Map.AddEdge(EdgeAC);
28 Map.AddEdge(EdgeBC);
29 Map.AddEdge(EdgeBD);
30 Map.AddEdge(EdgeCE);
31 Map.AddEdge(EdgeED);
32 Map.AddEdge(EdgeDF);
33
34 Map.SetSourceNode(NodeA);
35 Map.SetTargetNode(NodeF);
```

■ B2

1 mark available for modifying Program.cs as shown without rewriting any code block

```
37 // B2
38 Map.VisualiseAll();
```

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■ B3

5 marks available for modifying the code as shown (or equivalent code):

Marks should be awarded for:

- calling the `GetClosestNode` method
- handling the case where `GetClosestNode` returns a null value
- handling the case where a node is returned
- correctly calling the new method from `Main()`
- correct use of private, static and parameters

```

40 // B3
41 /*
42 Console.WriteLine("The closest node to A is " + Map.GetClosestNode(NodeA));
43 Console.WriteLine("The closest node to B is " + Map.GetClosestNode(NodeB));
44 Console.WriteLine("The closest node to C is " + Map.GetClosestNode(NodeC));
45 Console.WriteLine("The closest node to D is " + Map.GetClosestNode(NodeD));
46 Console.WriteLine("The closest node to E is " + Map.GetClosestNode(NodeE));
47 // BUG // Console.WriteLine("The closest node to F is " + Map.GetClosestNode(NodeF));
48 */
49 OutputClosestNode(Map, NodeA);
50 OutputClosestNode(Map, NodeB);
51 OutputClosestNode(Map, NodeC);
52 OutputClosestNode(Map, NodeD);
53 OutputClosestNode(Map, NodeE);
54 OutputClosestNode(Map, NodeF);

```

```

118 // B3
119 private static void OutputClosestNode(Graph GivenGraph, Node GivenNode)
120 {
121     Node CloseNode = GivenGraph.GetClosestNode(GivenNode);
122
123     if (CloseNode == null)
124     {
125         Console.WriteLine("No nodes found for " + GivenNode.GetLetter() + ".");
126     }
127     else
128     {
129         Console.WriteLine("The closest node to " + GivenNode.GetLetter() + " is " + CloseNode.GetLetter());
130     }
131 }

```

■ B4

3 marks per correctly completed table; Section A may proceed to visit row H (albeit with 1 mark per correct path stated at the end)

Section A

Node	Visited?	Shortest Distance to Start Node	Path
A	V	0	-
B	V	$\infty \rightarrow 2$	A
C	V	$\infty \rightarrow 10$	B
D	V	$\infty \rightarrow 4$	A
E	V	$\infty \rightarrow 11$	D
F	V	$\infty \rightarrow 5$	B
G	V	$\infty \rightarrow 11$	D
H	V	$\infty \rightarrow 21$	G
I	V	$\infty \rightarrow 24 \rightarrow 20$ MINIMUM VALUE FOUND	G \rightarrow H

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Section B

Node	Visited?	Shortest Distance to Start Node	Previous Node
A	V	0	-
B	V	$\infty \rightarrow 4$	A
C	V	$\infty \rightarrow 2$	A
D	V	$\infty \rightarrow 14 \rightarrow 9$	B \rightarrow
E	V	$\infty \rightarrow 5$	C
F		$\infty \rightarrow 20$ MINIMUM VALUE FOUND	D

- Section B: Shortest path from A to I = A, B, F, I [1]
- Section B: Shortest path from A to F = A, C, E, D, F [1]

Program modifications:

Steps (1) and (2)

1 mark for a correct list of attributes

1 mark for a complete set of accessors and mutators

TableRow.cs

```

1 namespace Ex7Sec8
2 {
3     // B4
4     public class TableRow
5     {
6         // Attributes
7         private Node RowNode;
8         private bool Visited;
9         private int ShortestDistanceToStart;
10        private Node PreviousNode;
11
12        // Constructor
13        public TableRow(Node NextRowNode)
14        {
15            RowNode = NextRowNode;
16            Visited = false;
17            ShortestDistanceToStart = int.MaxValue;
18            PreviousNode = null;
19        }
20
21        // Accessor Methods
22
23        public Node GetRowNode()
24        {
25            return RowNode;
26        }
    }
}

```

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```

27
28     public bool GetVisited()
29     {
30         return Visited;
31     }
32
33     public int GetShortestDistanceToStart()
34     {
35         return ShortestDistanceToStart;
36     }
37
38     public Node GetPreviousNode()
39     {
40         return PreviousNode;
41     }
42
43     // Mutator Methods
44
45     public void SetRowNode(Node NewRowNode)
46     {
47         RowNode = NewRowNode;
48     }
49

```

```

49
50     public void SetVisited()
51     {
52         Visited = true; // included for convenience
53     }
54
55     public void SetVisited(bool NewVisitedValue)
56     {
57         Visited = NewVisitedValue;
58     }
59
60     public void SetShortestDistanceToStart(int NewTotalDistance)
61     {
62         // NB: This method does not perform the addition
63         ShortestDistanceToStart = NewTotalDistance;
64     }
65
66     public void SetPreviousNode(Node NewPreviousNode)
67     {
68         PreviousNode = NewPreviousNode;
69     }
70 }
71

```

Step (3)

4 marks for successfully implementing all parts of the algorithm in C#

1 mark lost per area of difficulty encountered, i.e. not achieved

```

152 // B4
153 private List<TableRow> GetTableRowTable()
154 {
155     List<Node> h1Nodes = new List<Node>();
156     Node MightBeAdded;
157
158     foreach (Edge Ed in Diagram)
159     {
160         Node MightBeAdded = Ed.GetStartNode();
161         if (!TableNodes.Contains(NodeMightBeAdded))
162         {
163             TableNodes.Add(NodeMightBeAdded);
164         }
165
166         Node MightBeAdded = Ed.GetEndNode();
167         if (!TableNodes.Contains(NodeMightBeAdded))
168         {
169             TableNodes.Add(NodeMightBeAdded);
170         }
171     }
172
173     List<TableRow> Table = new List<TableRow>();
174

```

```

173     List<TableRow> Table = new List<TableRow>();
174
175     foreach (Node Nod in TableNodes)
176     {
177         Table.Add(new TableRow(Nod));
178         if (SourceNode == Nod)
179         {
180             Table[Table.Count - 1].SetShortestDistance(0);
181         }
182     }
183
184     return Table;
185 }
186

```

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Step (4)

6 marks for successfully implementing all parts of the algorithm in C#

1 mark lost per area of difficulty encountered, i.e. not achieved

```
11 private Node SourceNode;
12 private Node TargetNode;
13 private List<TableRow> DijkstraTable; // B4 Step
14
15 // Constructors
16
17 public Graph()
18 {
19     Diagram = new List<Edge>();
20     DijkstraTable = GetCurrentTable(); // B4 Step
21 }
22
23 public Graph(List<Edge> NewGraphDiagram, Node NewSourceNode, Node NewTargetNode)
24 {
25     Diagram = NewGraphDiagram;
26     SourceNode = NewSourceNode;
27     TargetNode = NewTargetNode;
28     DijkstraTable = GetCurrentTable(); // B4 Step
29 }
```

```
36 public void SetDiagram(List<Edge> NewGraphDiagram)
37 {
38     Diagram = NewGraphDiagram;
39     DijkstraTable = GetCurrentTable(); // B4 Step
40 }
41
42 public void SetSourceNode(Node NewSourceNode)
43 {
44     SourceNode = NewSourceNode;
45     DijkstraTable = GetCurrentTable(); // B4 Step
46 }
47
48 public void SetTargetNode(Node NewTargetNode)
49 {
50     TargetNode = NewTargetNode;
51     DijkstraTable = GetCurrentTable(); // B4 Step
52 }
53
54 // Miscellaneous Methods
55
56 public void AddEdge(Edge NewEdge)
57 {
58     Diagram.Add(NewEdge);
59     DijkstraTable = GetCurrentTable(); // B4 Step
60 }
61 }
```

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Step (5)

6 marks for successfully implementing all parts of the algorithm in C#

1 mark lost per area of difficulty encountered, i.e. not achieved

```

187 // B4 Step (5)
188 public void PrintTable()
189 {
190     // Headings
191     Console.WriteLine("-----CURRENT TABLE-----");
192     Console.WriteLine("Distance from START to node: SHORTEST DISTANCE TO START");
193
194     // For each row in the table
195     foreach (var row in DijkstraTable)
196     {
197         // Column 1: NODE
198         if (DijkstraTable[row].GetRowNode() == null)
199         {
200             Console.Write('_');
201         }
202         else
203         {
204             Console.Write(DijkstraTable[row].GetRowNode().GetLetter());
205         }
206         Console.Write("\t"); // to finish the column.
207
208         // Column 2: VISITED?
209         Console.Write(DijkstraTable[row].GetVisited()+"\t\t"); //
210
211         // Column 3: SHORTEST DISTANCE
212         ShortDis = DijkstraTable[row].GetShortestDistanceToStart();
213         if (ShortDis == int.MaxValue)
214         {
215             Console.Write("inf"); // infinity symbol
216         }
217         else
218         {
219             Console.Write(ShortDis);
220         }
221         Console.Write("\t\t\t"); // to finish the column.
222
223         // Column 4: PREVIOUS NODE
224         if(DijkstraTable[row].GetPreviousNode() == null)
225         {
226             Console.Write('\u0008'); // NULL symbol
227         }
228         else
229         {
230             Console.Write(DijkstraTable[row].GetPreviousNode().GetLetter());
231         }
232         Console.WriteLine(); // to finish the column AND move to next row
233     }
234     // Footer
235     Console.WriteLine("-----");
236 }

```

B5

1 mark available for each of the main bullet points in the question being fully implemented

Marks could be further:

- awarded as bonuses for coming up with original extensions/improvements
- awarded for excellent code style even if some areas required assistance
- deducted for very poor coding style

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■ B6

3 marks available for a complete, working implementation of the requirements, even example shown

Marks are awarded for:

- a correct method signature and return statement
- the correct deployment of IF and FOR
- accurate use of list indexing and method calls that carry out

```

277 // B6
278 public Node GetNextUnvisited()
279 {
280     int NotedIndex = int.MaxValue;
281     int MinimumDist = -1;
282
283     for(int i=0; i<DijkstraTable.Count; i++)
284     {
285         if(!DijkstraTable[i].GetVisited() && DijkstraTable[i].GetShortestDistanceToStart() < MinimumDist)
286         {
287             NotedIndex = i;
288             MinimumDist = DijkstraTable[i].GetShortestDistanceToStart();
289         }
290     }
291
292     return DijkstraTable[NotedIndex].GetRowNode();
293 }

```

■ B7

5 marks available for implementing the code as shown (or equivalent code):

Marks could be awarded for:

- [2] finding the relevant nodes which emanate from the given node in the diagram
- [2] isolating only those that have not yet been visited
- [1] implementing the quick check and returning a successful outcome

```

295 // B7
296 // Get all nodes that have NodeToCheck as their start or end node
297 // Allow X where: NodeToCheck ||-----> X
298 // Allow X where: NodeToCheck <-----> X
299 // Disallow X where: NodeToCheck <-----|| X
300 public List<Node> GetAllEmanatingNodes(Node NodeToCheck)
301 {
302     List<Node> EmanatingNodes = new List<Node>();
303
304     foreach (Edge E in Diagram)
305     {
306         // Allow X where: NodeToCheck ||-----> X
307         if (E.GetStartNode() == NodeToCheck && E.GetOneWay())
308         {
309             EmanatingNodes.Add(E.GetEndNode());
310         }
311
312         // Allow X where: NodeToCheck <-----> X
313         else if (!E.GetOneWay() && (E.GetStartNode() == NodeToCheck || E.GetEndNode() == NodeToCheck))
314         {
315             if (E.GetStartNode() == NodeToCheck)
316             {
317                 EmanatingNodes.Add(E.GetEndNode());
318             }
319             else if (E.GetEndNode() == NodeToCheck)
320             {
321                 EmanatingNodes.Add(E.GetStartNode());
322             }
323         }
324     }
325 }

```

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```

323     }
324 }
325
326 // Now inspect the table to eliminate any visited nodes
327 int Counter = 0;
328 int LocationIndexOfNode;
329 while (Counter < EmanatingNodes.Count)
330 {
331     // Locate this node in the table
332     LocationIndexOfNode = ConvertNodeToRowNumber(Node);
333
334     if (DijkstraTable[LocationIndexOfNode].GetVisited())
335     {
336         EmanatingNodes.RemoveAt(Counter--);
337     }
338
339     Counter++;
340 }
341
342 // B7 quick check:
343 Console.WriteLine("++++++ Checking the Get All Emanating Nodes");
344 if (EmanatingNodes.Count == 0)
345 {
346     Console.WriteLine("No emanating nodes exist");
347     return null;
348 }
349 foreach (Node N in EmanatingNodes)
350 {
351     Console.WriteLine("NODE " + N.GetLetter());
352 }
353
354 return EmanatingNodes;
355 }

```

■ B8

3 marks available for modifying the code as shown (or equivalent code):

Marks could be awarded for:

- iterating through all rows
- appropriately checking for the equality of two objects
- handling the return statement, including consideration of possible errors

```

434 // B8
435 public int ConvertNodeToRowNumber(Node GivenN)
436 {
437     intRowIndex = -1;
438
439     for (int i = 0; i < DijkstraTable.Count; i++)
440     {
441         if (DijkstraTable[i].RowNode().Equals(GivenN))
442         {
443             return i;
444         }
445     }
446
447     if (RowIndex == -1) { Console.WriteLine(":(");
448     return RowIndex;
449 }

```

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```

416         DijkstraTable[TableRowIndex].SetVisited(true);
417
418         // If target node has been reached, flag it
419         if (Current == TargetNode)
420         {
421             TargetNodeNotVisited = false;
422         }
423
424         // On next iteration, use the node which value has the min
425         Current = GetClosestNode(Current);
426
427         Console.WriteLine("\n\n");
428         PrintTable();
429     }
430
431     // THIS TABLE REPRESENTS THE SHORTEST PATH
432
433

```



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EXERCISE 8 – BOMB SEARCH

SECTION A

■ A1

1 mark for:

`GetMove()`

■ A2

1 mark for:

Class name: Program

Line number: 15

■ A3

3 marks for:

The number of bombs that will be present/placed on the board... [1]

... will be one fifth of the total number of tiles...[1]

... but this is a DIV operation, so it will truncate any decimals [1] (it won't be exactly)

■ A4

3 marks for:

All new tiles are, by default, set to be hidden (not revealed) [1]

... and the number of adjacent bombs cannot yet be known, so it defaults to 0 [1]

... but whether it is a bomb or not can be passed in as a parameter [1].

■ A5

1 mark for explaining one reason why the redundant code is useful, not how it works

During the game, tiles will be regularly revealed, so this use of the method is intended to require the programmer to pass in any parameter. Flipping a tile is not a feature of the game even if there is no `SetReveal()` method.

■ A6

1 mark for explaining why it is an overflow exception, or more precisely:

`System.OverflowException`

■ A7

2 marks (1 mark for explaining how try-catch statements work, and 1 mark for explaining why they are useful in this case):

[1] How it works: Try-catch statements are used to handle errors by attempting to run the code in the catch block instead if an error is thrown within the try block.

[1] In this case: If a `System.OverflowException` arises because negative numbers are used, the program can exit cleanly or request input from the user to prevent it from crashing.

■ A8

2 marks for:

A list can contain any number of elements, [1]

... whereas an array has a fixed size (it is immutable). [1]

Also: The size of an array is stored as a constant, but when working with lists a method is used to set its size at run-time.

■ A9

Any 2 marks for explaining the following:

While it would still work, [1]

... the grid structure of the game board is suited to an immutable array [1]

... as it will never need to grow/shrink during the game [1]

... and arrays offer all of the structural features required [1].

Lists could perhaps be useful if adding advanced features later such as hidden zones.

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■ A10

1 mark for writing the correct code:

```
Arena.GetLength(1);
```

SECTION B

■ B1

5 marks available for the code as shown (or equivalent code):

- [1] for outputting revealed bombs
- [1] for outputting hidden bombs
- [1] for outputting the number of adjacent bombs
- [1] for the style and clarity of output, e.g. meaningful sentences, not raw numbers
- [1] for suitable test code being added to `Program.cs`

■ B2

8 marks available for modifying the code as shown (or equivalent code):

- [1] per correctly functioning accessor method with suitable return type and parameters
- [1] per correctly functioning mutator method with void return type and one parameter

■ B3

16 marks available for modifying the code as shown (or equivalent code):

Marks are awarded for:

- [1] using the variable `Bombs` to make a list of Bomb tiles of the correct length
- [1] using `Rows*Cols-Bombs` to make a list of Safe tiles
- [1] creating an empty shuffled list
- [1] establishing a WHILE loop with the criteria joined using AND
- [1] implementing random selection (thus achieving shuffling)
- [1] adding the correct tile to the shuffled list each time
- [1] removing the correct tile from the correct list each time
- [1] adding any leftover elements from the correct list after one list is empty
- [1] placing the tiles into the 2D array `Arena`
- [7] for building and applying a method for updating the adjacent bomb values
the algorithm (described in the task) being achieved

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8 marks available for modifying the code as shown (or equivalent code):

Marks could be awarded for:

- [1] displaying B for a bomb
- [1] displaying a single digit for how many bombs surround a tile
- [1] for partitioning the rows
- [1] for partitioning the columns
- [1] for displaying row numbers
- [1] for displaying column numbers
- [2] for the DisplayGameBoard method showing ? symbols and spaces

```

198 public void DisplayBoard()
199 {
200     // Bold overline the entire grid
201     Console.WriteLine("\n=====");
202     for (int c = 0; c < Cols; c++)
203     {
204         Console.WriteLine("=====");
205     }
206     Console.WriteLine();
207
208     // Output the column number in the heading
209     Console.WriteLine(" # |");
210     for(int c=0; c<Cols; c++)
211     {
212         Console.WriteLine(" "+c+" |");
213     }
214     Console.WriteLine();
215
216     // Underline the column number headings
217     Console.WriteLine("-----|");
218     for (int c = 0; c < Cols; c++)
219     {
220         Console.WriteLine("-----|");
221     }
222     Console.WriteLine();
223
224     for (int row = 0; row < Rows; row++)
225     {
226         // Display the row number on the left
227         Console.WriteLine(" " + row + " |");
228
229         // Output the tiles at each column position
230         for (int col = 0; col < Cols; col++)
231         {
232             if (Arena[row, col].IsBomb())
233             {
234                 Console.WriteLine(" B |");
235             }
236             else
237             {
238                 Console.WriteLine(" "+Arena[row,col]+" |");
239             }
240         }
241         Console.WriteLine();
242     }

```

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```

243         // Underline the row
244         Console.Write("-----|");
245         for (int c = 0; c < Cols; c++)
246         {
247             Console.Write("-----|");
248         }
249         Console.WriteLine();
250     }
251
252     // Bold underline the entire grid
253     Console.Write("-----");
254     for (int c = 0; c < Cols; c++)
255     {
256         Console.Write("-----");
257     }
258     Console.WriteLine();
259 }

```

For the DisplayGameBoard method:

```

262 public void DisplayGameBoard()
263 {
264     // Bold overline the entire grid
265     Console.Write("\n-----");
266     for (int c = 0; c < Cols; c++)
267     {
268         Console.Write("-----");
269     }
270     Console.WriteLine();
271
272     // Output the column numbers in the heading
273     Console.Write(" ");
274     for (int c = 0; c < Cols; c++)
275     {
276         Console.Write(" " + c + " |");
277     }
278     Console.WriteLine();
279
280     // Underline the column number headings
281     Console.Write("-----|");
282     for (int c = 0; c < Cols; c++)
283     {
284         Console.Write("-----|");
285     }
286     Console.WriteLine();
287
288     // Present the tile
289     int FoundBombs;
290     for (int row = 0; row < Rows; row++)
291     {
292         // Display the row number on the left
293         Console.Write(" " + row + "|");
294
295         // Output tiles at each column position along
296         // the row
297         for (int col = 0; col < Cols; col++)
298         {
299             if (Arena[row, col].GetRevealed())
300             {
301                 if (Arena[row, col].GetIsBomb())
302                 {
303                     Console.Write(" B |");
304                 }
305             }
306         }
307     }
308 }

```

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```

304         else
305         {
306             FoundBombs = Arena[row, col].GetAdjacent
307             if(FoundBombs == 0)
308             {
309                 Console.Write(" "); // leave a
310             }
311             else
312             {
313                 Console.Write(" " + Arena[row, col]
314             )
315             }
316         }
317     }

```



From Program.cs:

```

20         Game.DisplayBoard();
21         Game.DisplayGameBoard();
22     }

```

■ B5

6 marks available for programming the `GetMove()` function as shown below (or equivalent)

Marks could be awarded for:

- [1] per DO-WHILE (or alternative) to disallow progress until a valid value is entered
- [1] per use of TRY-CATCH to intercept invalid data types, max of [2] marks
- [1] for clear outputs to prompt the user throughout
- [1] for returning an array of two values

```

150         // B5
151         public int[] GetMove()
152         {
153             // tile chosen
154
155             Console.WriteLine("Enter the row number (0-" + (Rows - 1) + ") or column number (0-" + (Cols - 1) + ")");
156             int ChosenRow = -1;
157             do
158             {
159                 try
160                 {
161                     ChosenRow = int.Parse(Console.ReadLine());
162                     if (ChosenRow < 0 || ChosenRow >= Rows)
163                     {
164                         Console.WriteLine("Valid options are 0-" + (Rows - 1) + " for rows and 0-" + (Cols - 1) + " for columns");
165                     }
166                 }
167                 catch (FormatException fx)
168                 {
169                     Console.WriteLine("Please only enter integers. Try again.");
170                 }
171             } while (ChosenRow < 0 || ChosenRow >= Rows);

```



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```

174
175     Console.WriteLine("Enter the column number (0-" + (Cols - 1) + ")");
176     int ChosenCol = -1;
177     do
178     {
179         try
180         {
181             ChosenCol = int.Parse(Console.ReadLine());
182             if (ChosenCol < 0 || ChosenCol >= Cols)
183             {
184                 Console.WriteLine("Values entered are 0-" + Cols + " only.");
185             }
186         }
187         catch (FormatException)
188         {
189             Console.WriteLine("Please only enter integers. Try again.");
190         }
191     } while (ChosenCol < 0 || ChosenCol >= Cols);
192
193     int[] ChosenPosition = { ChosenRow, ChosenCol };
194     return ChosenPosition;
195 }
196

```

■ B6

8 marks available for modifying the code as shown (or equivalent code):

Marks could be awarded for:

- [1] calling `GetMove()`
- [1] displaying an appropriate message if the user selects a tile that has already been revealed, returning `False` in this case
- [1] revealing a tile chosen by the user if and only if it has not already been revealed
- [1] returning `True` if a bomb tile is revealed
- [1] returning `False` if a safe tile has been revealed
- [3] modifying the main program to continually display the state of the arena until the user chooses to reveal tiles

```

396
397 public bool Reveal()
398 {
399     int[] Coordinates = GetMove();
400
401     // Check if it was revealed previously
402     if (Arena[Coordinates[0], Coordinates[1]].GetRevealed())
403     {
404         Console.WriteLine("\nERROR: That tile has already been revealed.");
405         return false;
406     }
407
408     // Reveal that tile
409     Arena[Coordinates[0], Coordinates[1]].SetRevealed(true);
410
411     // Return whether it was a bomb
412     if (Arena[Coordinates[0], Coordinates[1]].GetIsBomb())
413     {
414         Console.WriteLine("\nBOMB STRUCK!!! GAME OVER!!!");
415         return true;
416     }
417
418     {
419         SafeTilesFound++; // B7
420         return false;
421     }
422 }

```

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From Program.cs:

```
23 // B6
24 bool BombStruck;
25
26 do
27 {
28     BombStruck = Game.Reveal(
29     Game.DisplayGameScreen());
30 } while(!BombStruck);
```

■ B7

6 marks available for modifying the code as shown (or equivalent code):

Marks could be awarded for:

- [1] adding a new counter variable as an instance attribute to Board.cs
- [1] adding a getter and setter method for the new attribute
- [1] adding an assignment statement to the constructor to initialise it to 0
- [1] incrementing the counter variable as part of the Reveal() method
- [2] amending the Main() method to use the new variable appropriately

NOTE: The program must NOT output success and failure messages simultaneously, make selections once all the safe tiles have been found.

```
8 // Attributes
9 private int Rows;
10 private int Cols;
11 private int Bombs;
12 private Tile[,] Arena;
13 private int SafeTilesFound; // B7
```

```
15 // Constructor
16 Board(int R, int C)
17 {
18     Rows = R;
19     Cols = C;
20     Arena = new Tile[R, C];
21     Bombs = R * C / 5;
22     SafeTilesFound = 0; // B7
23 }
```

```
46 // B7
47 public int GetSafeTilesFound()
48 {
49     return SafeTilesFound;
50 }
```

```
74 // B7
75 public void SetSafeTilesFound(int QtySafe)
76 {
77     SafeTilesFound = QtySafe;
78 }
79
```

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Within the function Board.Reveal():

```
408         // Reveal that tile
409         Arena[Coordinates[0], Coordinates[1]] = ' ';
410
411         // Return whether it was a bomb
412         if (Arena[Coordinates[0], Coordinates[1]] == 'B')
413         {
414             Console.WriteLine("Bomb STRUCK!");
415             return true;
416         }
417
418         SafeTilesFound++; // B7
419         return false;
420     }
421 }
422 }
```

From Program.cs:

```
23     // B6 & B7
24     bool BombStruck;
25     int SafeTilesToFind = Game.GetRows() * Game.GetCols() - Game.GetBombCount();
26     do
27     {
28         BombStruck = Game.Reveal();
29         Game.DisplayGameBoard();
30     } while (!BombStruck && Game.GetSafeTilesFound() < SafeTilesToFind);
31
32     if (Game.GetSafeTilesFound() == SafeTilesToFind)
33     {
34         Console.WriteLine("CONGRATULATIONS! YOU HAVE WON!!!\nNumber of\nGame.DisplayBoard();");
35     }
36
37     Console.WriteLine("*****The End*****");
38     Console.ReadKey(); // holder
39 }
```

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EXERCISE 9 – FILE HANDLING AND HASH TABLES

SECTION A

■ A1

1 mark for:

Line 52

■ A2

1 mark for giving a suitable line number:

Line 23 / Line 12

■ A3

2 marks (1 mark for any appropriate point made); for example:

In the `GenerateNewProductCode` method, the result of multiplying the barcode by 10,000 using MOD, so the highest value it could be is 9,999, which means that it result [1].

The category number is a single digit, and when it is multiplied by 10,000 it will produce 0000 [1].

When these two numbers are added, the original category number thus becomes a single digit. [1]

■ A4

2 marks (1 mark for each distinct relevant point):

A tuple is an immutable data structure where the values can be of various data types but cannot be modified.

■ A5

1 mark for explaining why a tuple may not be used; for example:

The `Quantity` field would have to change, which would mean constantly creating new tuples across, which is inefficient in terms of time and space.

The data types are all the same (long), so there is no need for the flexibility of other data types.

■ A6

1 mark for:

File

■ A7

2 marks (1 mark for explaining that a hash function is used to place the data; 1 mark for explaining that a new entry is created when multiple data entries are placed in the same location):

A hash function is used on the data to be stored to produce a number that corresponds to the location where the data will be stored. If there is already data at that position in the table (i.e. a collision), the data is appended to a list of data entries in that position in the table.

■ A8

a) 2 marks (1 mark for explaining that a hash function produces a value based on the given input; 1 mark for explaining that a hash function works only one way, i.e. that the output value can be calculated from the input but the input cannot be calculated from the output value):

A hash function is a function that produces a value within a certain limited range given a specific input. The original input cannot be calculated from the output value. The hash function is used to store data in hash files.

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- b) 2 marks (1 mark for explaining that a hash function generates collisions as the algorithm generates too wide a range of possible combinations to reduce storage space / table size; 1 mark for explaining that this would be very inefficient as all of the unused locations would still need to be available (a lot of memory/room):

This phenomenon is called a collision. [1]

A hash function is a function that produces a value which depends on the key for a range of values typically similar to the number of items that need to be stored. If the number of combinations for the key is too large, the algorithm generates too wide a range of values, which will be sparsely populated, which would be inefficient as that would require a lot of memory/room).

■ A9

2 marks for defining each term; 2 marks for comparative/contrasting remarks:

Serial files are appended with new data, so it is effectively organised into chronological order. Sequential files have their data inserted at a position determined by the relative position of some part of the data record can be compared with the other data records to determine the correct sequence.

Serial files require less complex insertion operations but can take a long time to search (random access is not possible, but linear searches $O(N)$ are).

Sequential files require more complex insert/delete operations, but they can be used for fast search performances.

■ A10

8 marks (-1 mark for each data entry not placed correctly)

Hash Table Location	First Entry	Other Entries
Table [0]	56551,395032849,1299,5,3	38399,439
Table [1]		
Table [2]		
Table [3]		
Table [4]	84097,373042803,2299,4,3	
Table [5]		
Table [6]		
Table [7]	58306,449598094,599,9,3	45857,948
Table [8]		
Table [9]	51565,534359435,1499,2,1	
Table [10]		
Table [11]		
Table [12]	94000,5849,399,12,7	30000,288
Table [13]		
Table [14]	77325,129819233,525,2,0	
Table [15]		
Table [16]	79250,976895865,4450,7,2	
Table [17]		
Table [18]		

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SECTION B

■ B1

1 mark available for commenting out code (using `//` or `/* */`) and 1 mark for creating precise name given:

```
10 {
11     // Test data to type in: CatNo=3, ProCode=439234001, ProductName=Antique
12     // Should yield Product Code=873
13     // log[] AntiqueProductInfo = HeadInNewProductInformation(ProCode, CatNo);
14     // ShowFactSheet(ProCode, CatNo, Zurasahandle);
```



■ B2

2 marks available for modifying the code as shown (or equivalent code):

Marks awarded for:

- correct method signature
- correct implementation of the hashing algorithm

```
89 // B2
90 private static long GenerateHashValue(long ProCode)
91 {
92     return (ProCode + ProCode / 29) % 19;
93 }
```

■ B3

2 marks available for modifying the code as shown (or equivalent code):

Marks could be awarded for:

- correctly inserting it in the same style as other lines
- calling the existing GenerateHashValue function

```
76 Console.WriteLine("QUANTITY SOLD:\t\t" + Product[4]);
77 Console.WriteLine("HASH VALUE:\t\t" + GenerateHashValue(ProCode));
```

■ B4

8 marks available for modifying the code as shown (or equivalent code):

Award mark for:

- using TRY-CATCH to intercept exceptions
- using a suitable read method to read successfully
- handling the first array of strings, one per line
- trimming off the new line characters
- splitting where there are commas
- parsing the individual number strings to turn them into longs
- adding the newly read array to a list of arrays
- returning a list of arrays of long integers

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```

2 using System.Collections.Generic;
3 using System.IO; // Required for file handling
4

```

```

95 // B4
96 private static List<long[]> ReadInOldTextFile()
97 {
98     string[] FileLines;
99     try
100     {
101         FileLines = File.ReadAllLines(@"C:\...\Ex9SecA\PRODU
102     }
103     catch (FileNotFoundException fnfex)
104     {
105         File.WriteLine("FILE NOT FOUND!");
106         return null;
107     }
108
109     string[] LineStrings;
110     long[] SingleLineOfNumbers = new long[5];
111     List<long[]> WholeFileAsList = new List<long[]>();
112
113     for (int li = 0; li < FileLines.Length; li++)
114     {
115         LineStrings = FileLines[li].Trim().Split(',');
116         for (int i = 0; i < LineStrings.Length; i++)
117         {
118             SingleLineOfNumbers[i] = long.Parse(LineStrings[i]);
119         }
120
121         WholeFileAsList.Add(SingleLineOfNumbers);
122         SingleLineOfNumbers = new long[5];
123     }
124
125     return WholeFileAsList;
126 }

```

■ B5

3 marks available for modifying the code as shown (or equivalent code):

Marks could be awarded for:

- correct method signature
- iterating through the whole list
- calling the ShowFactFile method, passing each array in the list one at a time

```

81 // B5
82 private static void ShowFactFileOfWholeTable(List<long[]>
83 {
84     for (int pos = 0; pos < WholeFile.Count; pos++)
85     {
86         ShowFactFile(WholeFile[pos]);
87     }
88 }
89

```

In Main():

```

16
17 List<long[]> OldFileContents = ReadInOldTextFile(); /
18 ShowFactFileOfWholeTable(OldFileContents); // B5

```

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■ B6

6 marks available for modifying the code as shown (or equivalent code):

Marks could be awarded for:

- declaring and creating a HashTable variable with the correct data type
- pre-populating the HashTable with 19 empty lists
- calling the existing ReadInOldTextFile() method to gather data from
- finding the hash value for that row
- inserting the row into the correct list in the HashTable
- returning the whole HashTable

```

130 private List<List<long[]>> InitiallyPopulateHashFile()
131
132 // Create the blank hash table
133 List<List<long[]>> HashTable = new List<List<long[]>>();
134
135 // Create 19 empty lists inside the hash table
136 for(int i=0; i<19; i++)
137 {
138     HashTable.Add(new List<long[]>());
139 }
140
141 // Read all records in from text file
142 List<long[]> OldFileContents = ReadInOldTextFile();
143
144 int HashValue;
145
146 // For each record, use its hash value to append it to one of the
147 for(int r=0; r<OldFileContents.Count; r++)
148 {
149     HashValue = (int) GenerateHashValue(OldFileContents[r][0]);
150     HashTable[HashValue].Add(OldFileContents[r]);
151     // tester // Console.WriteLine("> > > > ADDING " + OldFileContents[r][0]);
152 }
153
154 return HashTable;
155 }

```

In Main():

```

19 List<List<long[]>> HashT = InitiallyPopulateHashFile();

```

■ B7

14 marks available for modifying the code as shown (or equivalent code):

Marks could be awarded:

- for calling InitiallyPopulateHashFile to build a HashTable
- for creating an empty array of 19 strings to push out to the file
- for iterating through all rows of the hash table
- for iterating through all elements in the list on each row
- [4] for successfully converting arrays to strings
- for delimiting the different products using the '>' character...
- for ... except at the end of a row
- for adding the line to be written to the array of strings (that will be pushed out to the file)
- for opening the file to write all the data
- for using TRY-CATCH to intercept and handling exceptions
- for a method call from Main()

In Main():

```

22 WriteMigratedData(); // B7

```

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Outside Main():

```

157 // B7
158 private static void WriteMigratedData()
159 {
160     // copied down from Main() method for B7
161     List<List<long[]>> HashT = InitiallyPopulateHashFile(); // original
162
163     // Create an array of strings to push out to the file
164     string[] LinesToBeWritten = new string[77]
165
166     string StringBuiltAtThatLine = "";
167
168     // Iterate through each row of the hash table
169     for (int TableRow = 0; TableRow < HashT.Count; TableRow++)
170     {
171         StringBuiltAtThatLine = "";
172
173         // Convert the list of arrays held there to a string representation
174
175         // Step through each list found there
176         for (int ListPoint = 0; ListPoint < HashT[TableRow].Count; ListPoint++)
177         {
178             StringBuiltAtThatLine = StringBuiltAtThatLine + ConvertArrayToString(HashT[TableRow][ListPoint]);
179             if(ListPoint != HashT[TableRow].Count - 1)
180             {
181                 StringBuiltAtThatLine = StringBuiltAtThatLine + ",";
182             }
183         }
184     }
185 }

```

```

186 // tester // Console.WriteLine("-----[[[ ARRAY ]]]] NOW INCLUDES " + StringBuiltAtThatLine);
187 LinesToBeWritten[TableRow] = StringBuiltAtThatLine;
188 }
189
190 // Open the hash file HASHFILE.txt in WRITE mode
191 try
192 {
193     File.WriteAllLines("C:\\Users\\Owner\\Desktop\\VOCAL A-Level Python to C Sharp Exercises\\SOURCE CODE FILES\\HASHFILE.txt", LinesToBeWritten);
194 }
195 catch (FileNotFoundException ex)
196 {
197     Console.WriteLine("FILE NOT FOUND");
198 }
199 }

```

```

200 private static string ConvertArrayToString(long[] GivenArray)
201 {
202     string StringRep = "";
203     for(int index=0; index<GivenArray.Length; index++)
204     {
205         StringRep = StringRep + GivenArray[index];
206         if(index != GivenArray.Length - 1)
207         {
208             StringRep = StringRep + ",";
209         }
210     }
211
212     return StringRep;
213 }
214 }
215 }

```

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■ B8

3 marks available for modifying the code as shown (or equivalent code):

Marks could be awarded for:

- [1] passing HashT in as a parameter
- [1] no longer declaring HashT inside the method
- [1] removing the call to other method (InitiallyPopulateHashFile)

```

229 // BS
230 private static void UpdateHashFile(ref List<List<long[]>> HashT)
231 {
232     // Create an array of strings to push out to the file
233     string[] LinesToBeWritten = new string[19];
234
235     string BuiltAtThatLine = "";
236
237     // Iterate through all rows of the hash table
238     for (int TableRow = 0; TableRow < HashT.Count; TableRow++)
239     {
240         StringBuiltAtThatLine = "";
241
242         // Convert the list of arrays held there to a string representation
243
244         // Step through each list found there
245         for (int ListPoint = 0; ListPoint < HashT[TableRow].Count; ListPoint++)
246         {
247             StringBuiltAtThatLine = StringBuiltAtThatLine + ConvertArrayTo
248             if (ListPoint != HashT[TableRow].Count - 1)
249             {
250                 StringBuiltAtThatLine = StringBuiltAtThatLine + ">";
251             }
252         }
253
254         LinesToBeWritten[TableRow] = StringBuiltAtThatLine;
255     }
256
257     // Open the hash file HASHFILE.txt in WRITE mode
258     try
259     {
260         File.WriteAllLines("C:\\Users\\...\\Ex9Sec8\\HASHFILE.txt", LinesToBeWritten);
261     }
262     catch (FileNotFoundException fnfex)
263     {
264         Console.WriteLine("FILE NOT FOUND!");
265     }
266 }

```

■ B9

8 marks available for modifying the code as shown (or equivalent code):

Marks could be awarded for:

- [1] for initialising a blank hash table structure as a list of lists of long integers
- [1] for accessing the file and pulling in all data (e.g. using ReadAllLines)
- [1] for applying TRY-CATCH to the file read operation
- [1] for iterating through all file rows and skipping empty rows
- [1] for splitting at the '>' character
- [1] for managing the addition of a new row of arrays to the hash table
- [2] for converting a string to an array of longs (within or as a separate method)

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```

268 // 89
269 private static List<List<long[]>> ReadHashFile()
270 {
271     // Create the blank hash table
272     List<List<long[]>> HashTable = new List<List<long[]>>();
273
274     // Create 19 empty lists inside the hash table
275     for (int i = 0; i < 19; i++)
276     {
277         HashTable.Add(new List<long[]>());
278     }
279
280     // Read in the hash file as an array of strings
281     string[] FileLines = File.ReadAllLines(@"C:\...\Ex9Sec8\HASHFILE.txt");
282
283     // tester // Console.WriteLine("***** Adding *****");
284
285     catch (FileNotFoundException ex)
286     {
287         Console.WriteLine("FILE NOT FOUND!");
288         return null;
289     }
290
291     // Work through each row, firstly splitting it where > occurs (collisions)
292     string[] RowFromHashFile = { };
293     long[] SingleDataRecord = { };
294
295     for(int RowNum=0; RowNum<FileLines.Length; RowNum++)
296     {
297         if(FileLines[RowNum] == "")
298         {
299             continue; // just skip this row entirely as it is empty
300         }
301
302         // row is now represented as an array of more strings (long =
303         RowFromHashFile = FileLines[RowNum].Split('>');
304
305         // Work through each array and dismantle it, adding it to the
306         for (int Num = 0; Num < RowFromHashFile.Length; Num++)
307         {
308             SingleDataRecord = ConvertStringToLongArray(RowFromHashFile[Num]);
309             HashTable[RowNum].Add(SingleDataRecord);
310             // tester // Console.WriteLine("***** Adding *****");
311         }
312     }
313
314     return HashTable;
315 }
316
317 }
318

```

Optional supporting method:

```

216 // 89
217 private static long[] ConvertStringToLongArray(string GivenString)
218 {
219     long[] ProductArray = new long[5];
220     string[] SeparatedValues = GivenString.Split(',');
221     for (int index = 0; index < ProductArray.Length; index++)
222     {
223         ProductArray[index] = long.Parse(SeparatedValues[index]);
224     }
225
226     return ProductArray;
227 }
228

```

In Main():

```

23
24 ReadHashFile(); // 89
25

```

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EXERCISE 10 – REVERSE POLISH

SECTION A

■ A1

1 mark for:

It performs EXCLUSIVE OR on the bits of both operands.

■ A2

1 mark for:

Line 9

■ A3

2 marks (1 mark for explaining that if the given value can be converted into an integer; 1 mark for explaining that the function returns *False* if it fails to convert the value):

The `IsInt` function tries to convert the value into an integer. If the value can be converted into an integer and the function returns *True*. Otherwise, if the value cannot be converted, the `CATCH` block executes and the function returns *False*.

■ A4

2 marks for giving the correct expression (1 mark if the given expression is only partially correct):
 $3 \ 2 + 4 \ 1 - * \ 4 /$

■ A5

2 marks for giving the correct expression (1 mark if the given expression is only partially correct; 1 mark for ignoring redundant brackets):

$(4 + 5) * (3 - 2 / 1)$

■ A6

1 mark for each point up to a maximum of 4:

- [1] It is a FILO (First-In, Last-Out) or LIFO (Last-In, First-Out) data structure.
- [1] Items are added, i.e. pushed, on to the top of a non-full stack.
- [1] Items are removed, i.e. popped, from the top of a non-empty stack.
- [1] Other items in the stack are inaccessible until they are at the top of the stack.
- [1] A stack pointer is a separate integer variable that notes where the top of the stack is.

■ A7

2 marks for giving the correct expression (1 mark if the given expression is only partially correct):
 $6 \ 3 - 2 *$

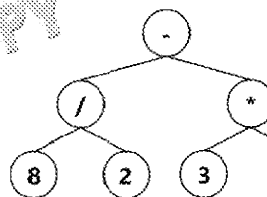
■ A8

2 marks for giving the correct expression (1 mark if the given expression is only partially correct; 1 mark for ignoring redundant brackets):

$(6 - 3) * 2$

■ A9

6 marks (1 mark for each operator that has been given the correct child nodes; 1 mark for each operator that has its child nodes in the correct order, i.e. the left child node being the first operand given and the right child node being the second operand given):



■ A10

6 marks (1 mark for each operator that has been given the correct child nodes; 1 mark for each operator that has its child nodes in the correct order, i.e. the left child node being the first operand given and the right child node being the second operand given):

SECTION B

■ B1

2 marks available for modifying the code as shown (or closely equivalent code):

- [1] for return type
- [1] for parameter part

```
22 private static List<string> ConvertToPostfix(List<string> Elements)
23 {
24 }
```

■ B2

2 marks available for modifying the code (as shown below or closely equivalent code):

[1] per correctly written line

```
25 List<string> Stack = new List<string>(); // B2
26 List<string> OpStack = new List<string>(); // B2
```

■ B3

2 marks available for modifying the code (as shown below):

- [1] for foreach stepping through Elements
- [1] for calling the variable Item

```
30
31 foreach (string Item in Elements)
32 {
```

■ B4

2 marks available for modifying the code as shown (or closely equivalent code):

- [1] for starting calling the IsInteger method
- [1] for using the Add method of the List class

```
31 foreach (string Item in Elements)
32 {
33     // B4
34     if (IsInteger(Item))
35     {
36         Stack.Add(Item);
37     }
38     else
```

■ B5

2 marks available for modifying the code as shown (or closely equivalent code):

- [1] for correctly checking the size of the list
- [1] for reading with the variable LastOp the value at the top of OpStack

```
38     else
39     {
40         // B5
41         if (OpStack.Count != 0)
42         {
43             LastOp = OpStack[OpStack.Count - 1];
44         }
```

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■ B6

11 marks available for modifying the code as shown (or equivalent code):

Marks could be awarded for:

- [2] for the correctly implemented IF statement, [1] of which is for the correct condition
- [1] for using the Add method to push to the OpStack stack/list
- [1] for correctly phrased ELSE IF and its condition
- [1] for setting up the WHILE loop correctly, with Operator pre-set to null
- [1] for implementing a pop operation correctly in two lines of code
- [1] for IF statement dealing with Operator != "(" by pushing Operator to Stack
- [1] for ELSE part containing a nested IF-ELSE
- [1] for IF block correctly adding LastOp to Stack
- [1] for ELSE block popping Item at the END of OpStack, not popping it but overwriting it
- [1] for ELSE block pushing Item to OpStack

```

46 // B6
47 if (OpStack.Count == 0 || Item == "{" || ((LastOp == "+" || LastOp == "-" || LastOp == "*" || LastOp == "/") || LastOp == "("))
48 {
49     OpStack.Add(Item);
50 }
51 else if (Item == "(")
52 {
53     Operator = null;
54     while (Operator != "(" && OpStack.Count != 0)
55     {
56         Operator = OpStack[OpStack.Count - 1];
57         OpStack.RemoveAt(OpStack.Count - 1);
58         if (Operator != "(")
59         {
60             Stack.Add(Operator);
61         }
62     }
63 }
64 else
65 {
66     if (LastOp != "(")
67     {
68         Stack.Add(LastOp);
69         OpStack[OpStack.Count - 1] = Item;
70     }
71     else
72     {
73         OpStack.Add(Item);
74     }
75 }

```

■ B7

4 marks available for modifying the code as shown (or equivalent code):

Marks could be awarded for:

- [1] descending counter implemented in FOR loop
- [1] starting at final element of OpStack
- [1] for pushing to Stack
- [1] for popping from OpStack

```

79 // B7
80 for (int i = OpStack.Count - 1; i >= 0; i--)
81 {
82     Stack.Add(OpStack[i]);
83     OpStack.RemoveAt(i);
84 }
85 return Stack;
86

```

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■ B8

2 marks available for modifying the code as shown (or equivalent code):

Marks could be awarded for:

- [1] for calling `DisplayListOfElements` to show results
- [1] for calling `ConvertToPostfix` to show results

```

11 public static void Main(string[] args)
12 {
13     // B8
14     Console.WriteLine("In infix notation:");
15     DisplayListOfElements(ConvertToInfix(ConvertToPrefix("93 + 28 - 12 / 43 * 5")));
16
17     Console.WriteLine("In Reverse Polish (postfix) notation:");
18     DisplayListOfElements(ConvertToPostfix(ConvertToInfix(ConvertToPrefix("93 + 28 - 12 / 43 * 5"))));
19
20     Console.ReadKey(); // holder
21 }

```

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